



Stijn Van Leuven^{1,2,3}

Pieter De Meutter^{1,3}, Johan Camps¹, Piet Termonia^{2,3} & Andy Delcloo^{2,3}

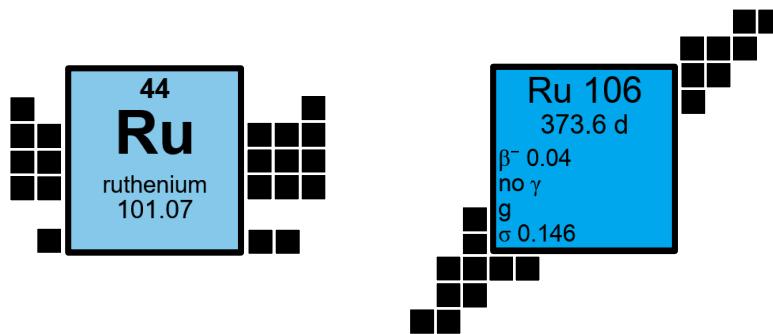
¹ **sck cen**
Belgian Nuclear Research Centre

² GHENT
UNIVERSITY

³ RMI

SOURCE RECONSTRUCTION BASED ON INVERSE MODELLING WITH DEPOSITION MEASUREMENTS

CASE STUDY // Undisclosed ^{106}Ru release in 2017



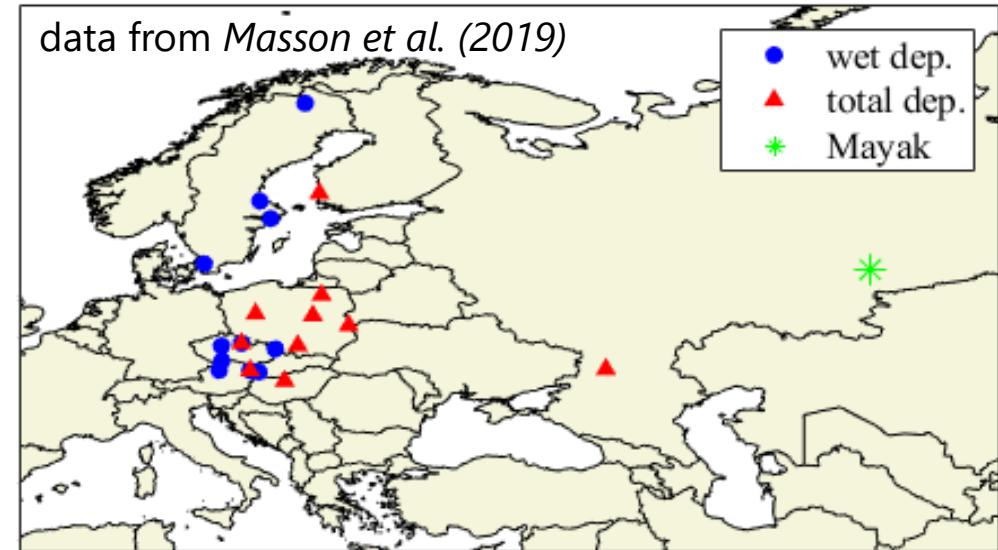
Observations

- September – October 2017
- air concentration (up to 180 mBq/m³) and deposition (up to 90 Bq/m²) in Europe

Source term from previous literature

- location** → Mayak nuclear installation
- release** → 200 – 500 TBq (1.6 – 4 g ^{106}Ru)
- based on air concentration measurements

Location of deposition detections



Research question

Theoretically, can (mobile, cheap) wet deposition measurements be used to complement (fixed, expensive) air concentration measurements for the purpose of inverse modelling?

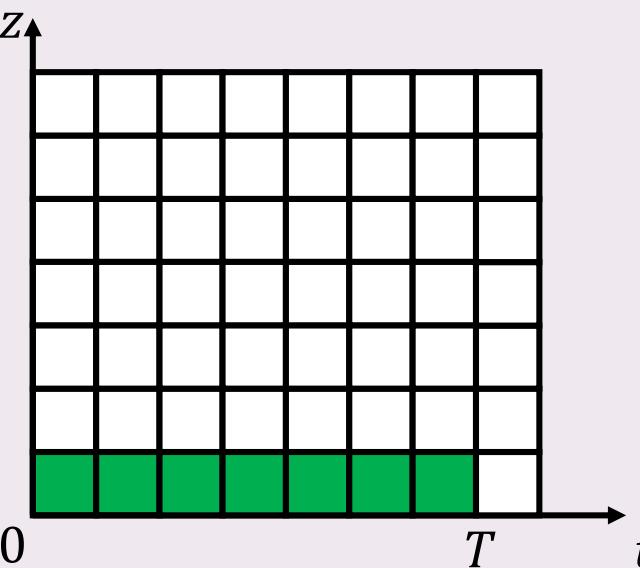
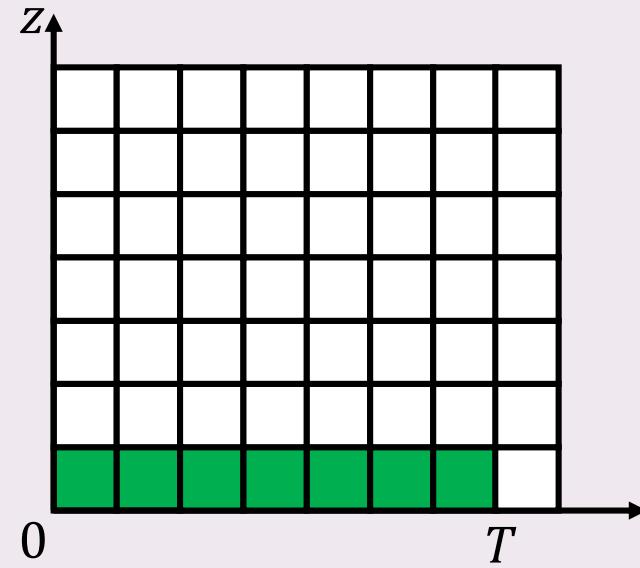
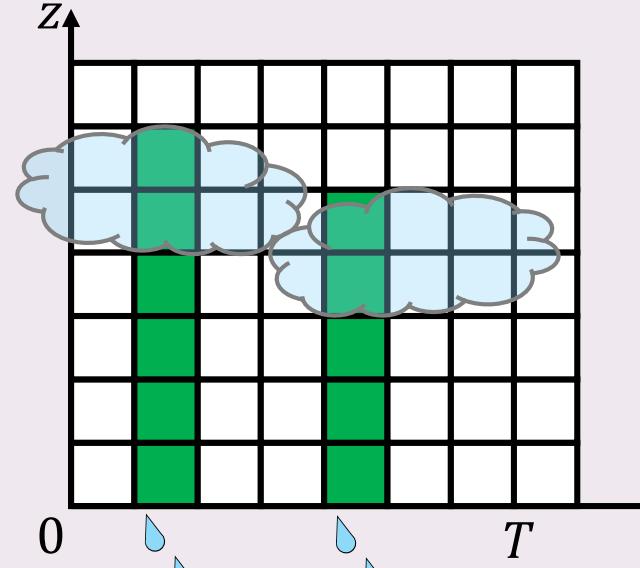
THEORY // Inverse modelling

- **source-receptor-sensitivity** M_{ij} is the sensitivity of **observation** y_i to **source term** x_j

$$y_i = \sum_j M_{ij} x_j$$

- only need to **calculate** M_{ij} 's **once** to generate y_i for any x_j
- we consider y as either **air concentration** (Bq/m^3) or **deposition** (Bq/m^2)
→ different SRS fields M_{ij} for each quantity

THEORY // Air concentration and deposition have different physical implications for inverse modelling

air concentration	dry deposition	wet deposition
$y = \frac{1}{T} \int_0^T c \, dt$ T = measurement window	$y = \int_0^T v_d c \, dt$ v_d = deposition velocity	$y = \int_0^T dt \int_0^h \Lambda c \, dz$ Λ = scavenging coefficient h = height of cloud top
		

MODELS // Flexpart + FREAR

- **ATM → Flexpart v10** (*Pisso et al. 2019*) in backward-in-time mode (*Seibert et al. 2004, Eckhardt et al. 2017*)
- **inverse modelling code → FREAR** (*De Meutter and Hoffman 2020*), open-source FREAR v1

Input	<ul style="list-style-type: none">• SRS fields from ATM (Flexpart)• environmental observations (air concentration)
Methods	<ul style="list-style-type: none">• cost function optimisation• Bayesian inference• possible source region• field of regard
Output	<p>Source term</p> <ul style="list-style-type: none">• release location (probability)• release amount• release timing

More info at
• H22-066
(presentation)
• H22-079
(poster)

OBJECTIVES // Adding deposition to FREAR

- **FREAR v1** uses activity air concentration

$$c = M_c \cdot x$$

- **new implementation** for this study

$$\begin{bmatrix} c \\ d_{\text{wet}} \\ d_{\text{dry}} \\ d_{\text{tot}} \end{bmatrix} = \begin{bmatrix} M_c \\ M_{d_{\text{wet}}} \\ M_{d_{\text{dry}}} \\ M_{d_{\text{tot}}} \end{bmatrix} \cdot x$$

→ inverse modelling with multiple types of measurements **simultaneously!**
(any combination)

METHODS // Experiments

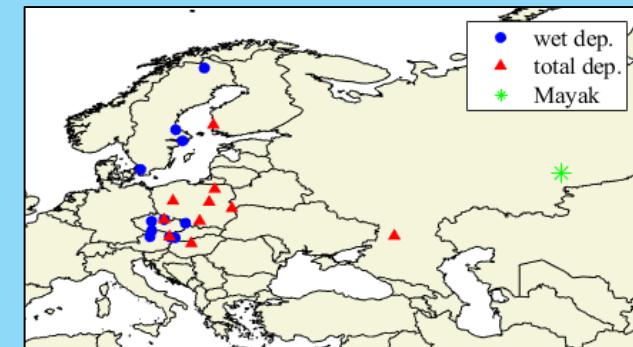
Twin experiment

1. forward ATM calculation with ^{106}Ru source term
(*Saunier et al. 2019*)
2. generate synthetic observations
3. inverse modelling with synthetic observations

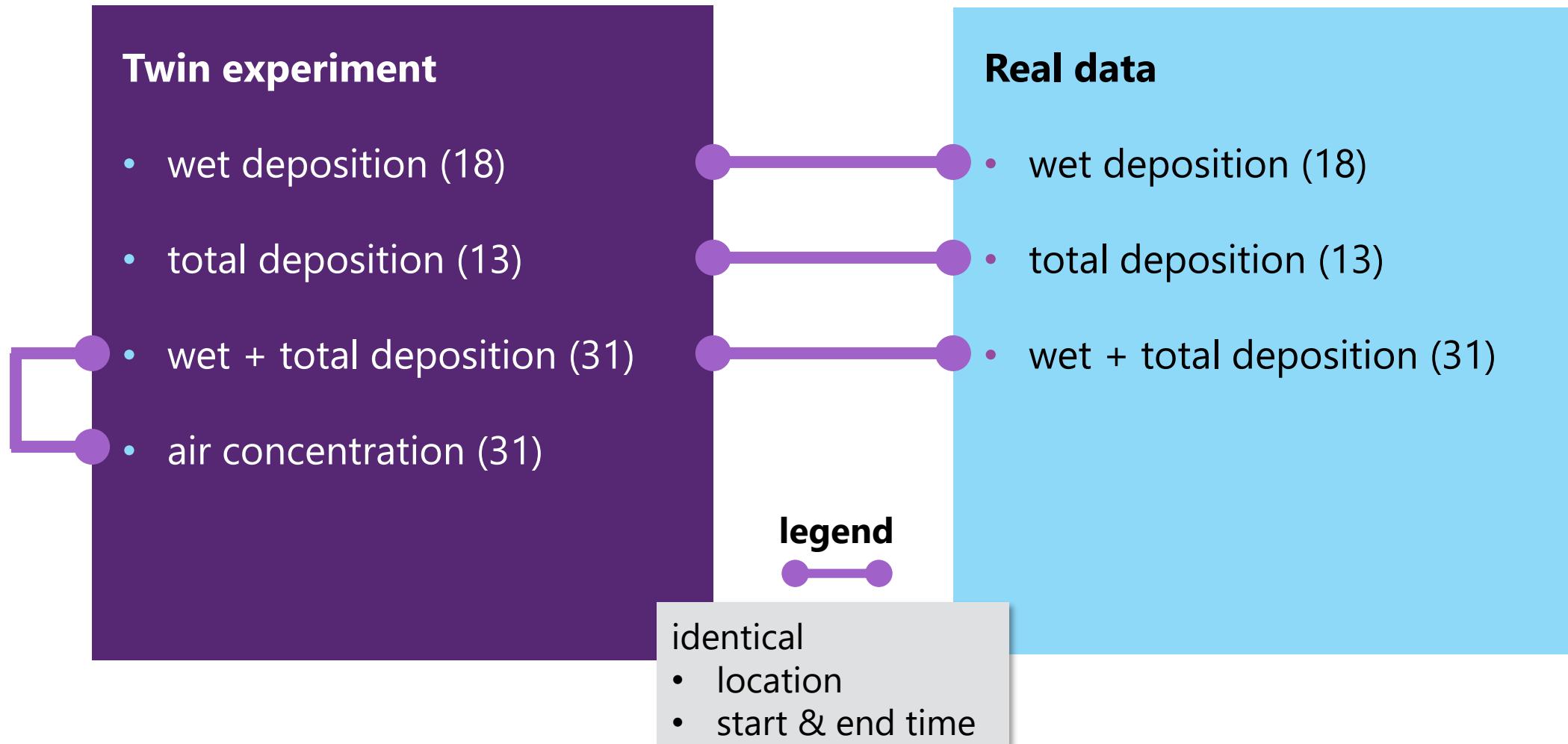
→ eliminates model- & observational errors

Real data

- inverse modelling with real observations
- observational data from *Masson et al. (2019)*

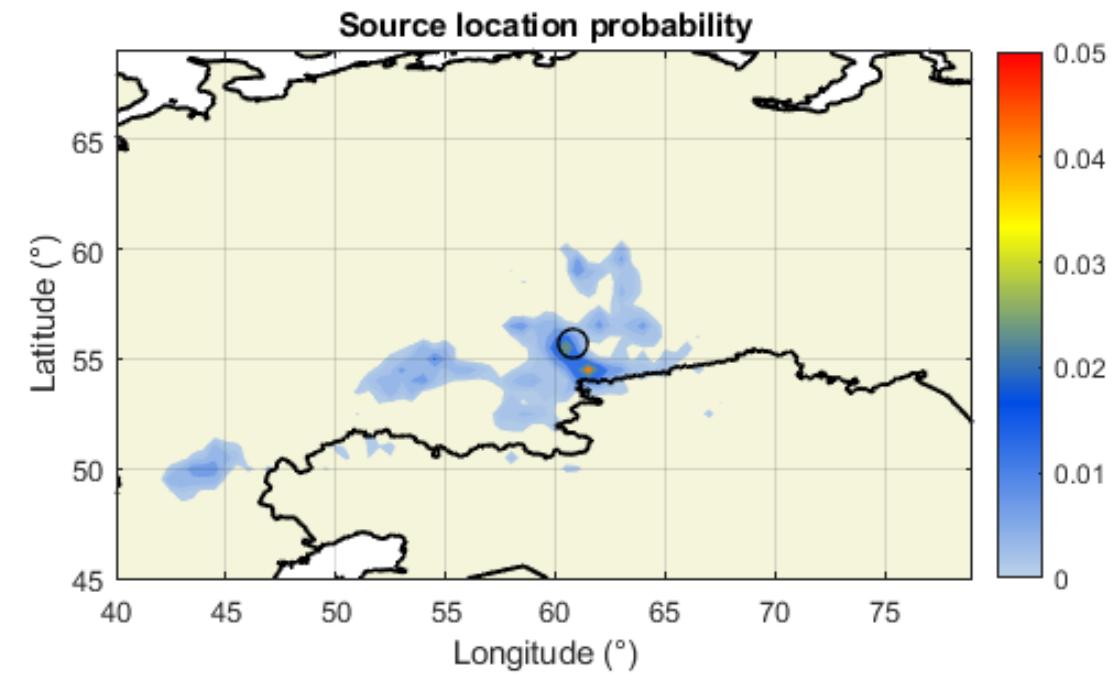
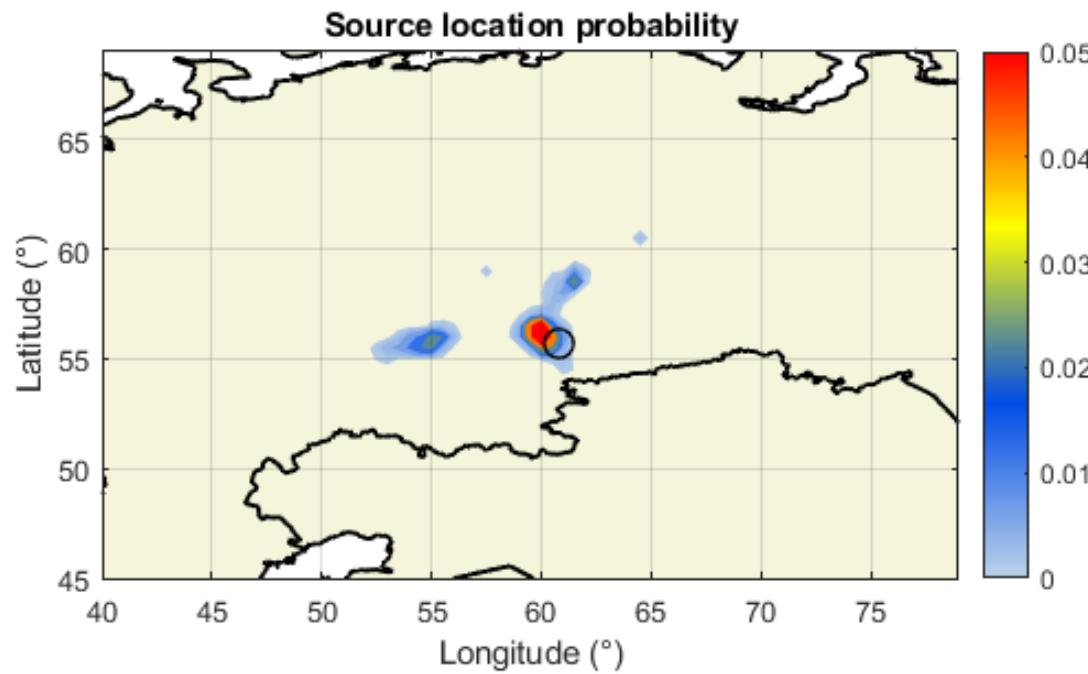


METHODS // Observations per experiment



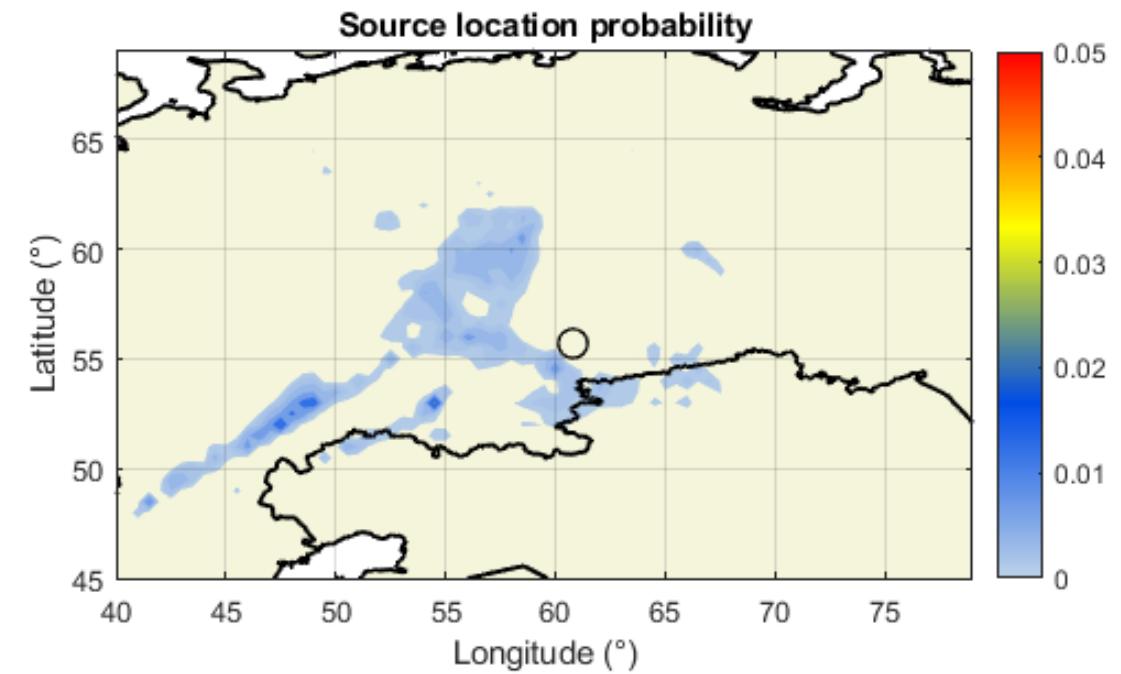
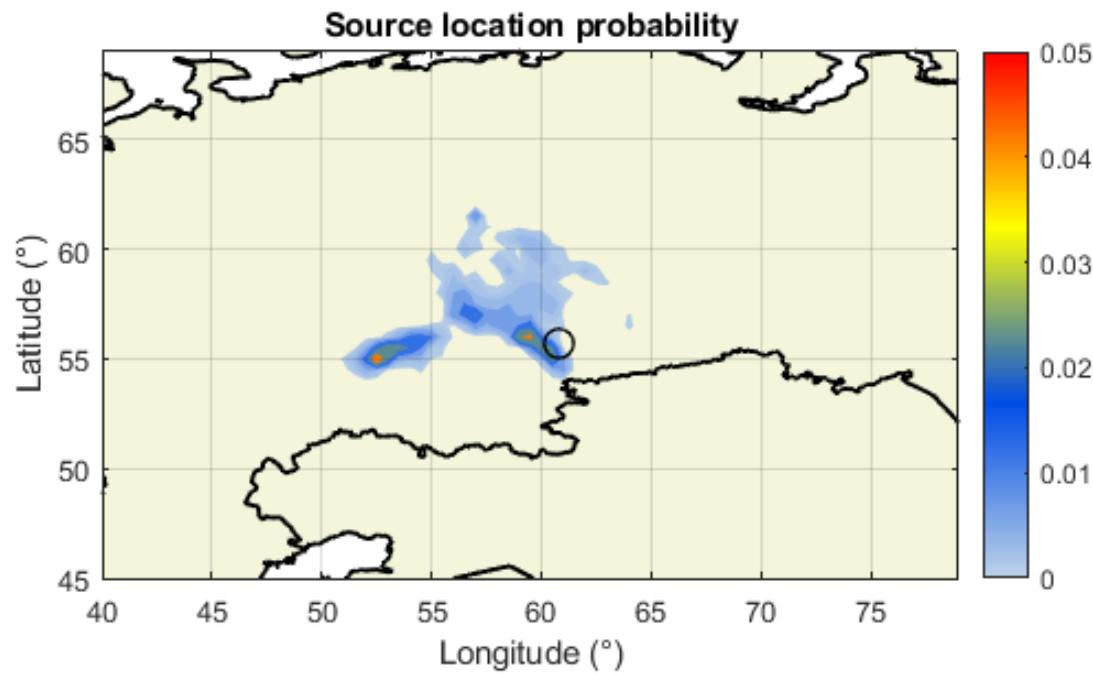
Bayesian inference

Wet deposition



Bayesian inference

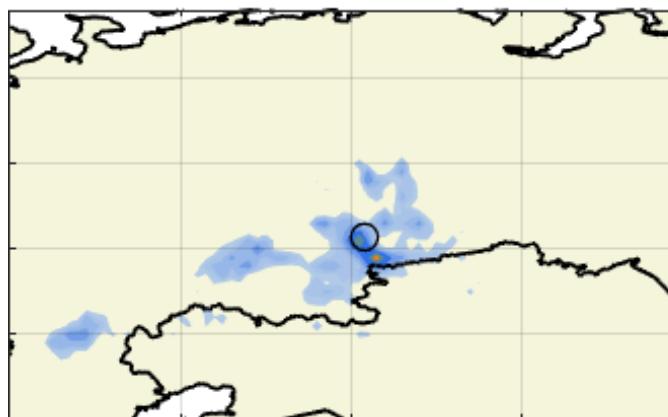
Total (wet+dry) deposition



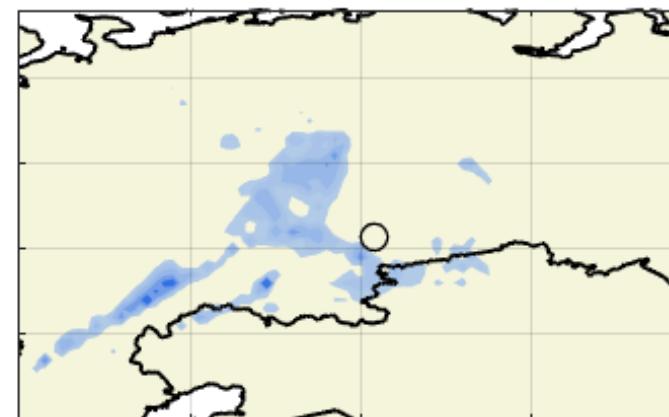


Bayesian inference

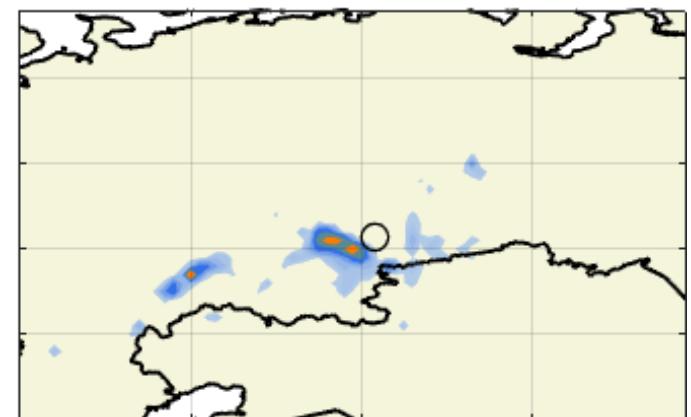
wet deposition



total deposition



wet + total deposition

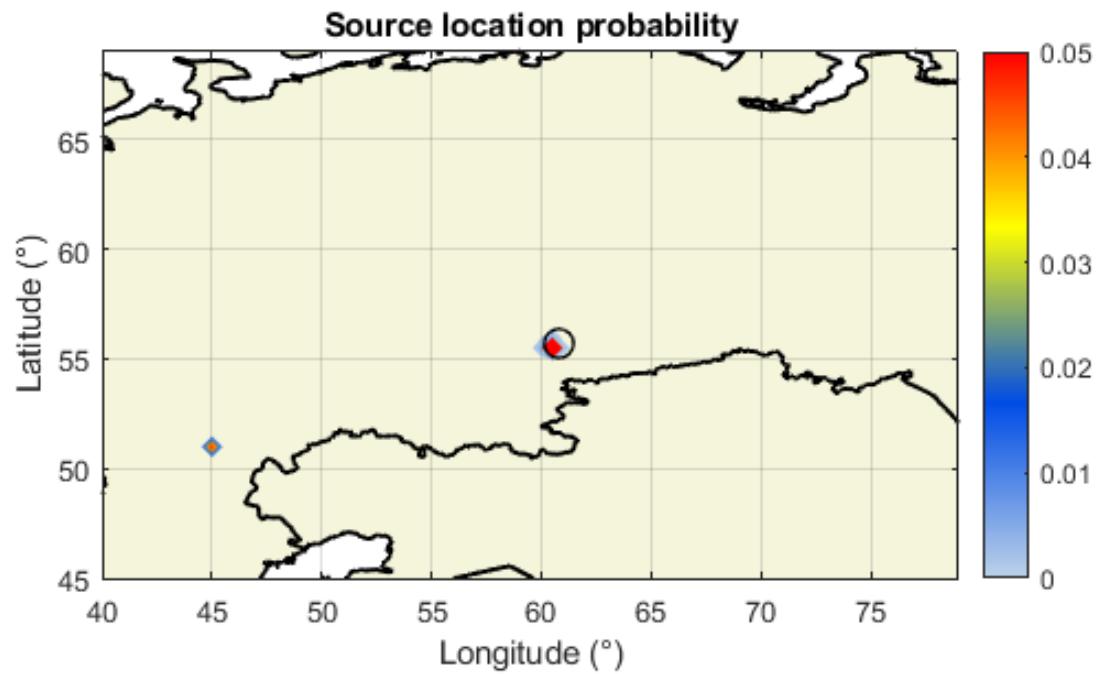


Twin experiment

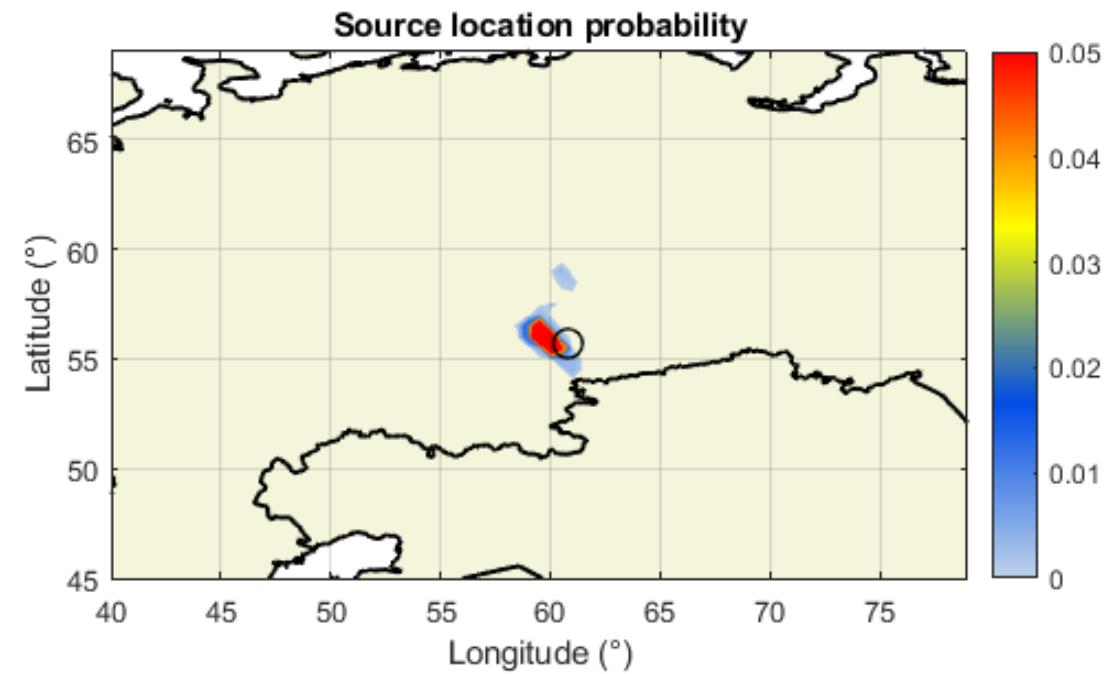
Bayesian inference



Air concentration



Wet + total deposition



CONCLUSIONS

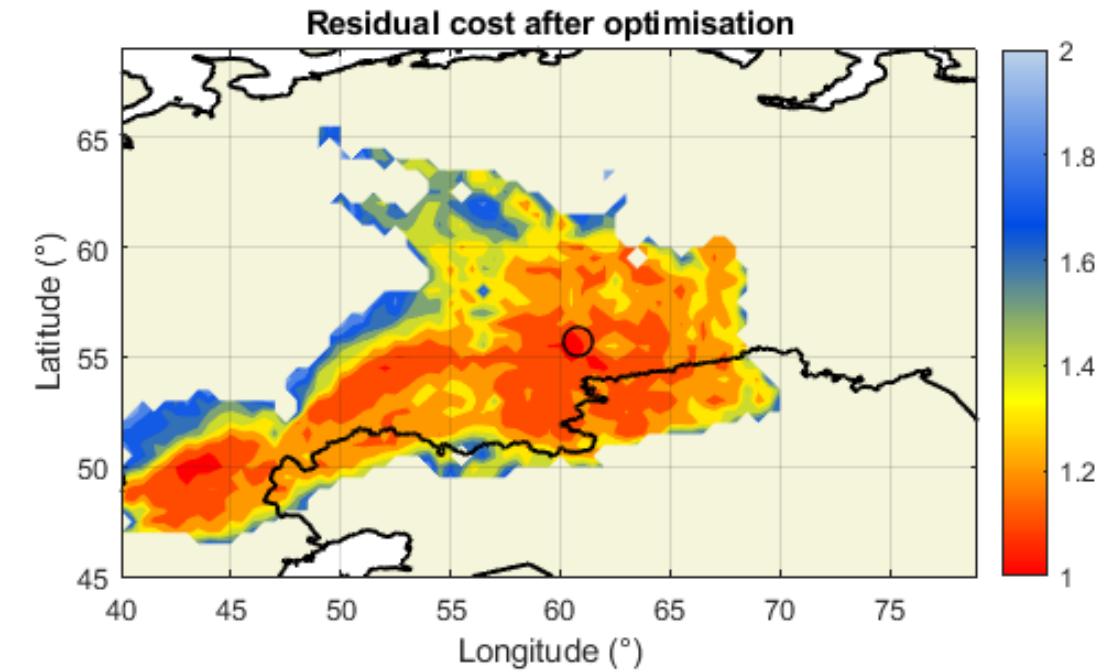
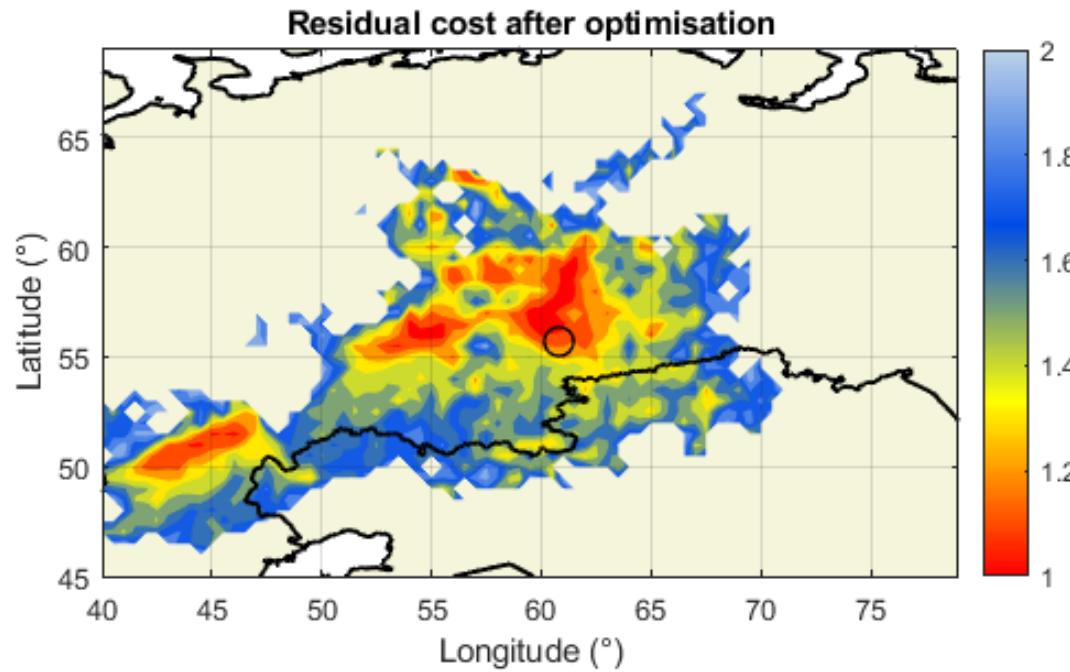
- ✓ Source reconstruction & localisation with deposition measurements is possible.
- ✓ This demonstrates that (mobile, cheap) wet dep measurements can theoretically be used to complement (fixed, expensive) air concentration measurements for the purpose of inverse modelling.
- ✓ Wet deposition measurements seem to contain less 'information' compared to air concentration (see twin experiment), but still provide very good results (see real data).
- ✓ Localisation with real data of total deposition seems to work less well (in this case + dataset).

REFERENCES

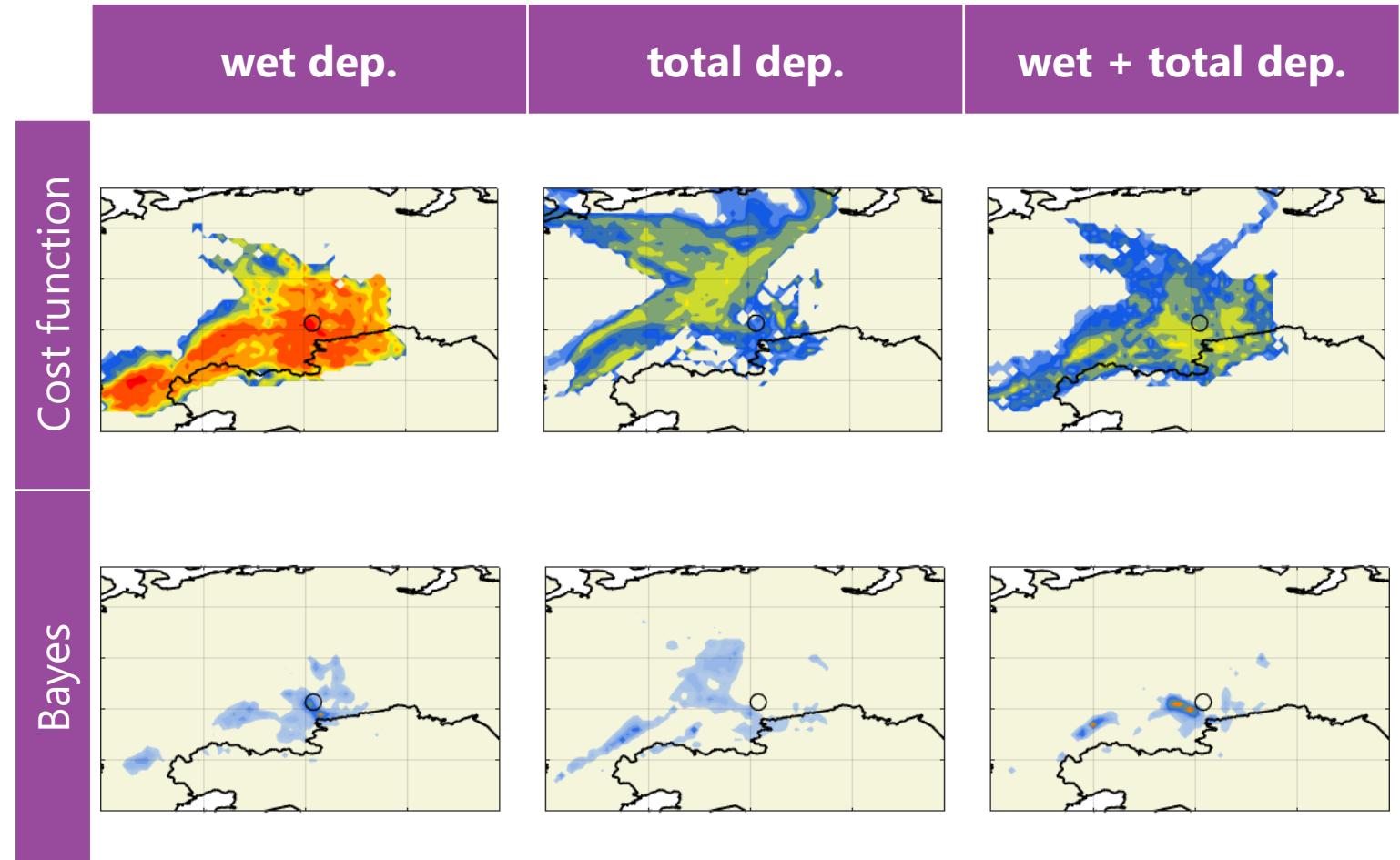
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Wet deposition

Cost function optimisation



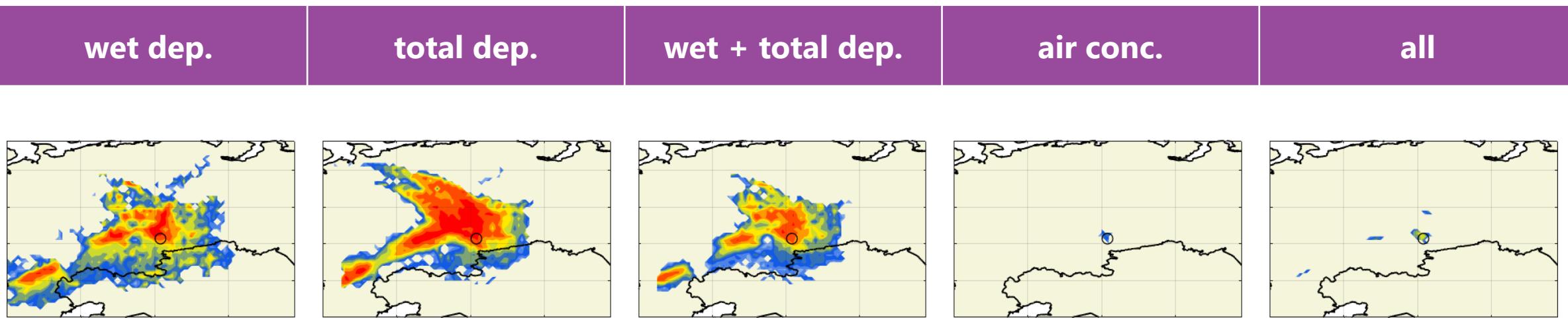
Real data



Twin experiment



Cost function



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