

# ENHANCING URBAN AIR POLLUTION MODELLING THROUGH A NETWORK SCIENCE APPROACH

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Politecnico  
di Torino



ÉCOLE  
CENTRALE LYON

Imperial College  
London

# What is the optimal place to reduce transport emissions?

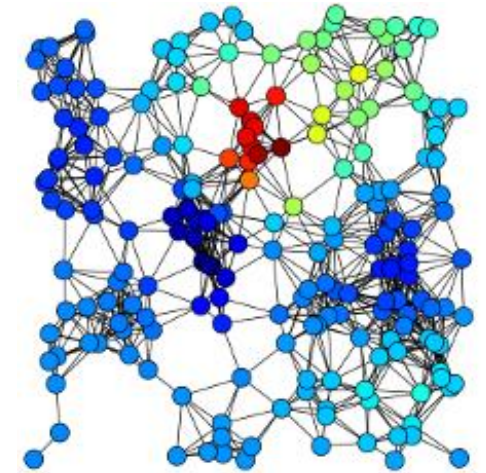
Photo by Gabriel Bouys/AFP



AIR QUALITY PLANS TO MEET AIR QUALITY STANDARDS IN CITIES

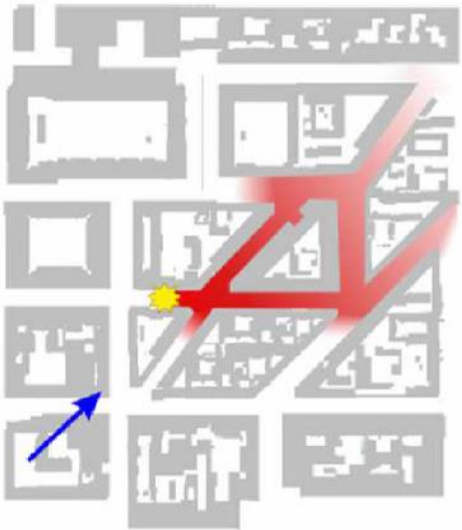


WHERE TO IMPOSE TRAFFIC RESTRICTIONS?

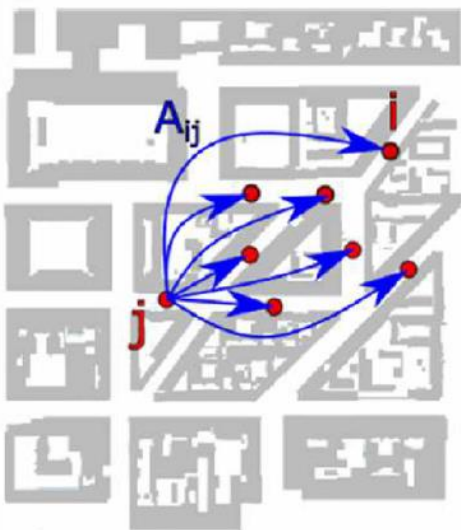


NETWORK APPROACH

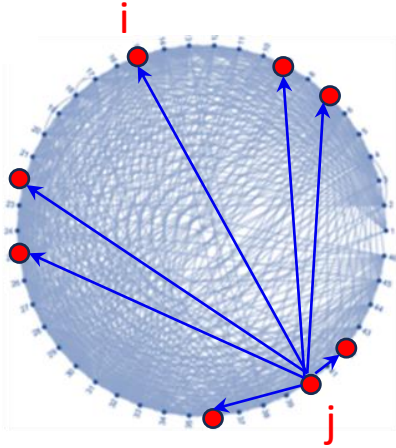
# Network representation



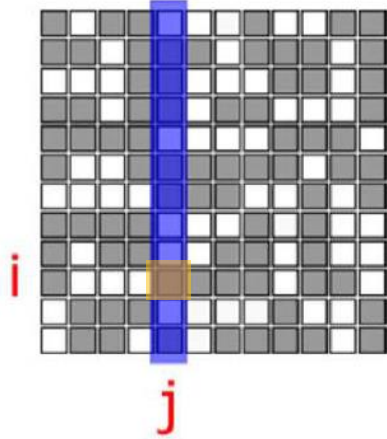
Dispersion from an emission source



The emission-receptor network



Streets  $\rightarrow$  Nodes  
Emission-Impact  $\rightarrow$  Links

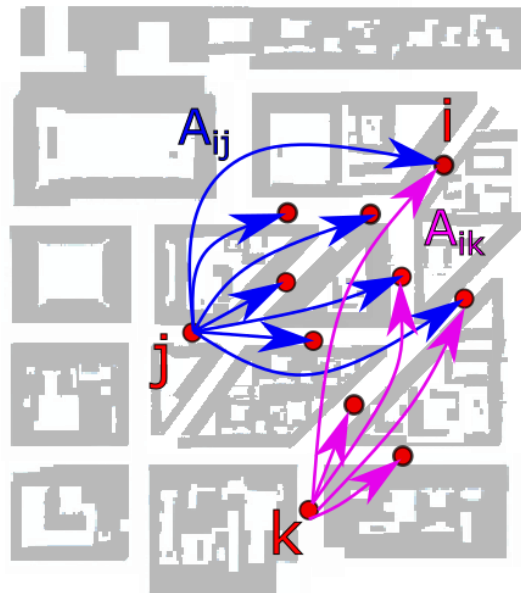


The weight matrix  $A$

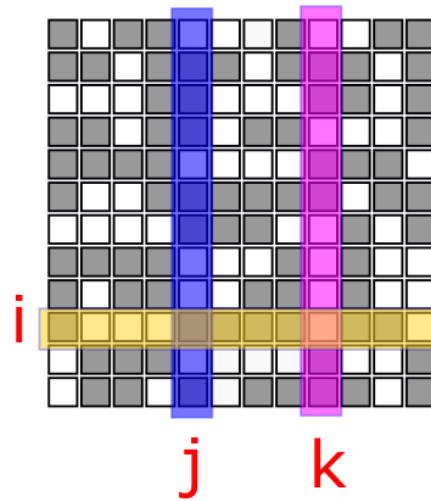
Emission-Impact  
quantification



# The linear assumption



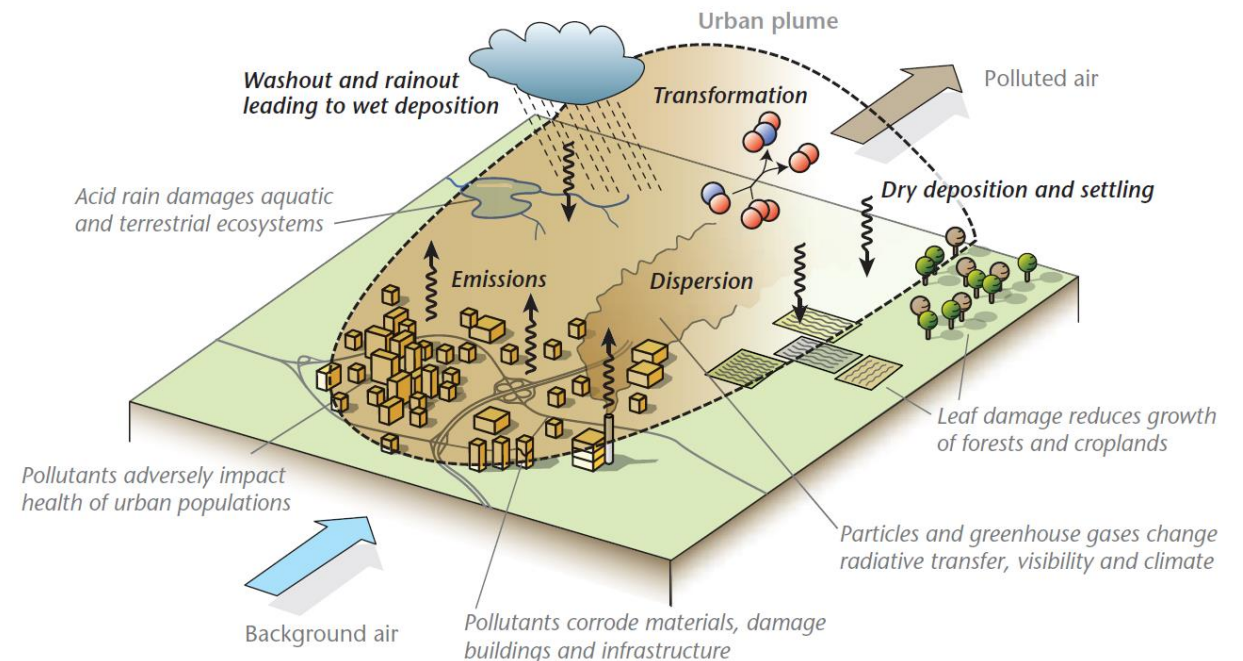
Weight matrix



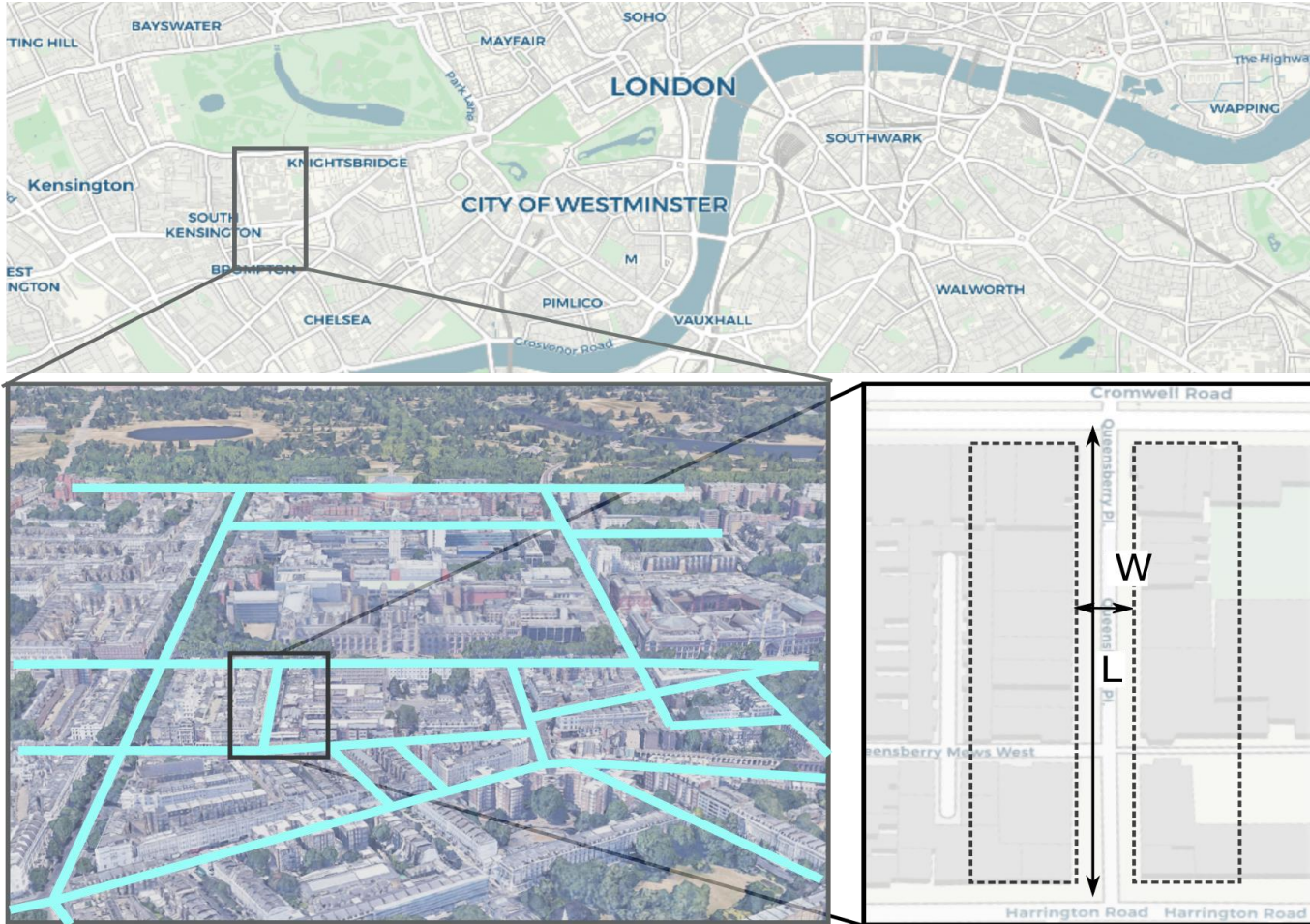
$$C = AQ \quad ?$$

**Linear relation  
between emissions  
and concentrations in  
the street network**

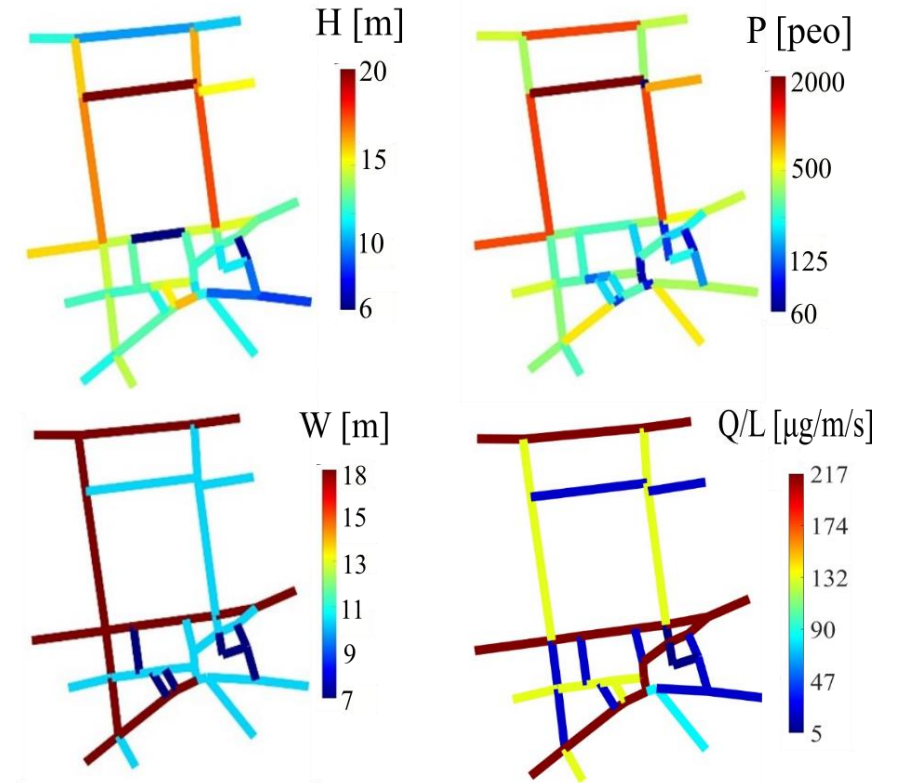
$$C_i = A_{ij}Q_j + A_{ik}Q_k$$



# South Kensington case study



46 streets  $\rightarrow$  46 nodes  $\rightarrow$  46x46 matrix **A** and **E**

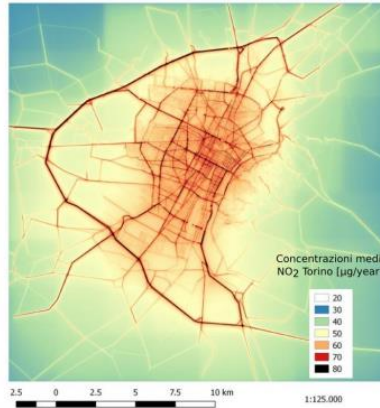


Average values of NOx emissions for 2021 from traffic simulation software and emission model

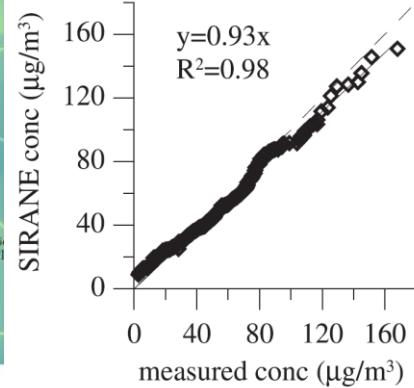


# Building matrix A

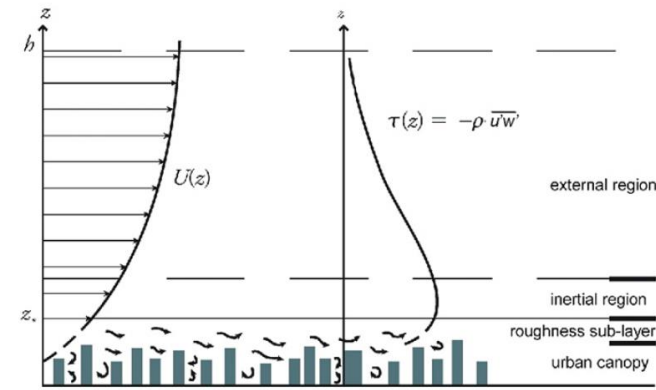
SIRANE software: NO<sub>2</sub> concentration in the city of Lyon



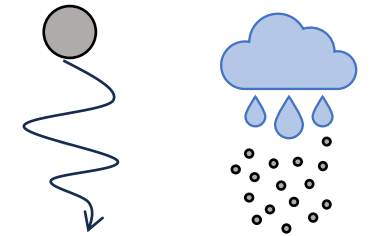
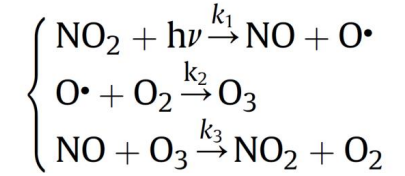
Validation in Lyon (NO<sub>2</sub>)



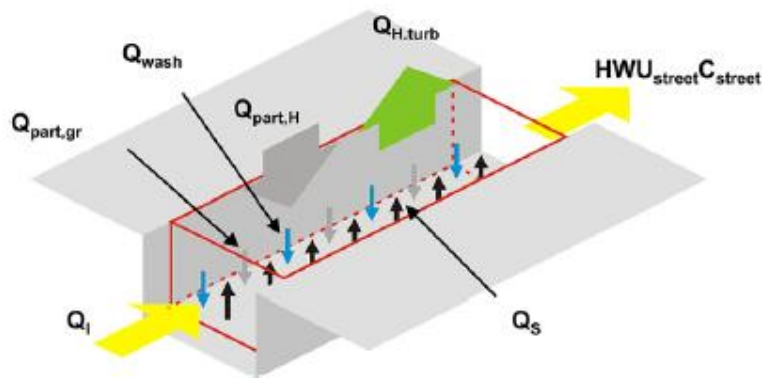
## METEOROLOGICAL PREPROCESSOR



## PHYSICO-CHEMICAL PROCESSES

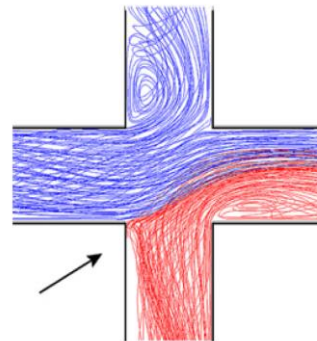


## MASS BALANCE IN EACH STREET CANYON



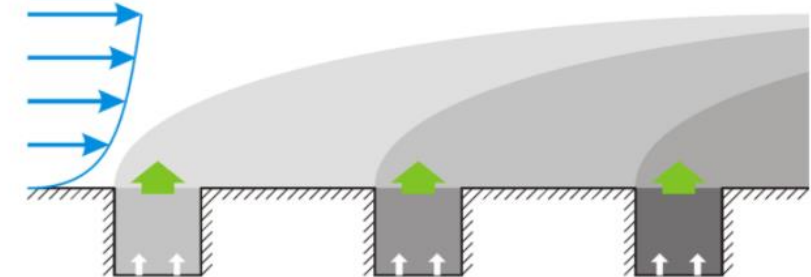
$$Q + Q_I = Q_{H,turb} + Q_{adv} + Q_{part} + Q_{wash}$$

## EXCHANGE MODEL AND MASS BALANCE IN STREET INTERSECTIONS



$$Q_{I,j} = \sum_i P_{i,j} (\phi_0) C_{street_i} + P_{ext \rightarrow j} C_{I,ext}$$

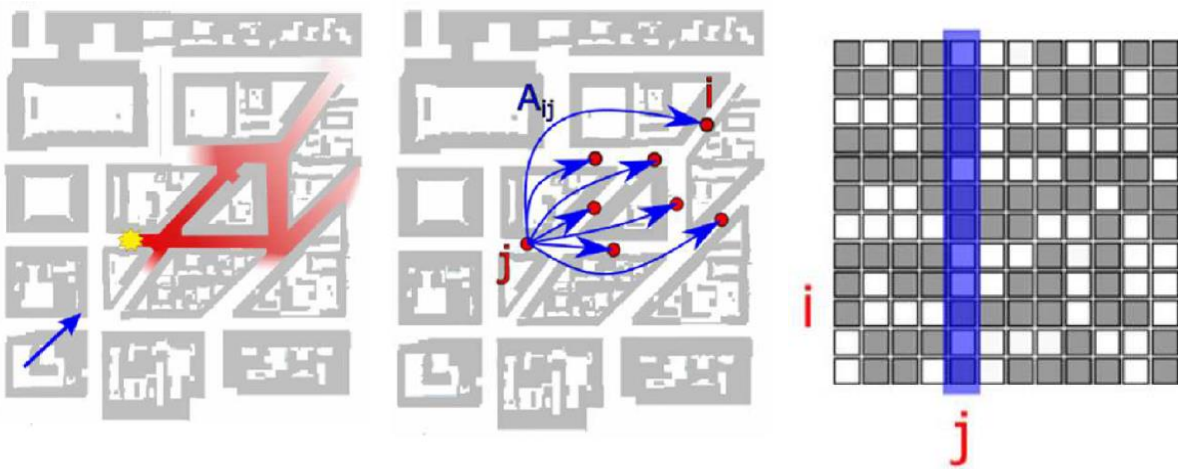
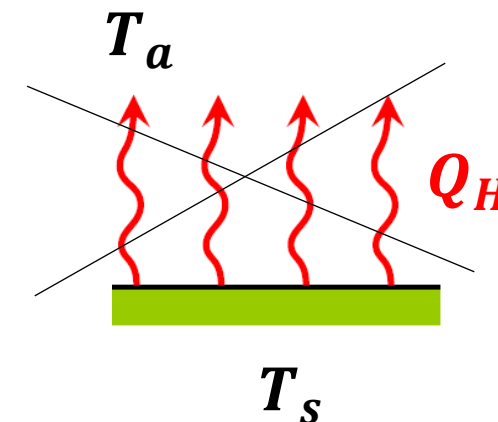
## GAUSSIAN PLUME MODEL ABOVE ROOF LEVEL



# Building matrix A



- **Inert** tracer emission (O<sub>3</sub>+ Night+ No precipitation)
- Null **background** concentration
- **Neutrally** stratified boundary layer → Albedo=1
- External **wind**  $U_0, \Phi$



- **Unit** passive scalar emission from street  $j$  ( $Q_j = 1$ )  
↓  
column  $j$  is filled ( $C_j$ )
- 1 h simulation for **each**  $j$  to fill the entire matrix  $A(U_0, \phi)$
- Simulations are repeated for **8 wind directions**

Emission-Impact matrix A

$$C = AQ$$

# Building the exposure matrix E



People in a street ( $p_i$ )

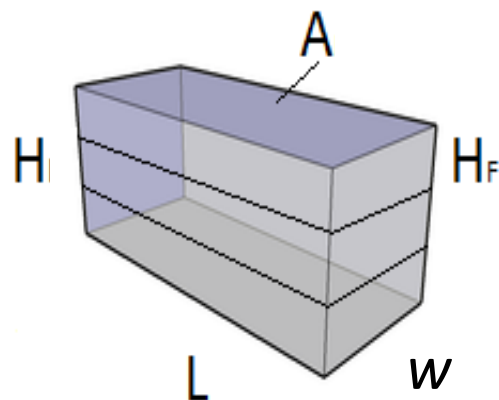
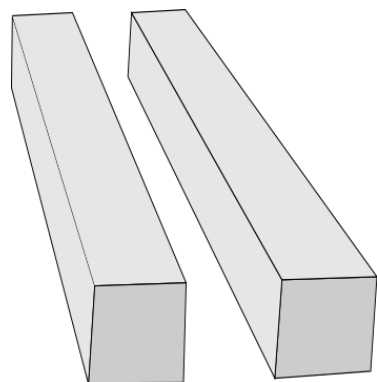
$$S_i = 2 \frac{H_i L_i w}{H_F}$$

Total living space  
for street

$$S_p = \frac{\sum_j 2H_j L_j w / H_F}{n_{TOT}}$$

Living space for  
a resident

$$p_i = 2 \frac{H_i L_i w}{H_F} \frac{n_{TOT}}{2 w \sum_j H_j L_j / H_F} = \frac{H_i L_i}{\sum_j H_j L_j} n_{TOT}$$



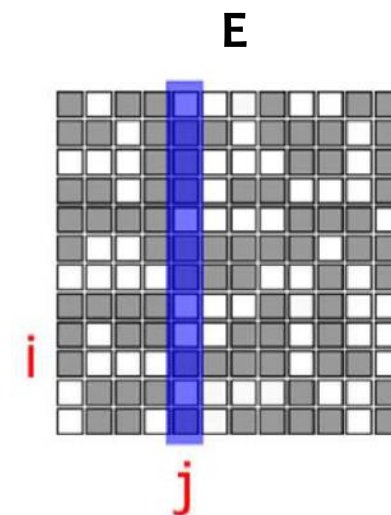
Exposure matrix E

$$e_i = q p_i C_i \quad [\text{g/h}]$$

$$\mathbf{e} = \mathbf{q} \mathbf{p} \circ \mathbf{C} = \mathbf{q} \mathbf{p} \circ \mathbf{A} \mathbf{Q} = \mathbf{E} \mathbf{Q}$$

Inhalation rate

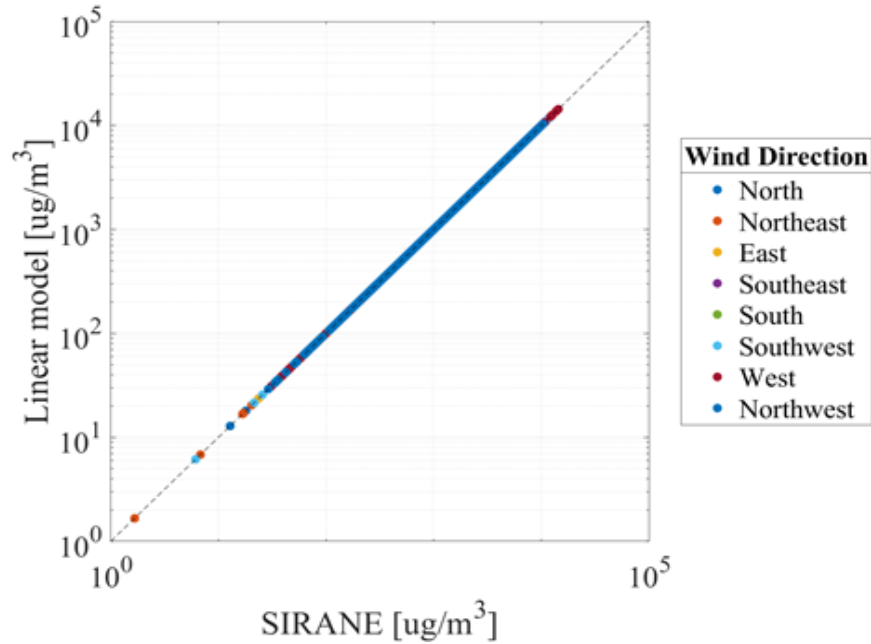
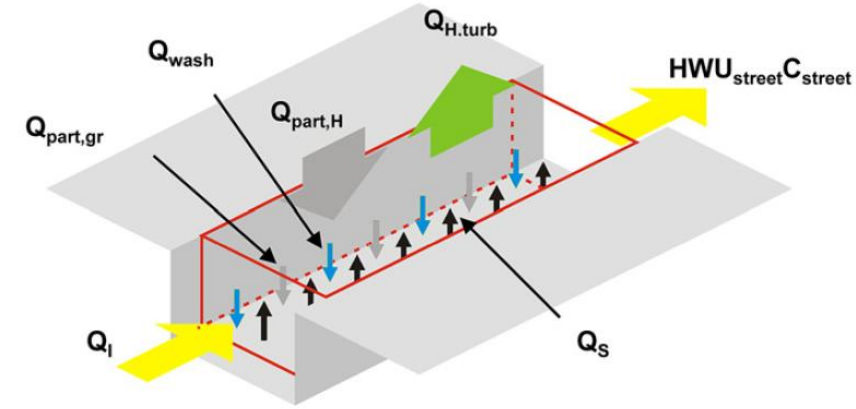
$$(q = 0.57 \frac{\text{m}^3}{\text{h}})$$





# Testing the linear assumption for the inert scenario

- I. Construction of matrix  $A(U_0, \Phi)$
- II. Random  $n$  emissions  $Q$  and find  $C$  with **linear model**:  $C = A Q$
- III. Simulations with **SIRANE** for same  $Q$
- IV. Comparison** of concentrations
- V. Test repeated 20 times for each  $\Phi$



Why does the linear assumption hold?

$$Q + Q_I = Q_{H,turb} + Q_{adv} + \cancel{Q_{part}} + \cancel{Q_{wash}}$$

Negligible re-entrainment from roofs

$$Q + U_S W H C_{up} = u_d W L C + U_S W H C$$

$$C_{up} \propto Q$$

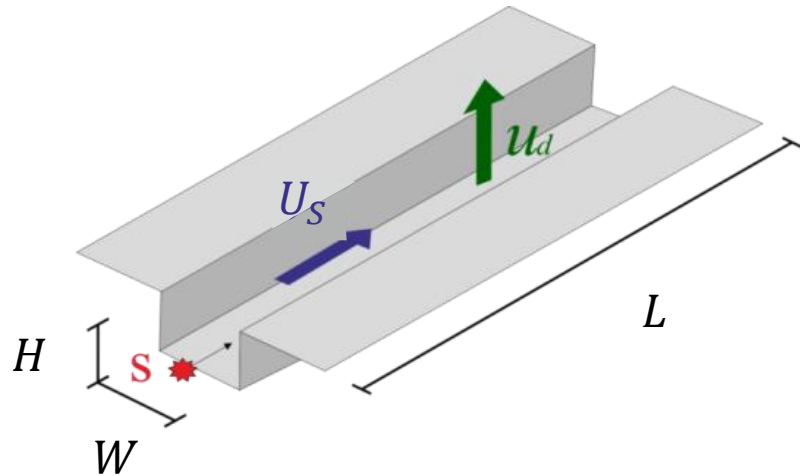
! Once matrix  $A(U_0, \Phi)$  is built, all the possible emission scenarios in the city can be easily computed!

# Wind speed correction

$$C = A Q$$

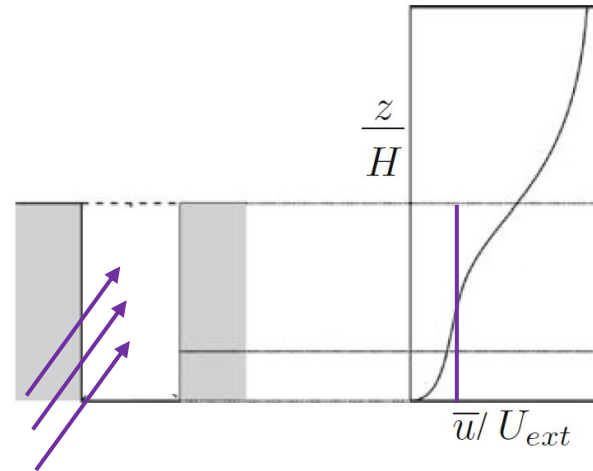
$$A(U_0, \Phi)$$

$$Q + U_S W H C_{up} = u_d W L C + U_S W H C$$



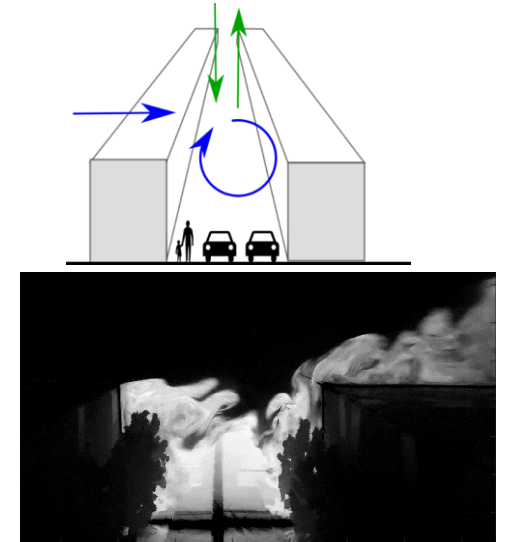
Longitudinal mean velocity  
in a street canyon

$$U_S \propto u_*$$



Vertical exchange  
velocity at roof level

$$u_d \propto \sigma_w \propto u_*$$



$$U_S, u_d \propto u_* \propto U \rightarrow A \propto \frac{1}{U}$$

$$A(U, \Phi) = \frac{U_0}{U} A_0(\phi)$$

Dispersion matrix  
for a general wind  
intensity

# Wind speed correction

- I. Construction of one matrix  $A_0(\Phi)$  for **single wind intensity**  $U_0$
- II. Construction of matrix  $A(U, \Phi)$  using wind correction:

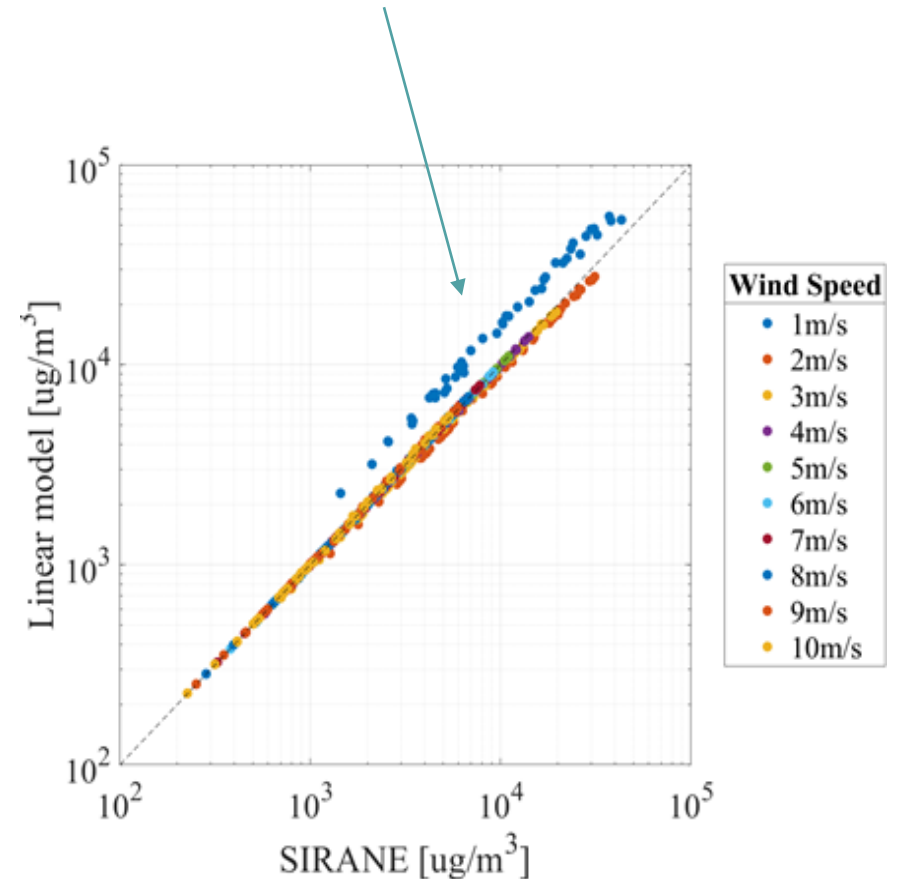
$$A(U, \Phi) = \frac{U_0}{U} A_0(\phi)$$

- III. Random n emissions  $\mathbf{Q}$  and find  $\mathbf{C}$  with **linear model**:

$$\mathbf{C} = \mathbf{A}\mathbf{Q}$$

- IV. Simulations with **SIRANE** for same  $\mathbf{Q}$  and *simulating different  $U$*
- V. **Comparison** of concentrations
- VI. For each  $U$  simulations are **repeated** for different wind directions  $\Phi$

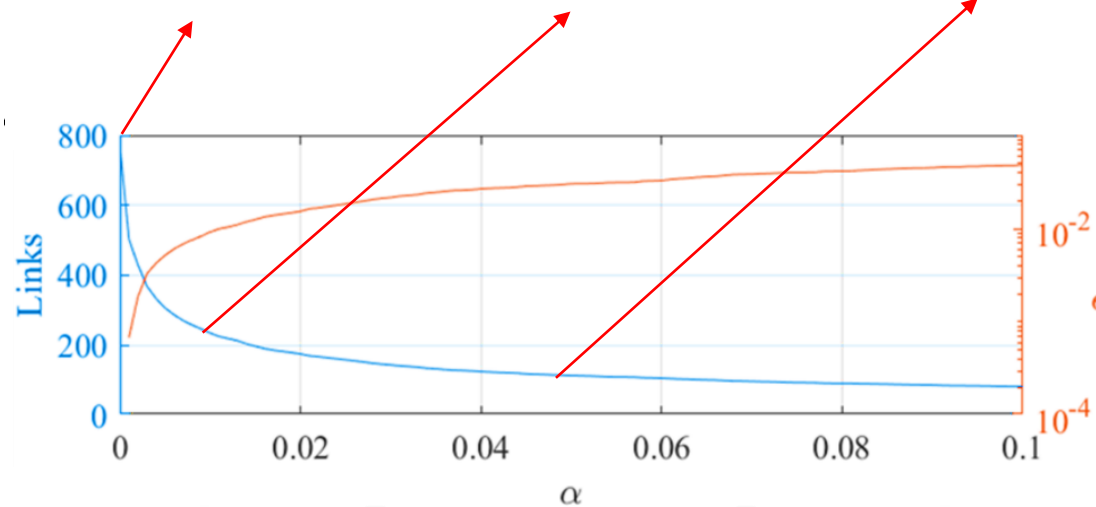
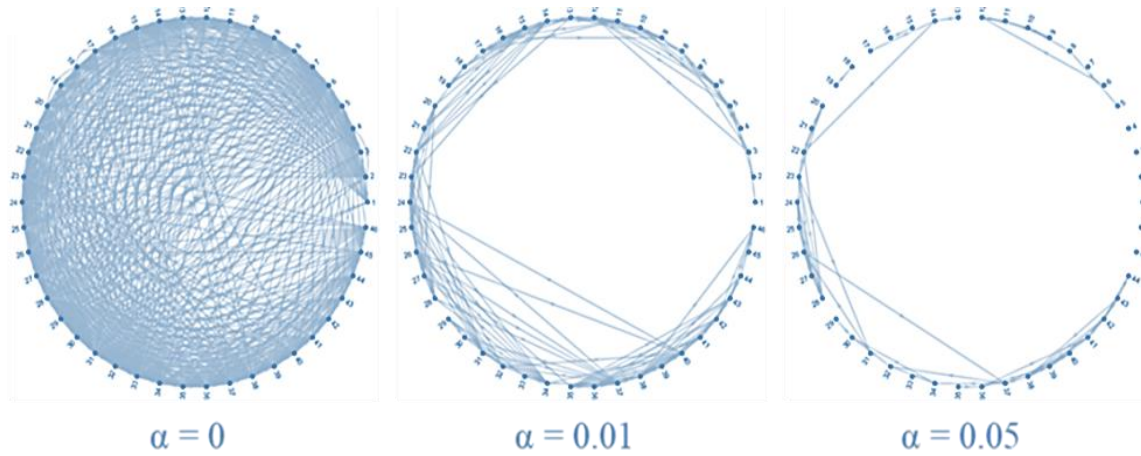
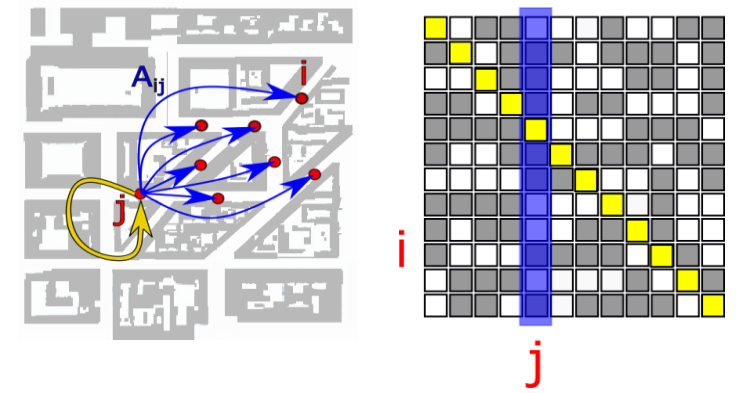
SIRANE prescribes a minimum  $u_*$



- ! Once a single matrix  $A_0(\Phi)$  is built, all the possible emission scenarios in the city can be easily computed also for different wind intensities!



# Reducing network complexity



Simplified matrix  $\check{A}$

$$\check{A}_{ij} = \begin{cases} A_{ij}, & \text{if } A_{ij} > \alpha \left( \prod_{i=1}^N A_{ii} \right)^{\frac{1}{N}} \\ 0, & \text{otherwise} \end{cases}$$

Error in reducing complexity

$$\epsilon = \frac{\|C - \check{C}\|_2}{\|C\|_2} = \frac{\|(A - \check{A})Q\|_2}{\|AQ\|_2} \approx \frac{\|A - \check{A}\|_2}{\|A\|_2}$$

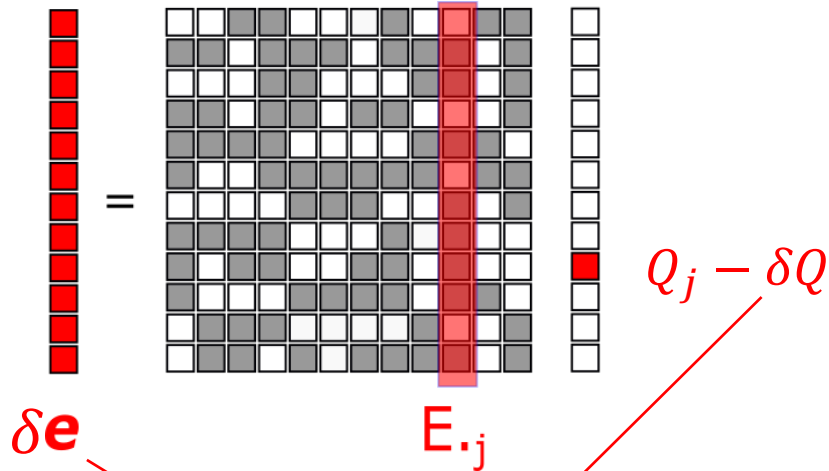
! The number of links in the network can be severely reduced without significantly alter the results.

# Where to reduce emissions?

Perturbation of emission-exposure model

$$e = qp \circ C = qp \circ AQ = EQ$$

$$\delta e = E\delta Q$$



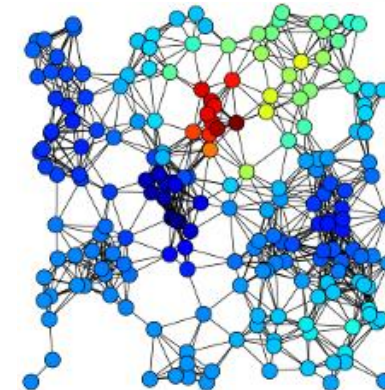
$$R_j = - \sum_i \delta e_i = \delta Q \sum_i E_{ij}$$

Total exposure reduction obtained by reducing emission in **street j**

Outdegree of node j

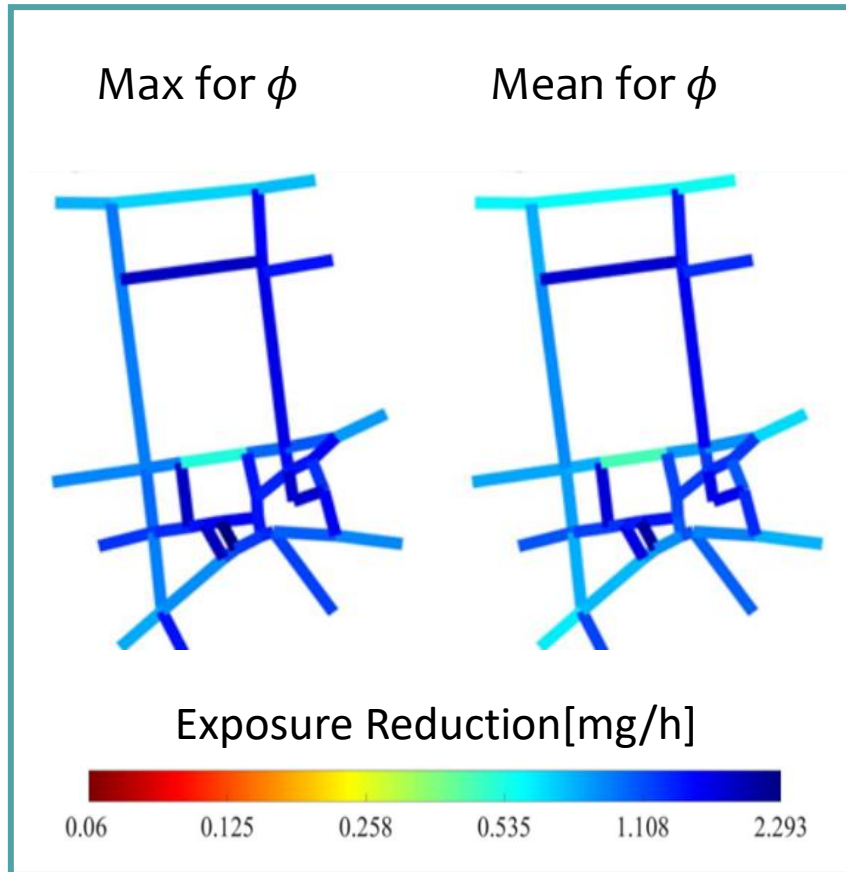


OUTDEGREE  
in NETWORK  
SCIENCE



# Where to reduce emissions?

$$R_j = - \sum_i \delta e_i = \delta Q \sum_i E_{ij}$$

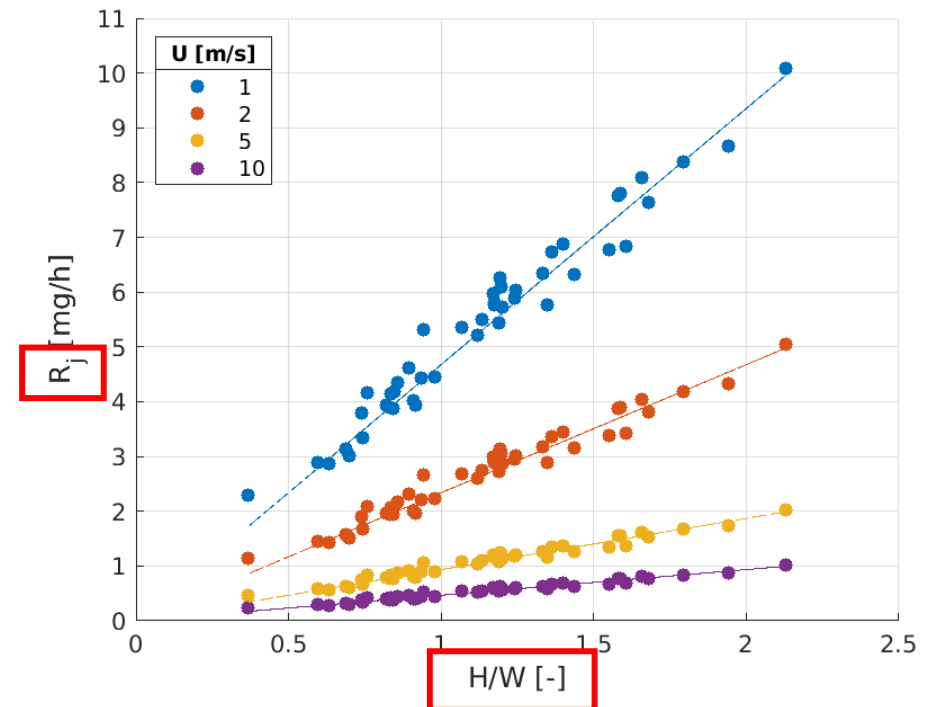


Weak dependence on wind direction  
since A is diagonally dominant

$$R_i \approx \delta Q E_{ii} = \delta Q q p_i A_{ii} = \delta Q q p_i \frac{U_0}{U} A_{0,ii}$$

$$Q_i + \cancel{U_{s,i} W_i H_i C_{i,up}} = u_{d,i} W_i L_i C_i + \cancel{U_{s,i} W_i H_i C_i} \longrightarrow A_{0,ii} = \frac{1}{u_d W L}$$

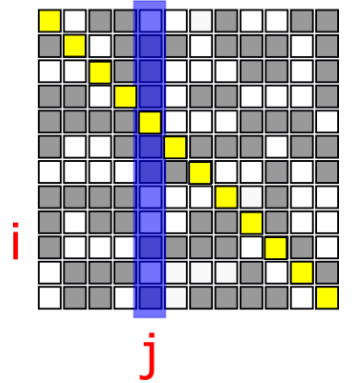
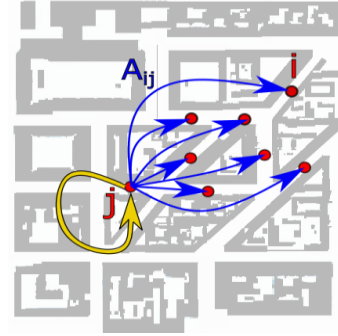
$$R_i \approx \delta Q E_{ii} = \frac{U_0}{U} \frac{\delta Q q n_{TOT}}{u_{d0} \sum_j H_j L_j} \frac{H_i}{W_i}$$



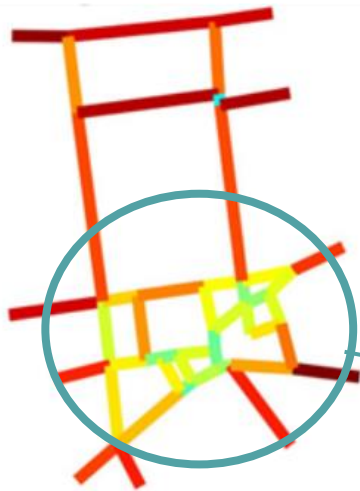


# Where to reduce emissions?

Consider all the connections except the **self-interactions**



Mean for  $\phi$   
(no self-interactions)



$$R_j = - \sum_i \delta e_i = \delta Q \sum_i E_{ij}$$

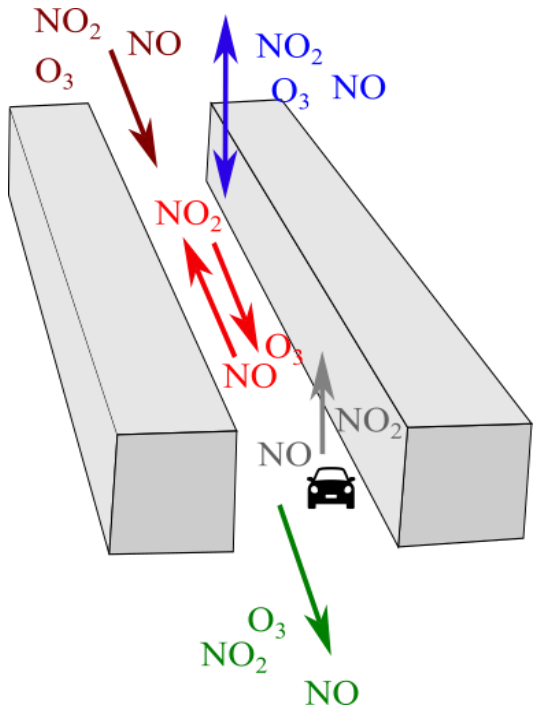
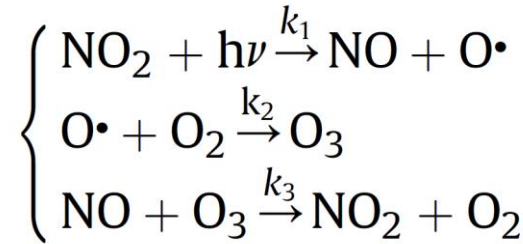
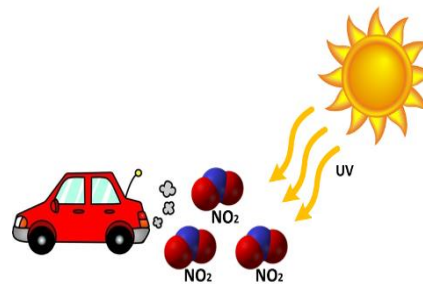
Strong interconnectivity

Exposure Reduction[mg/h]



# Extension to photochemical smog

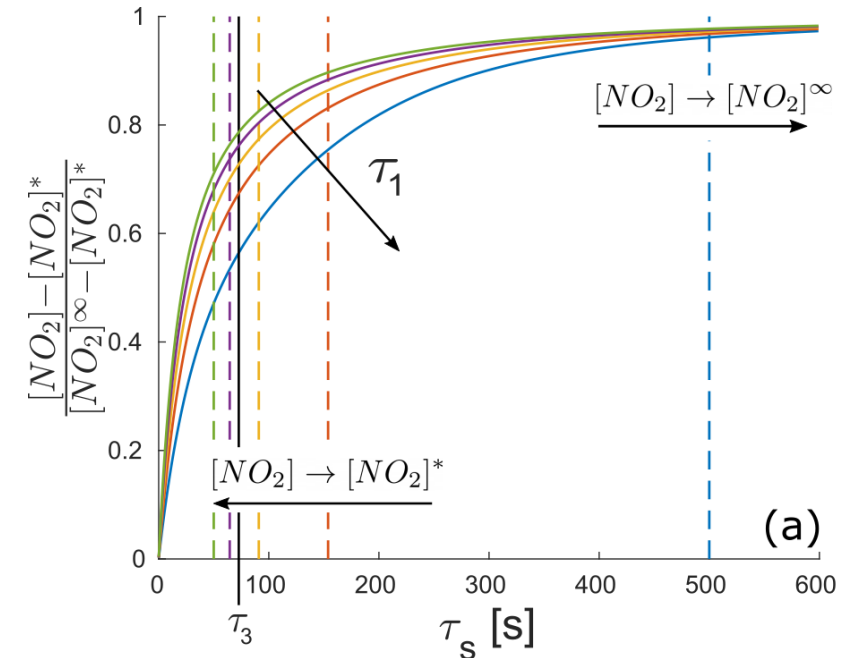
- Driven by solar radiation
- Due to traffic emissions ( $NO_x$ )
- Irritate the eyes and the respiratory tract
- Complex chemical reactions that can be simplified in the  $NO_2 - NO - O_3$  cycle



## PHOTOSTATIONARY ASSUMPTION

The **timescales of chemical reactions** are very short compared to the **timescales of turbulent transport**.

Chemical reactions can be applied **after** transport.



# Extension to photochemical smog

## I. TRANSPORT as PASSIVE SCALARS

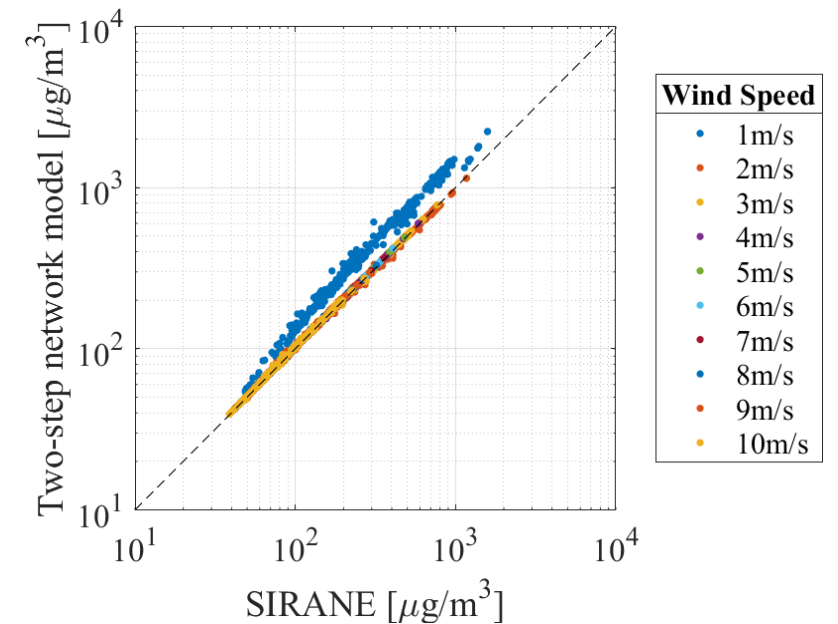
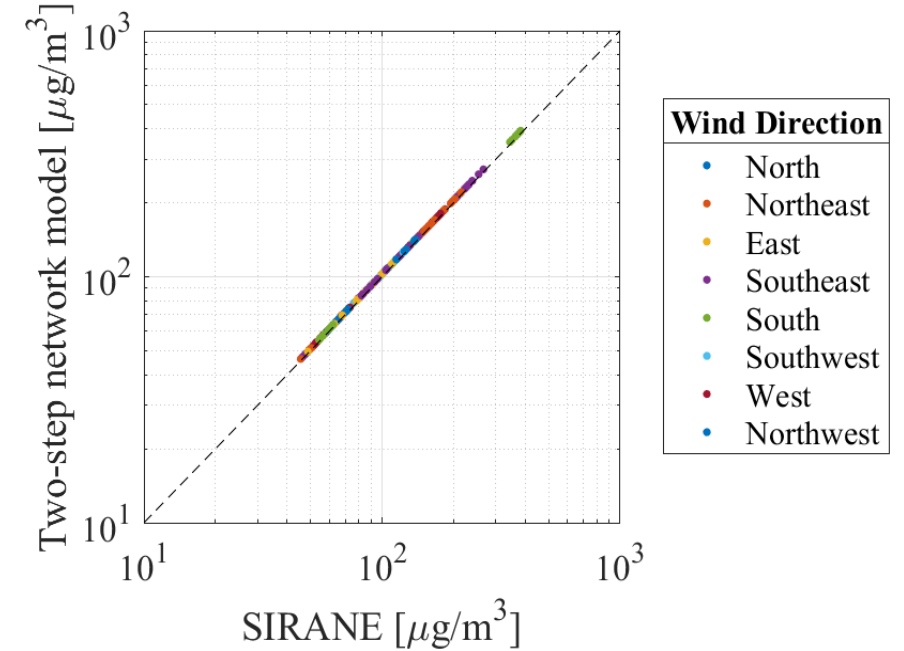
$$\begin{aligned}\tilde{C}_{NO_2} &= A Q_{NO_2}, \\ \tilde{C}_{NO} &= A Q_{NO}, \\ \tilde{C}_{O_3} &= A Q_{O_3}\end{aligned}$$

## II. NULL-CYCLE CHEMISTRY

$$C = f(\tilde{C}) = g(\tilde{C}_{NO_X})$$

## III. COMPARISON WITH SIRANE

SIMULATIONS FOR DIFFERENT WIND DIRECTIONS AND WIND INTENSITIES (ADOPTING VELOCITY CORRECTION)



! Multiple scenarios of chemical pollutant dispersion can be achieved starting from a single transport matrix  $A$



# Where to reduce emissions considering chemical reactions?

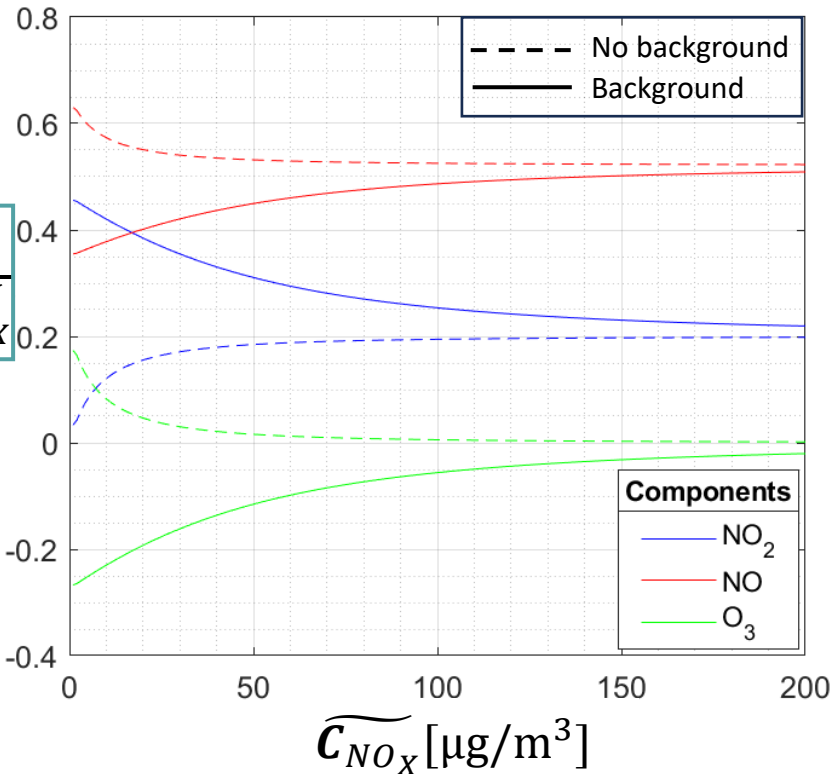
## Perturbation of emission-exposure model

~~$$e = qp \circ C = qp \circ AQ = EQ$$~~

$$e = qp \circ C = qp \circ f(\tilde{C}) = qp \circ f(AQ)$$

~~$$\delta e = E\delta Q$$~~

$$\delta e = qp \circ \delta C = qp \circ \delta f(\tilde{C}) = qp \circ \delta f(AQ)$$



## TAYLOR SERIES EXPANSION

$$\delta e = e - e_0 \approx qp \circ \frac{\partial f}{\partial \tilde{C}} A \delta Q$$

$$\delta e = E \delta Q \quad \text{where} \quad E = qp \circ \frac{\partial f}{\partial \tilde{C}} A$$

$$\frac{\partial f}{\partial \tilde{C}} = \frac{dg}{dC_{NO_x}} \left( (1-a) \frac{M_{NO}}{M_{NO_2}} \ a \ 0 \right)$$

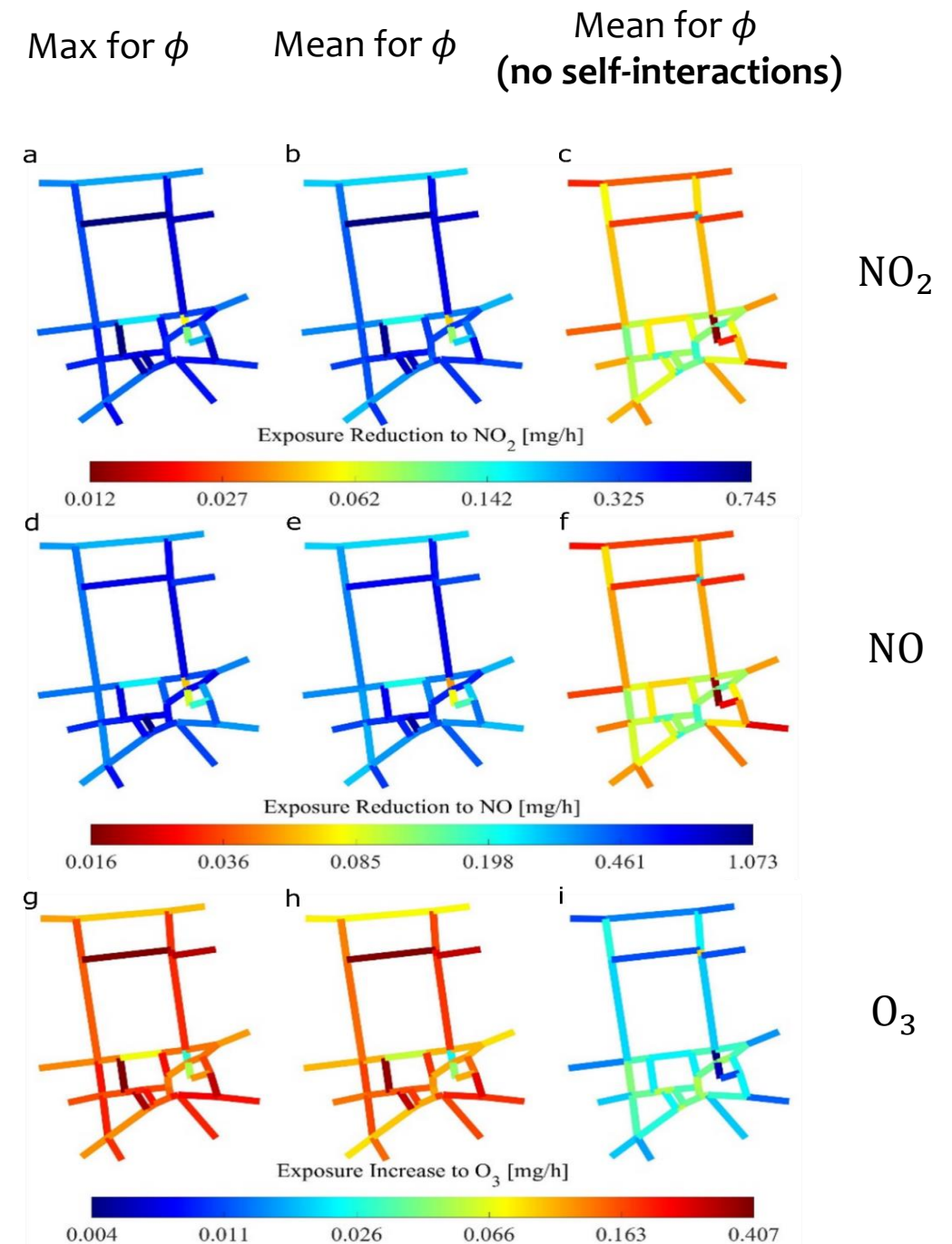
When the emitted and affected nitrogen oxides ( $\tilde{NO}_x$ ) are large, the relation between before-after reaction concentrations is almost **linear**

# Where to reduce emissions?

**Exposure Reduction/Increase**[mg/h] to NO<sub>2</sub>, NO, O<sub>3</sub> by decreasing the emission of NO<sub>2</sub>, NO (NO<sub>x</sub>)

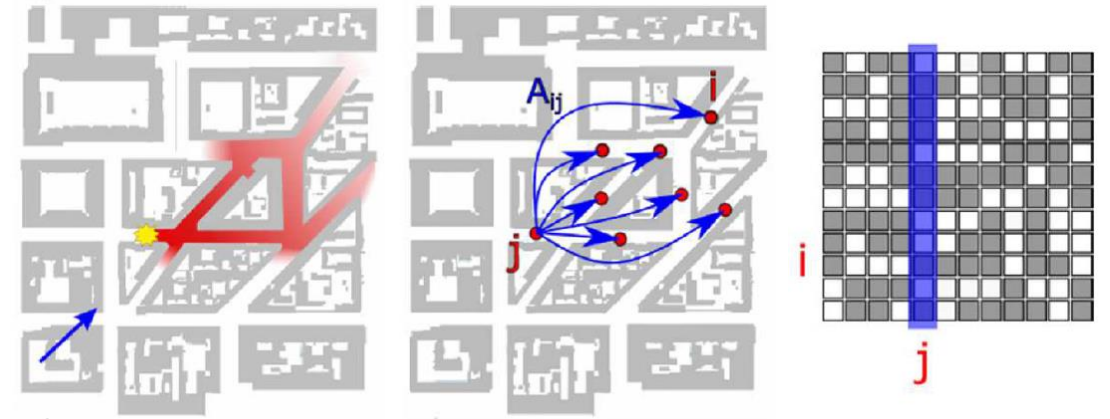
$$R_j = - \sum_i \delta e_i$$

- Exposure reductions are **linear functions** of the passive scalar case
- A reduction in NO<sub>x</sub> emission is responsible for a **concentration increase** of ozone



# Conclusions

- I. MULTIPLE SCENARIOS FROM A SINGLE TRANSPORT MATRIX (A)
- II. LINEAR SCALING FOR VELOCITY INTENSITY
- III. NETWORK REDUCTION
- IV. OUTDEGREE OF EXPOSURE MATRIX (E) PROVIDES BEST PLACE WHERE TO REDUCE EMISSIONS
- V. EXTENSION TO CHEMISTRY
- VI. SIMPLE AND MODULAR MODEL



## and perspectives...

- I. TRANSPORT MATRIX (A) FROM LES SIMULATIONS
- II. TEST FOR DIFFERENT STABILITY CONDITIONS AND CHEMICAL MODELS
- III. BETTER EXPOSURE MODEL