

**15th International Conference on Harmonisation within Atmospheric  
Dispersion Modelling for Regulatory Purposes (HARMO 15)  
Madrid, Spain; 6 to 9 May 2013**

# **Large-eddy simulation of wind flows and pollutant transport inside and over idealized urban street canyons in unstable thermal stratification**

**Ming-Chung Chan & Chun-Ho Liu\***

Department of Mechanical Engineering, The University of Hong Kong  
Pokfulam Road, Hong Kong, China



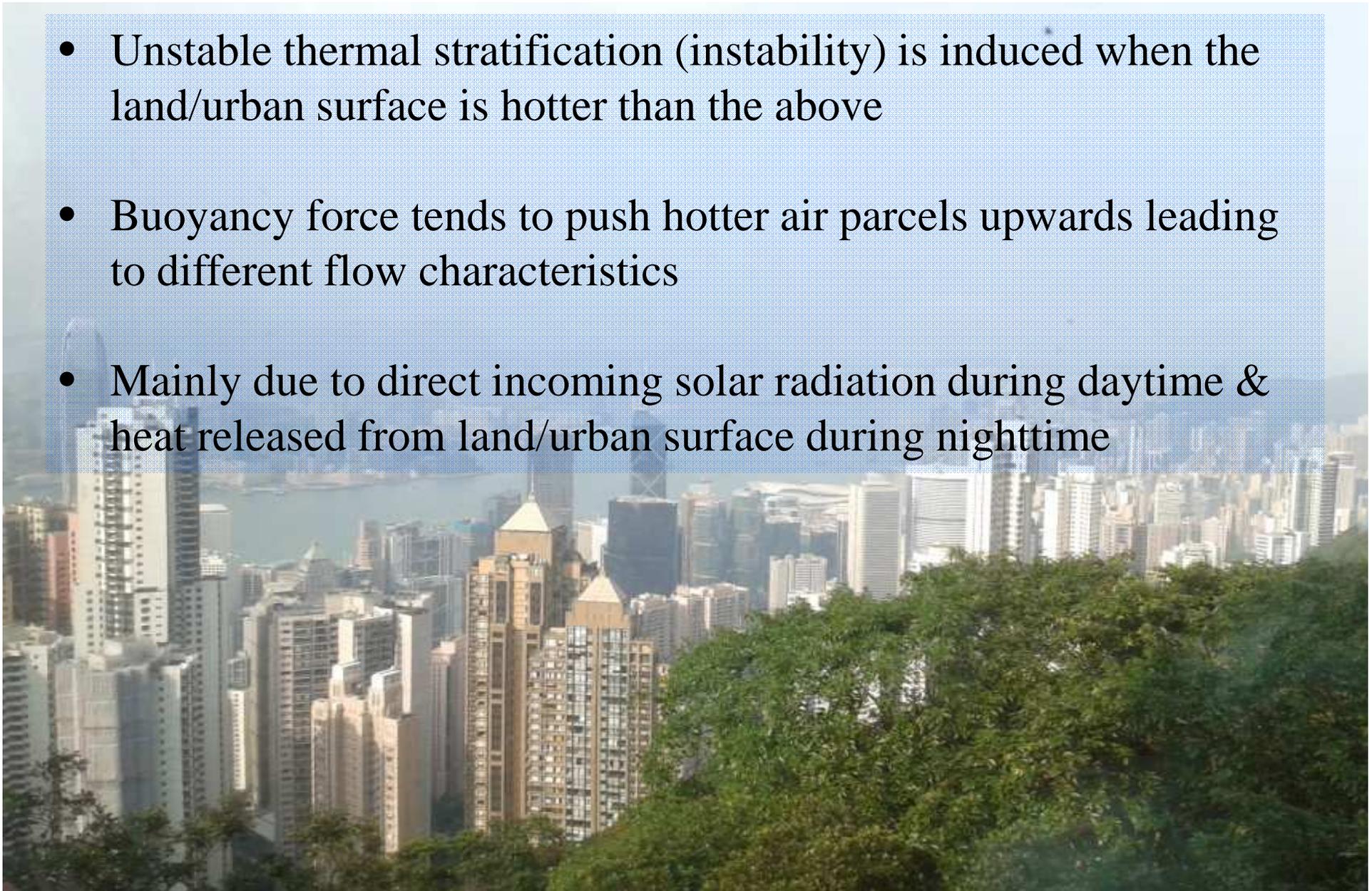
*\*Corresponding Author:* Dr. Chun-Ho LIU; Department of Mechanical Engineering, 7/F Haking Wong Building, The University of Hong Kong, Pokfulam Road, Hong Kong, CHINA; *Tel:* (852) 2859 7901; *Fax:* (852) 2858 5415; [liuchunho@graduate.hku.hk](mailto:liuchunho@graduate.hku.hk)

# Table of Contents

- Introduction
- Highlights of previous studies
- Objectives
- Methodology
- Comparison between LES & wind tunnel results
- Findings & discussion
- Conclusions

# Introduction

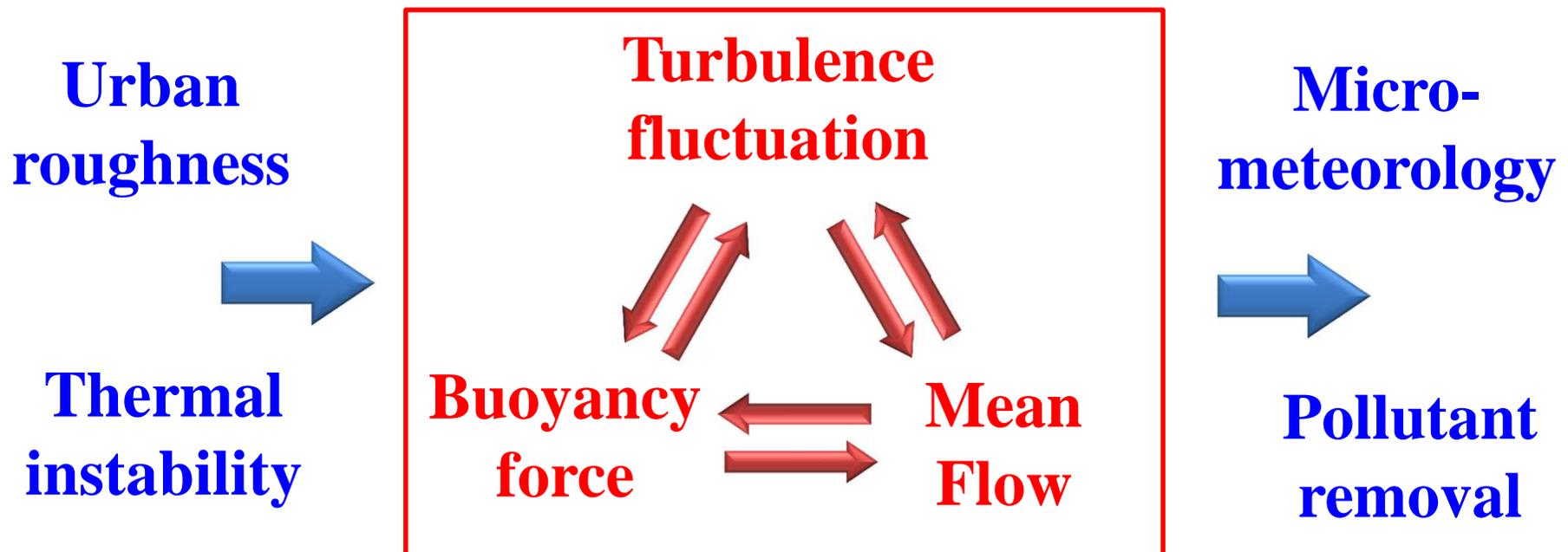
- Unstable thermal stratification (instability) is induced when the land/urban surface is hotter than the above
- Buoyancy force tends to push hotter air parcels upwards leading to different flow characteristics
- Mainly due to direct incoming solar radiation during daytime & heat released from land/urban surface during nighttime



Photography taken at Noon, - The Peak, Hong Kong

# Motivations

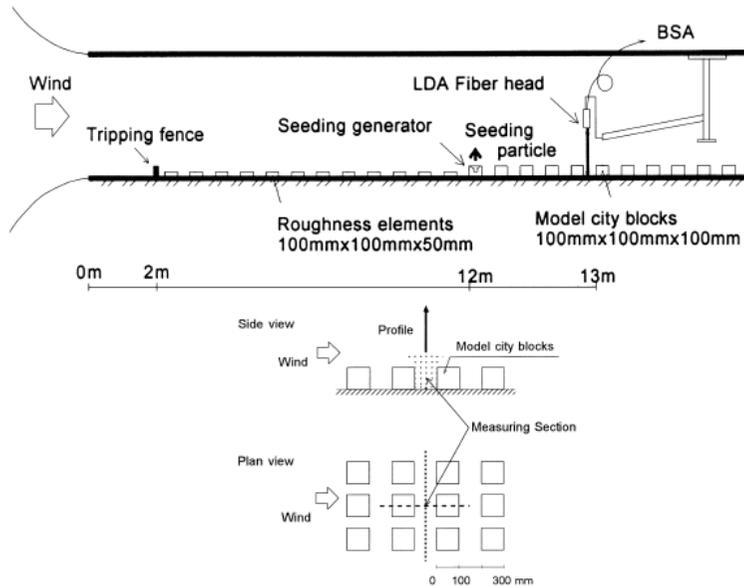
- Some previous studies showed that unstable stratification tends to promote pollutant dispersion & turbulent mixing, which in turn improves the street canyon air ventilation



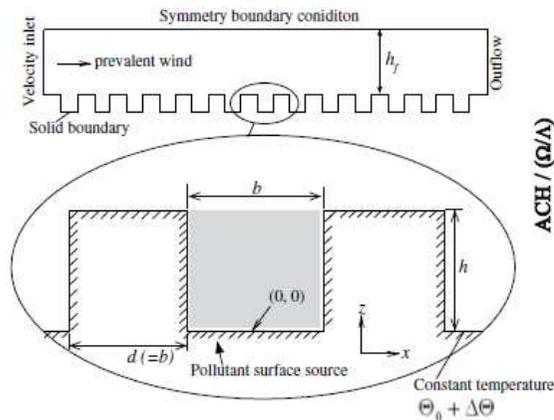
# Motivations

- Urban morphology is characterized by large roughness height which enhances turbulent generation
- High heat capacity of urban surface & trapping of thermal energy inside street canyons increase the duration of unstable stratification, compared with that over rural terrain
  - e.g. observation showed 85% in daytime & 64% at nighttime (Niachou et al. 2008)
- It is advantageous to understand the characteristics of flows & pollutant dispersion under unstable stratification in urban areas
- However, those researches are limited in the literature

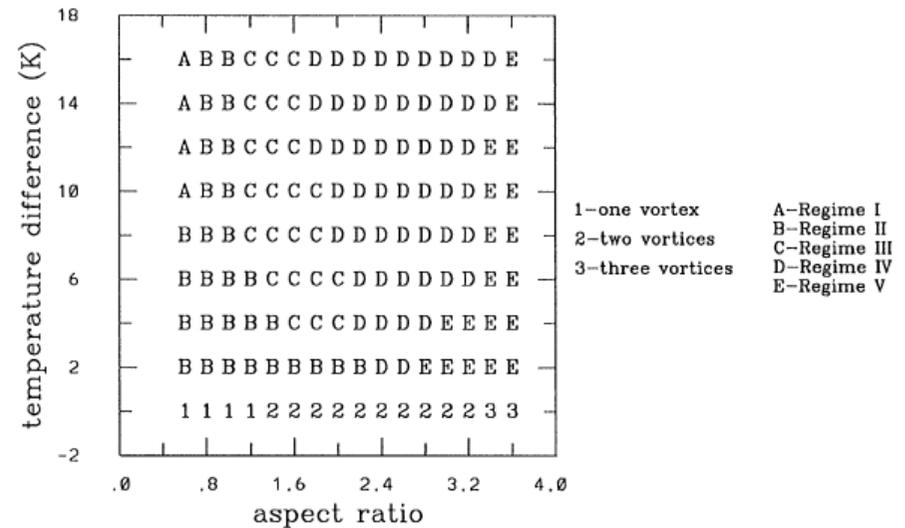
# Highlights of previous studies



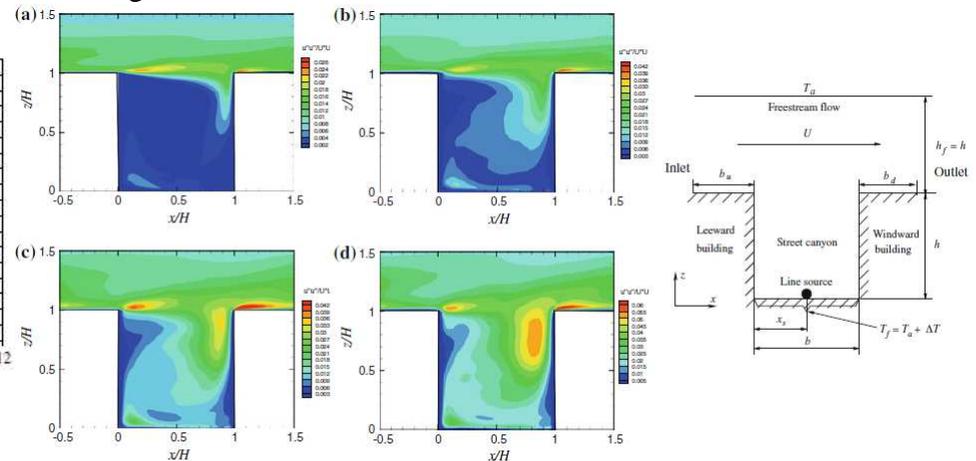
Uehara et al. (2000) – Wind tunnel experiments on how thermal stratification affects flows in and above urban street canyons



Cheng et al. (2009) – On the correlation of air and pollutant exchange for street canyons in combined wind-buoyancy-driven flow



Kim and Baik (2001) – Urban street-canyon flows with bottom heating



Li et al. (2010) – Large-eddy simulation of flow and pollutant transport in urban street canyons with ground heating

# Objectives

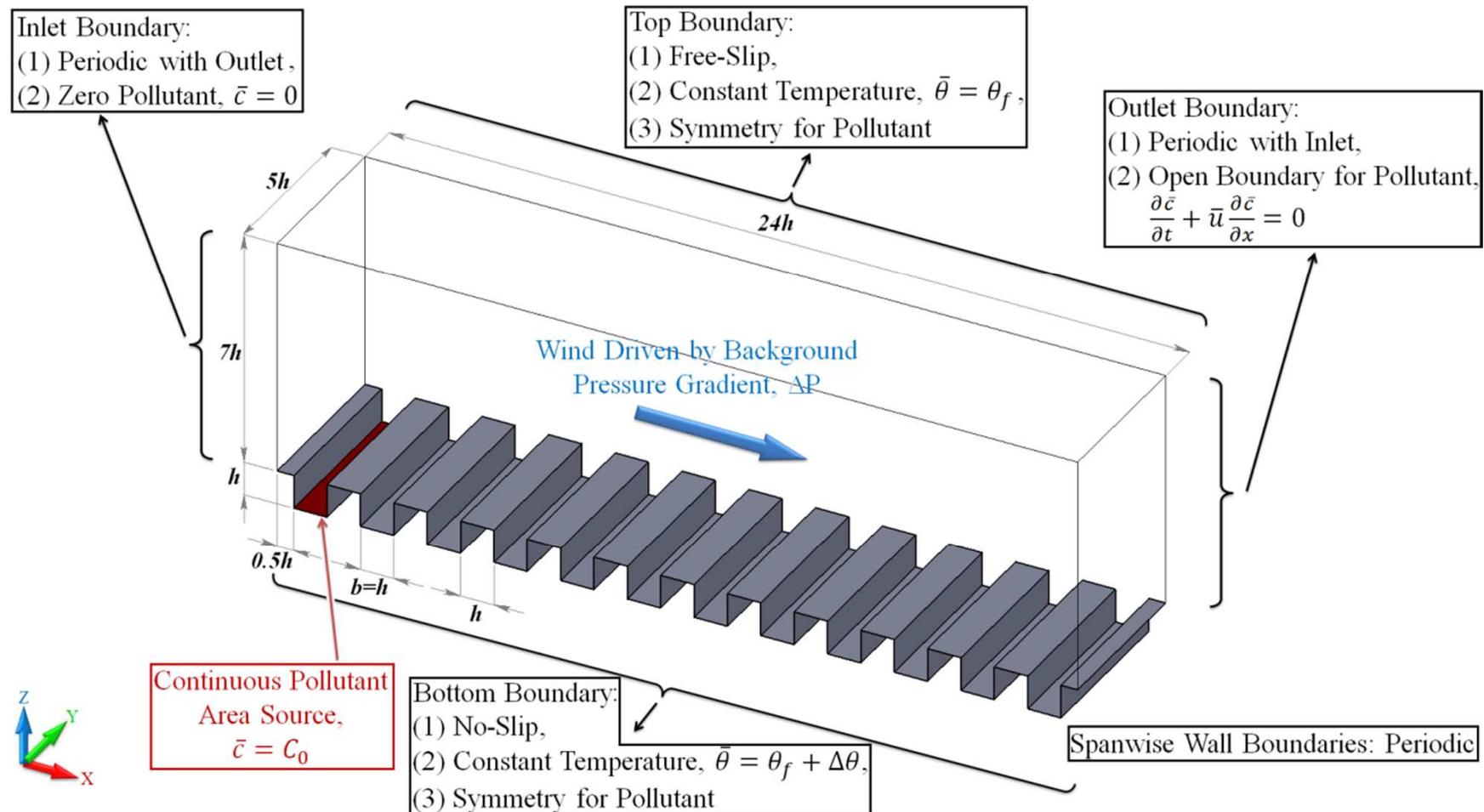
Since the micro-meteorology and pollutant removal of street canyons strongly depend on the flow conditions just above the urban roughness, this presentation mainly focuses on

- 1) the wind flows (mean wind & turbulent statistics),
- 2) the logarithmic mean wind profiles, and
- 3) the pollutant dispersion characteristics above urban surface under different intensities of (slightly) unstable stratification

This study is performed in a fundamental way by using idealized urban geometries & background conditions, & using LES to resolve all the large-scale turbulence explicitly

# Methodology

- Large-eddy simulation (**LES**) with one-equation subgrid-scale (**SGS**) turbulence model (incompressible flow)
- By the open-source CFD code – **OpenFOAM**, version 2.1.0



# Methodology

- Free-stream wind is driven by background pressure gradient  $\Delta P$  (constant for all models)
- Buoyancy force is modeled by the Boussinesq approximation & is controlled by the gravitational acceleration  $g$
- Solving the filtered governing equations for the resolved-scale flow vector, temperature & pollutant concentration

$$\frac{\partial \bar{u}_i}{\partial t} + \frac{\partial}{\partial x_j} \bar{u}_i \bar{u}_j = \boxed{\Delta P \delta_{i1}} - \frac{\partial \bar{p}}{\partial x_i} + (\nu + \nu_{SGS}) \frac{\partial^2 \bar{u}_i}{\partial x_j \partial x_j} + \boxed{\alpha g (\bar{\theta} - \theta_0) \delta_{i3}}$$

Background Pressure Gradient Buoyancy Force

# Methodology

- Analyzing the pseudo steady-state properties
- Ensemble averaging in the temporal & spanwise domains that denoted by  $\langle \phi \rangle$
- Simulation conditions:

AR	$Re_\tau$	$Re_H$	$Ri_\tau$	$Ri_H$
1	4140	89,000 ↓ 42,000	0 ↓ -400	0 ↓ -3.92

By force balance in free-stream domain,

$$\tau_w = \rho \cdot \Delta P \cdot H$$

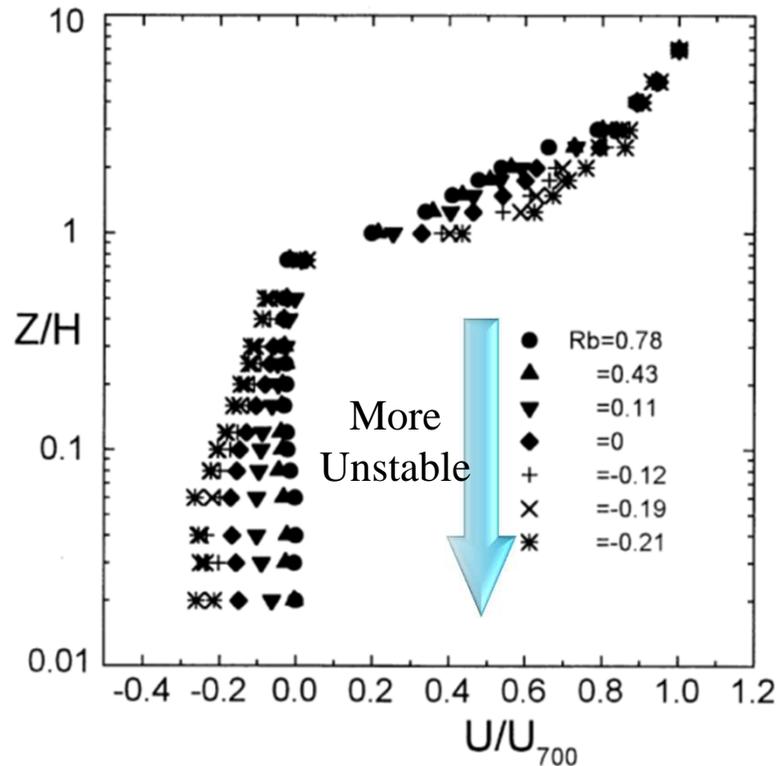
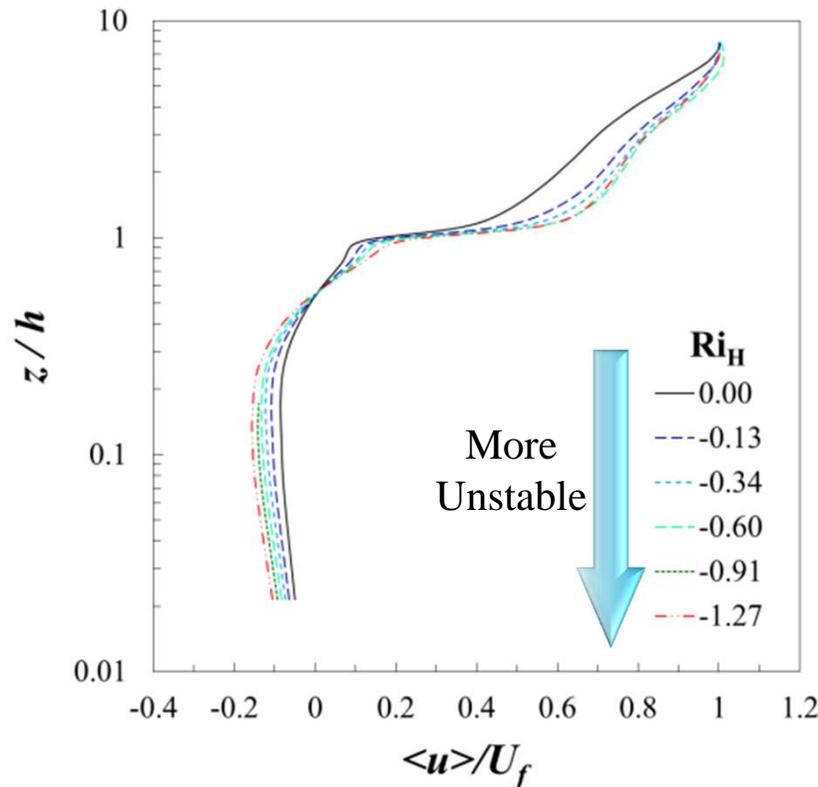
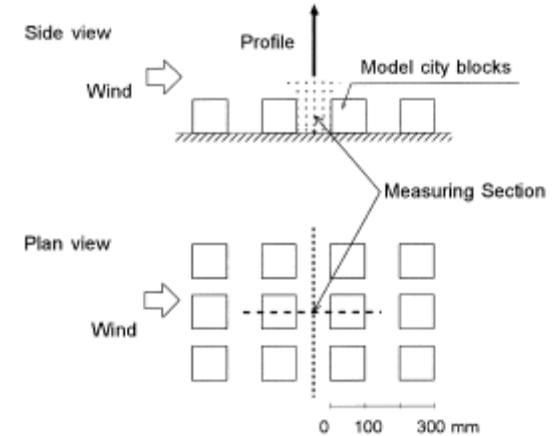
$$u_\tau = \sqrt{\tau_w / \rho} = \sqrt{\Delta P \cdot H}$$

$$Re_H = \frac{H \cdot U_f}{\nu} \quad Ri_H = -\frac{\alpha g H \Delta \theta}{U_f^2}$$

$$Re_\tau = \frac{H \cdot u_\tau}{\nu} \quad Ri_\tau = -\frac{\alpha g H \Delta \theta}{u_\tau^2}$$

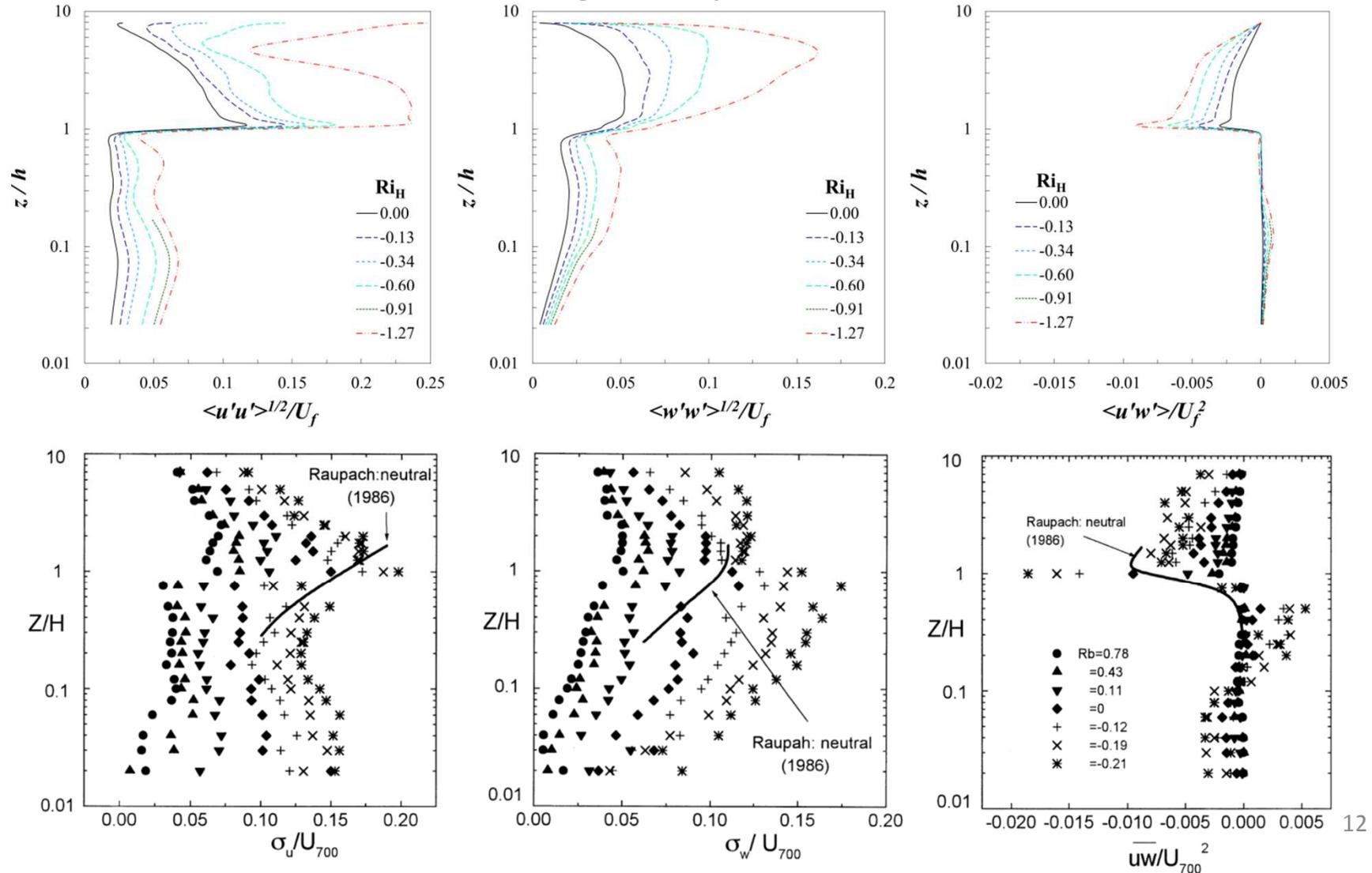
# Comparison between LES & wind tunnel models

- LES results show trends which are similar to the tunnel results by Uehara et al. (2000):
  - Wind flow relative to free-stream is enhanced both inside and above street canyon



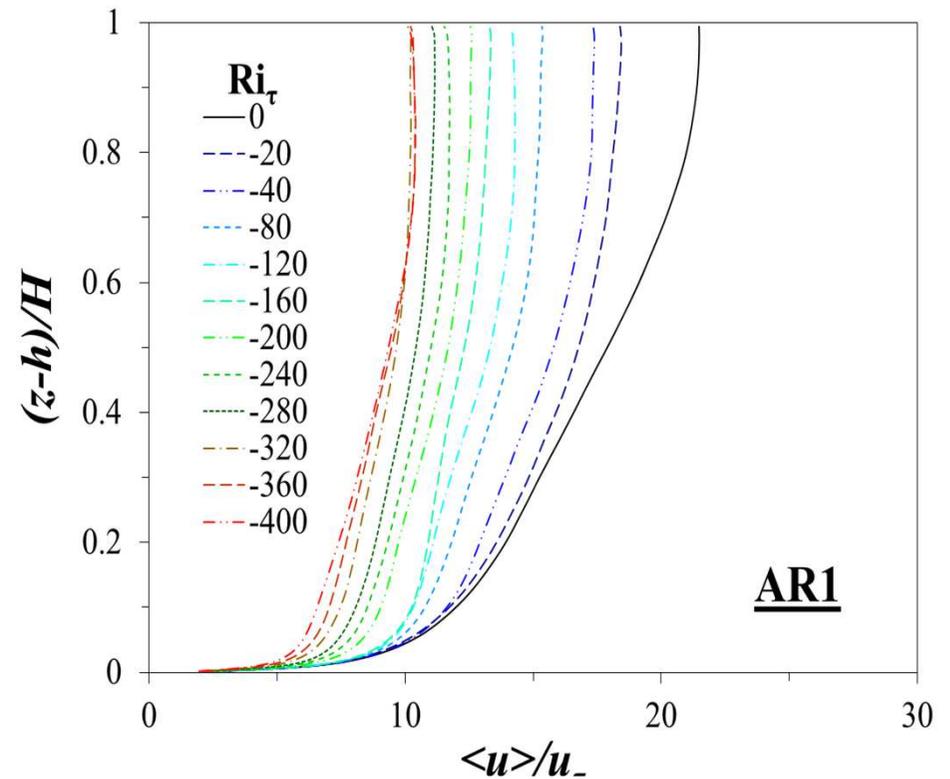
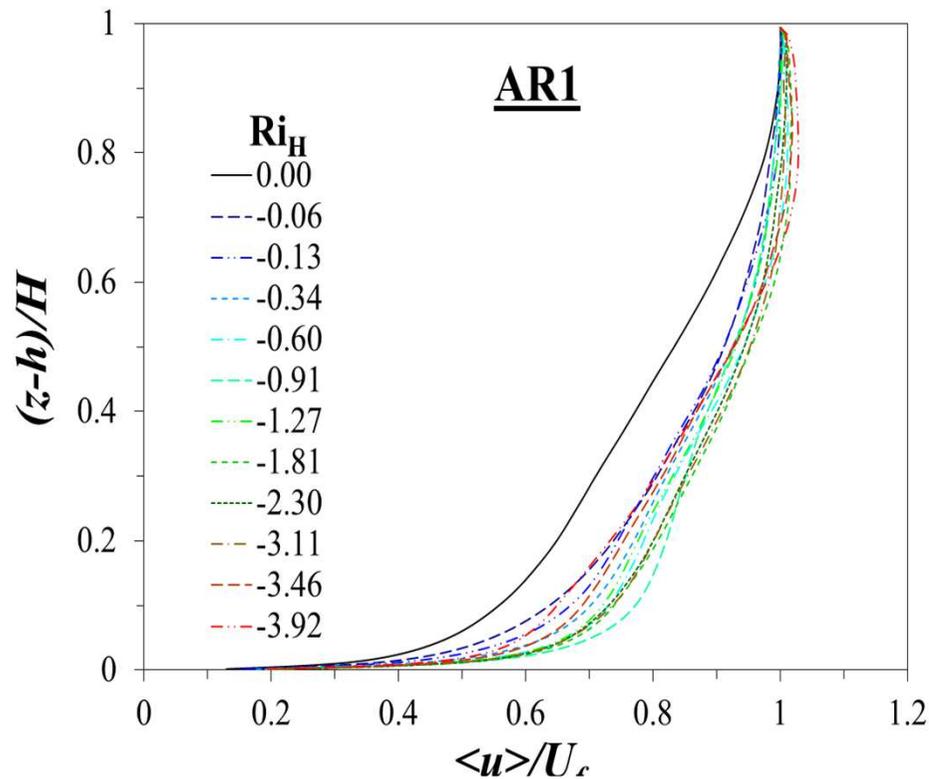
# Comparison between LES & wind tunnel models

- Smaller magnitudes for wind fluctuations is observed since 2D geometry (ribs) is used in LES but 3D geometry is used in wind tunnel



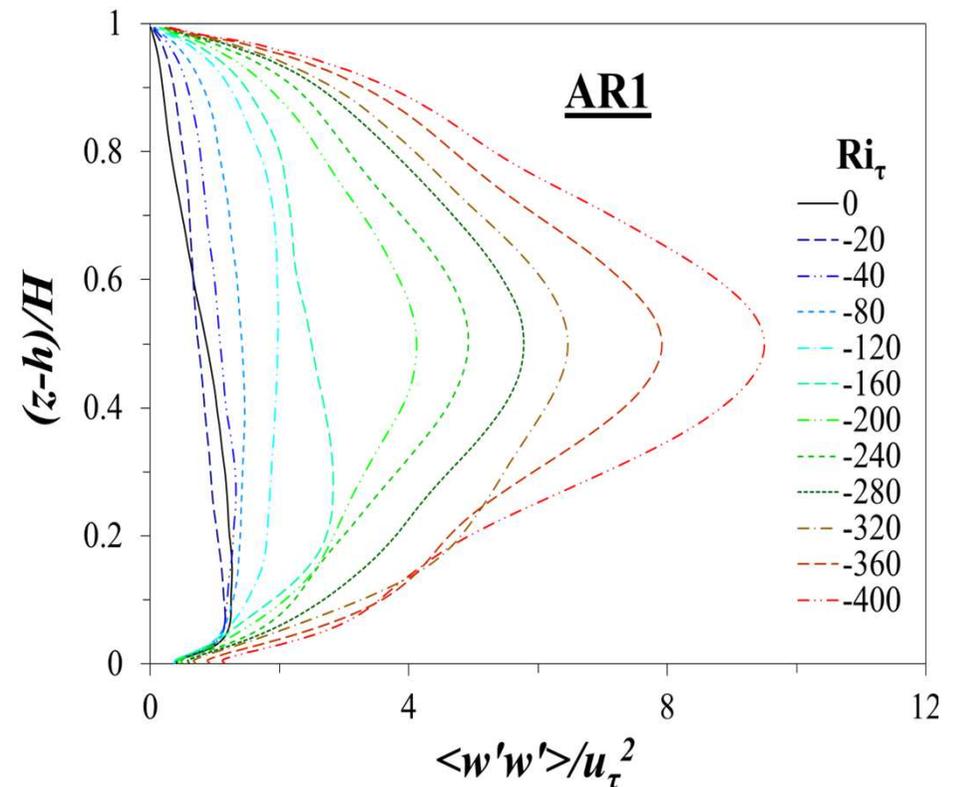
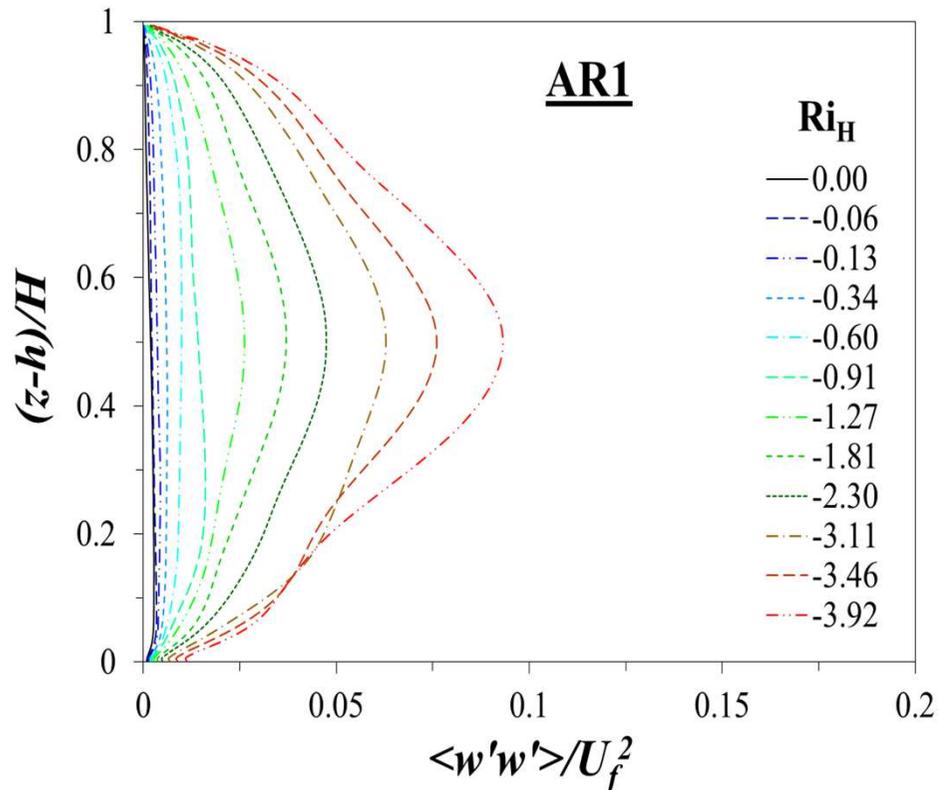
# Mean flow above urban roughness

- The mean flow is further averaged in streamwise direction
- When instability increases, gradient of mean wind profile near roughness elements increases & it is more uniform above
- With constant driving force (constant  $u_\tau$ ), mean wind reduces with instability



# Wind fluctuation above urban roughness

- When instability increases, wind fluctuation increases that implies enhanced turbulent mixing
- The local maximum point of fluctuation shifts upwards as instability increases



# Logarithmic law of the wall

Smooth surface

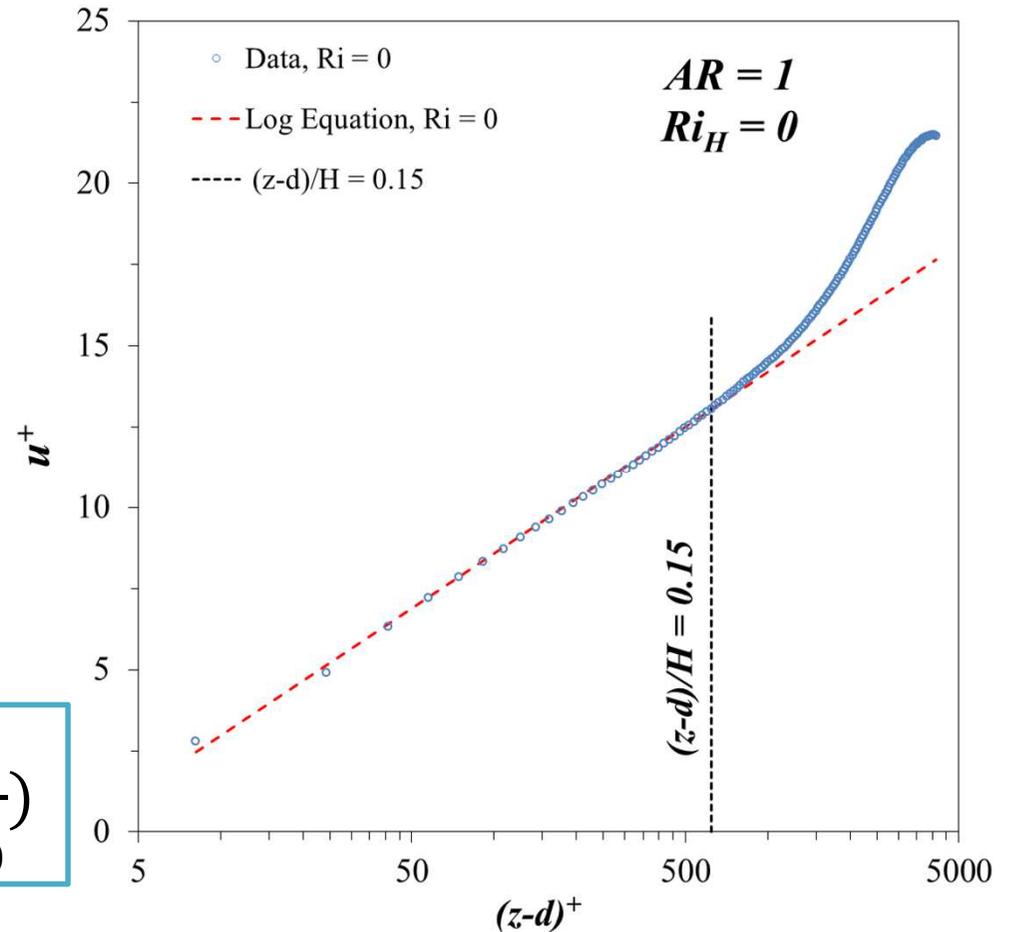
(by dimensional analysis):

$$\frac{du^+}{dz} = \frac{1}{z} \phi\left(\frac{z}{\delta_v}, \frac{z}{\delta}, \frac{z}{L}\right)$$

Neutral stratification:

$(z/\delta_v \gg 1, z/\delta \ll 1 \text{ \& } z/L \sim 0)$

$$\frac{du^+}{dz} = \frac{1}{\kappa z} \rightarrow u^+ = \frac{1}{\kappa} \ln\left(\frac{z}{z_0}\right)$$



Rough surface:

$$u^+ = \frac{1}{\kappa} \ln\left(\frac{z - d}{z_0}\right)$$

where

$$u^+ = \frac{\langle u \rangle}{u_\tau} \text{ \& } \delta_v = \frac{\nu}{u_\tau}$$

$u_\tau$ : friction velocity

$\delta_v$ : viscous length scale

$\delta$ : boundary layer/channel height

$L$ : Monin-Obukov length scale

$\kappa$ : von Kármán constant ( $\sim 0.41$ )

$d$ : displacement height

# Logarithmic law of the wall

Unstable stratification ( $L < 0$ ):

$$\frac{du^+}{dz} = \frac{1}{\kappa z} \phi_M\left(\frac{z}{L}\right)$$

Expanding  $\phi_M$  by Taylor's series and neglecting higher orders:

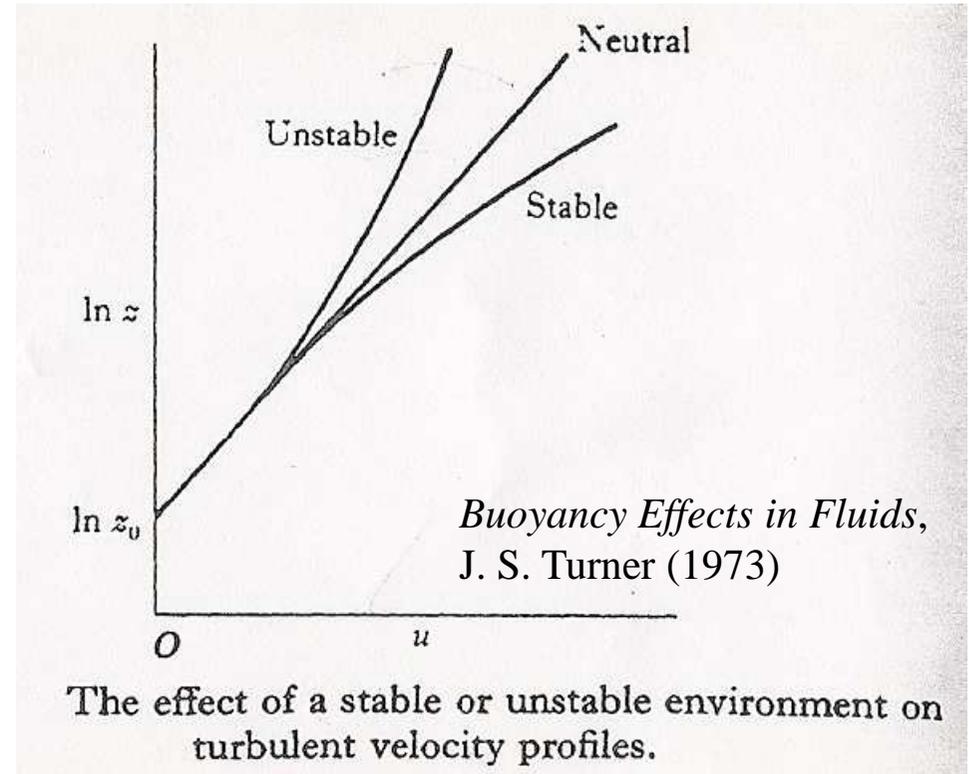
$$\frac{du^+}{dz} = \frac{1}{\kappa z} \left[ 1 + \alpha \left( \frac{z}{L} \right) \right]$$

$$u^+ = \frac{1}{\kappa} \left[ \ln \frac{z}{z_0} + \alpha \frac{z}{L} \right]$$

for  $z/L \ll 1$

Rough surface:

$$u^+ = \frac{1}{\kappa} \left[ \ln \frac{z-d}{z_0} + \alpha \frac{z-d}{L} \right]$$



where  $\alpha$  is an empirical constant  
( $\sim 4.5$  by Webb, 1970)

Monin-Obukov length:

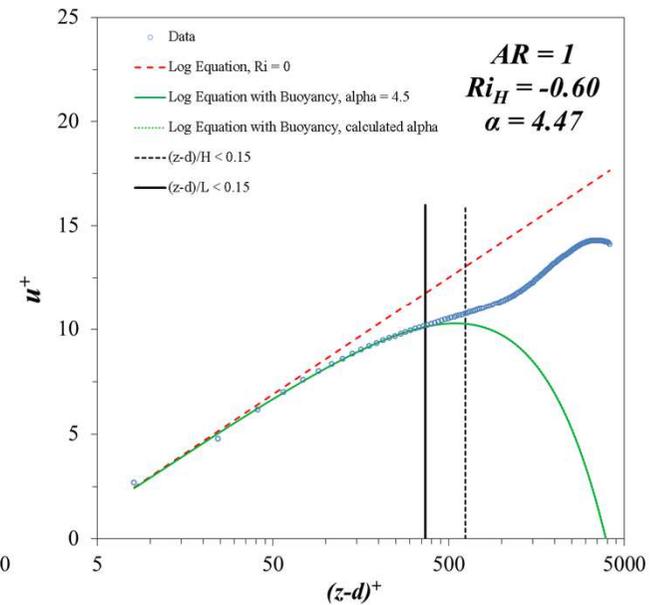
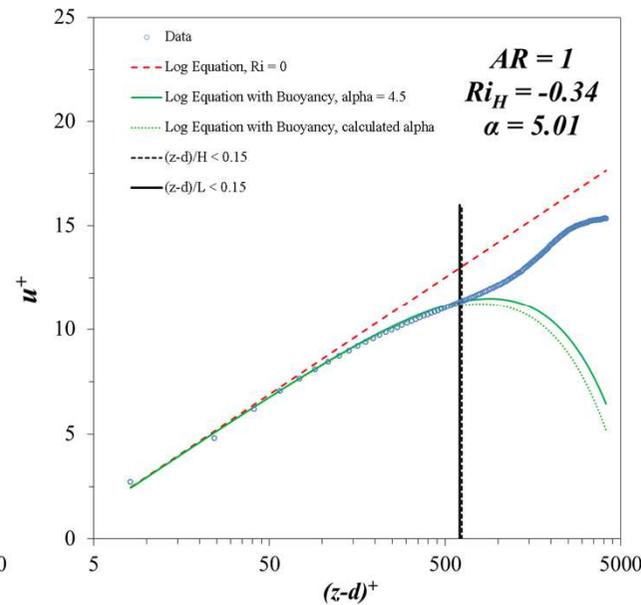
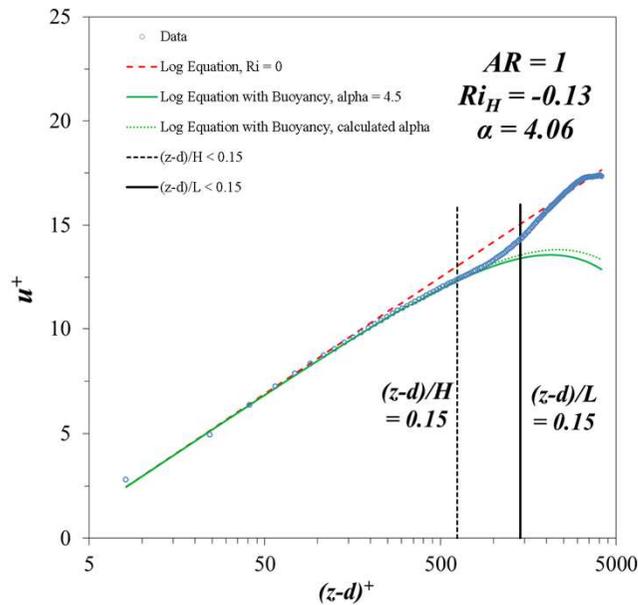
$$L = \frac{-u_\tau^3}{\kappa B}$$

Buoyancy flux:

$$B = \frac{g}{\theta} \cdot \overline{\theta' w'}$$

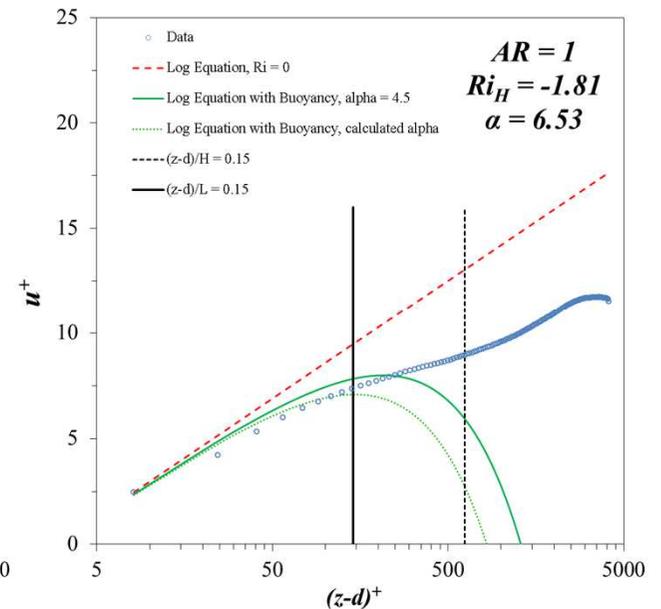
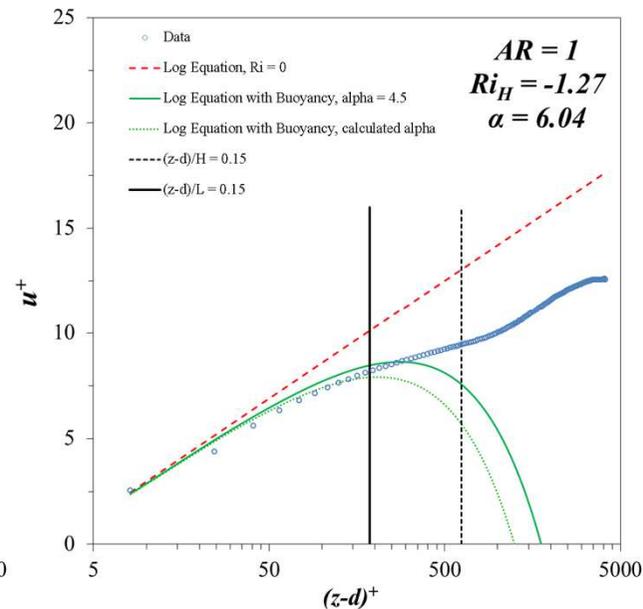
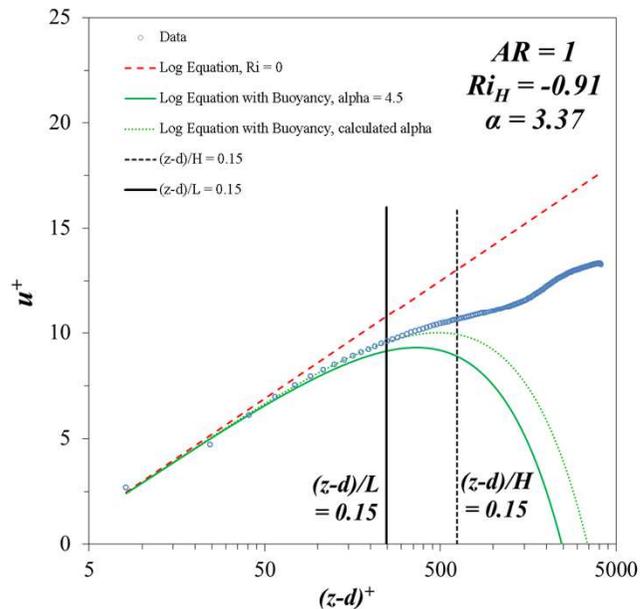
# Logarithmic law of the wall

- For slightly unstable cases, mean wind profiles are well described by the log-law equation
- Decrease in wind speed is due to the increased drag by (enhanced) turbulent mixing
- Empirical constant  $\alpha$  is calculated by the linear regression for small  $z/L$  (using data for  $z/L < 0.15$ ) that is found to be  $\sim 4.5$



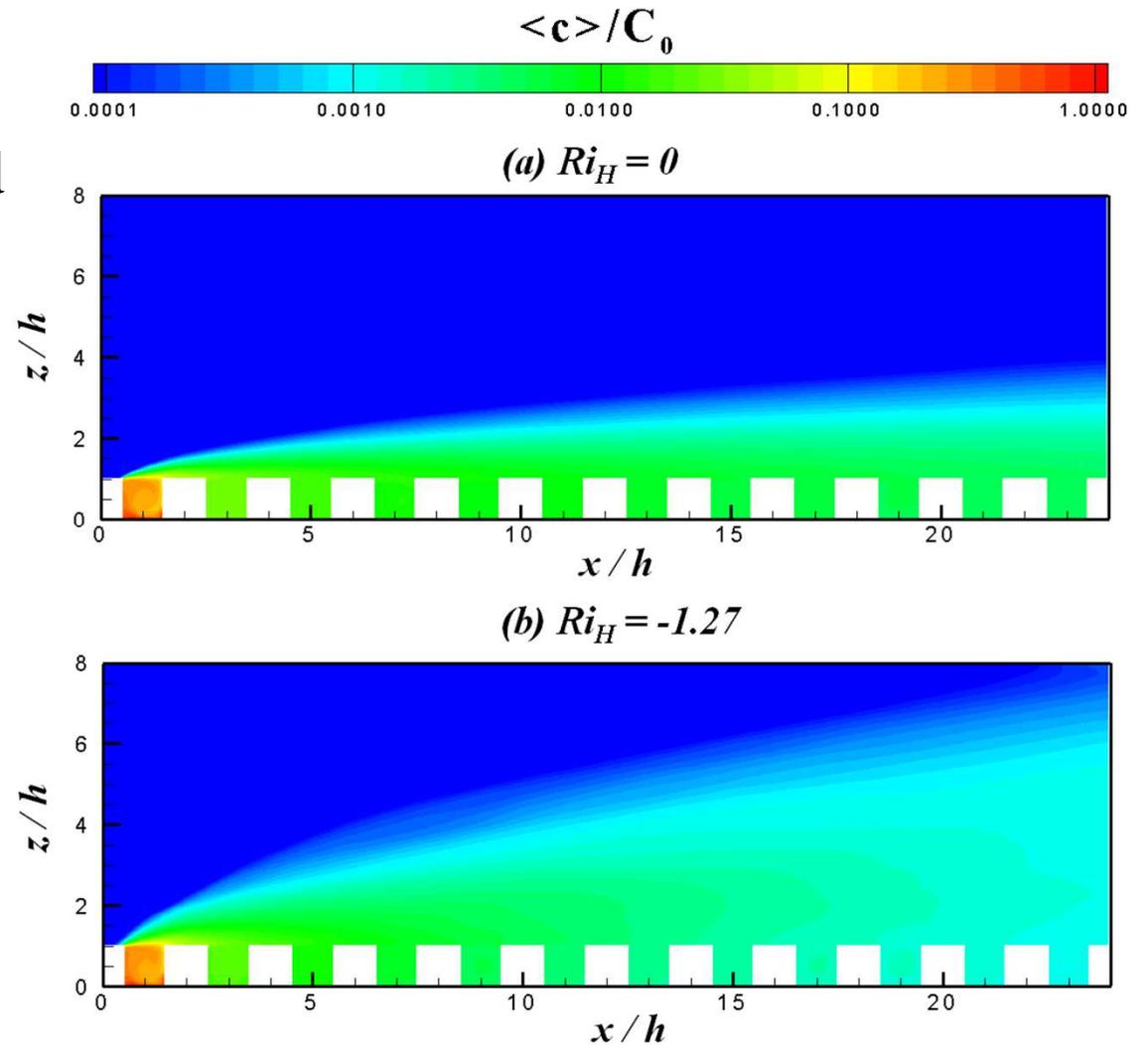
# Logarithmic law of the wall

- Further increasing the intensity of instability, the wind profiles are not well described by the equation, since  $z/L$  starts to be significant
- $d$  &  $z_0$  also varies with instability ( $Ri$ )
- For very strong instability, buoyancy force changes the flow mechanism, thus another function of  $\phi_M$  should be applied



# Plume dispersion above urban roughness

- Constant area source on 1<sup>st</sup> street canyon ground
- Upward plume dispersion is promoted in unstable stratification
- Due to the enhanced turbulent mixing
- Less influence on the downstream areas



# Conclusions

- The **LES** results show **similar trends** compared with those of the **wind tunnel** study by Uehara et al. (2000)
  - The deviation in magnitudes is due to the difference in **roughness geometry** (2D building elements in LES & 3D in wind tunnel study)
- The logarithmic law of the wall, which includes a **linear term of  $z/L$** , describes well the mean wind profile only under **very slightly** unstable stratification
- When the unstable stratification **enhances**
  - 1) turbulence is **enhanced** everywhere
  - 2) mean wind profile **gradient** is **higher** near urban roughness due to the **enhanced shear** by **turbulent mixing**
  - 3) mean wind profile **deviates more** from (neutral) logarithmic law of the wall because of the **reduced wind speed**
  - 4) pollutant dispersion is **promoted** (in the vertical direction)



**Thank you**