



NCAR

AUTOMATED SOURCE PARAMETER AND LOW LEVEL WIN ESTIMATION FOR ATMOSPHERIC TRANSPORT AND DISPERSION APPLICATIONS

**F. Vandenberghe, P. Bieringer, I. Sykes, J.
Hurst, G. Bieberbach, S. Parker
& L. Rodriguez**

**National Center for Atmospheric Research,
Boulder CO**



STE recent developments

- All source parameters: $[q_s, x_s, y_s, z_s, t_r]$ and wind $[u_e, v_e]$ are adjusted during the estimation process.
- Either wind components or wind speed and direction can be used and adjusted.
- Two step minimization:
 - 1) $[x_s, y_s, z_s, t_r, u_e, v_e]$ with logarithmic concentration
 - 2) q_s with plain concentration
- Addition of a background term (a priori information) in the cost function to remove ambiguities between source parameters.



Gaussian Puff Model

Input vector:

$$S = \begin{bmatrix} q_s \\ x_s \\ y_s \\ z_s \\ t_r \\ u_e \\ v_e \end{bmatrix}$$

Output vector:

$$C(t) = \begin{bmatrix} c_1(t) \\ c_2(t) \\ \dots \\ c_N(t) \end{bmatrix}$$

Model at time t on a given grid $1 \leq n \leq N$:

$$C_n(t) = \frac{q_s}{\sqrt{2\pi}^3 \sigma_x \sigma_y \sigma_z} \exp\left[-\frac{(x-x_s-u_e(t-t_r))^2}{2\sigma_x^2} - \frac{(y-y_s-v_e(t-t_r))^2}{2\sigma_y^2}\right] \left[\exp\left[-\frac{(z-z_s)^2}{2\sigma_z^2}\right] + \exp\left[-\frac{(z+z_s)^2}{2\sigma_z^2}\right] \right]$$



Ambiguity location wind

Same concentrations can be obtained by permutations of source location, wind and release time

$$C_n(t) = \frac{q_s}{\sqrt{2\pi}^3 \sigma_x \sigma_y \sigma_z} \exp\left[-\frac{(x - x_s - u_e(t - t_r))^2}{2\sigma_x^2} - \frac{(y - y_s - v_e(t - t_r))^2}{2\sigma_y^2}\right] \exp\left[-\frac{(z - z_s)^2}{2\sigma_z^2}\right] + \exp\left[-\frac{(z + z_s)^2}{2\sigma_z^2}\right]$$

Prior information needs to be provided to remove the ambiguity



NCAR

Cost function with prior (background) information

Distance of model predicted concentration C to the sensor measurements C^{obs} (with uncertainty σ^{obs})

$$J^{obs} = \frac{1}{2} \frac{\|C^{obs}(t) - C(t)\|^2}{\sigma^{obs}}$$

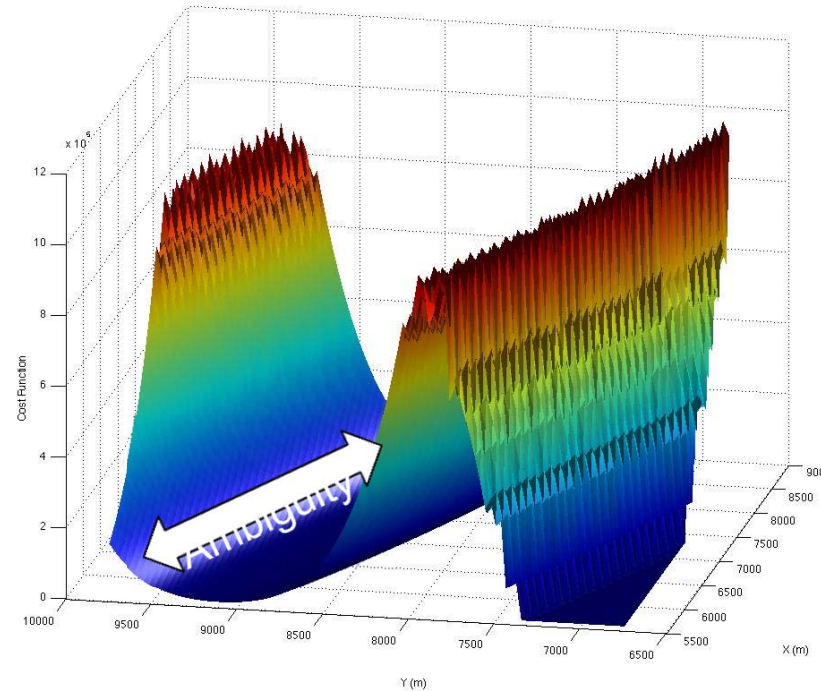
Distance of

$$J^{bck} = \frac{1}{2} \frac{\|x_s^{bck} - x_s\|^2}{\sigma^x} + \dots$$

Total cost

background term:

$$\frac{1}{2} \frac{\|v_e^{bck} - v_e\|^2}{\sigma^v}$$





Important point

σ 's are weight between the background information (first guess source provided by reverse SCIPUFF) and the concentration from sensor

$$2J = \frac{q_s^{bck} - q_s}{\sigma^q} + \frac{x_s^{bck} - x_s}{\sigma^x} + \frac{y_s^{bck} - y_s}{\sigma^y} + \frac{z_s^{bck} - z_s}{\sigma^z} + \frac{t_r^{bck} - t_r}{\sigma^r} + \frac{u_e^{bck} - u_e}{\sigma^u} + \frac{v_e^{bck} - v_e}{\sigma^v} + \frac{C^{obs}(t) - C(t)}{\sigma^{obs}}$$

$$2J = \frac{q_s^{bck} - q_s}{1\text{kg/s}} + \frac{x_s^{bck} - x_s}{500\text{m}} + \frac{y_s^{bck} - y_s}{500\text{m}} + \frac{z_s^{bck} - z_s}{0.5\text{m}} + \frac{t_r^{bck} - t_r}{45\text{s}} + \frac{u_e^{bck} - u_e}{1.4\text{m/s}} + \frac{v_e^{bck} - v_e}{1.4\text{m/s}} + \frac{C^{obs}(t) - C(t)}{0.5|C_{max}^{obs} - C_{min}^{obs}|}$$

small error, ie high confidence, z_s will be slightly changed during the estimation

It's important that each term is properly scaled, or the corresponding parameter will have too much or too little effect on the minimization.



Example FFT07 Case 37

- Reverse SCIPUFF estimated the source **567m** south east from the true release point, release mass was overestimated, but release time was correct
- For demonstration a **+36s** shift was added to the reverse SCIPUFF first guess, before STE.
- STE was carried with **10** iterations (7 log + 3 linear) when:
 - 1) All source parameters $[q_s, x_s, y_s, z_s, t_r, U_e, \theta_e]$ are adjusted,
 - 2) Release time is fixed, other parameters are adjusted
 - 3) Wind speed and direction is fixed, other parameters are adjusted

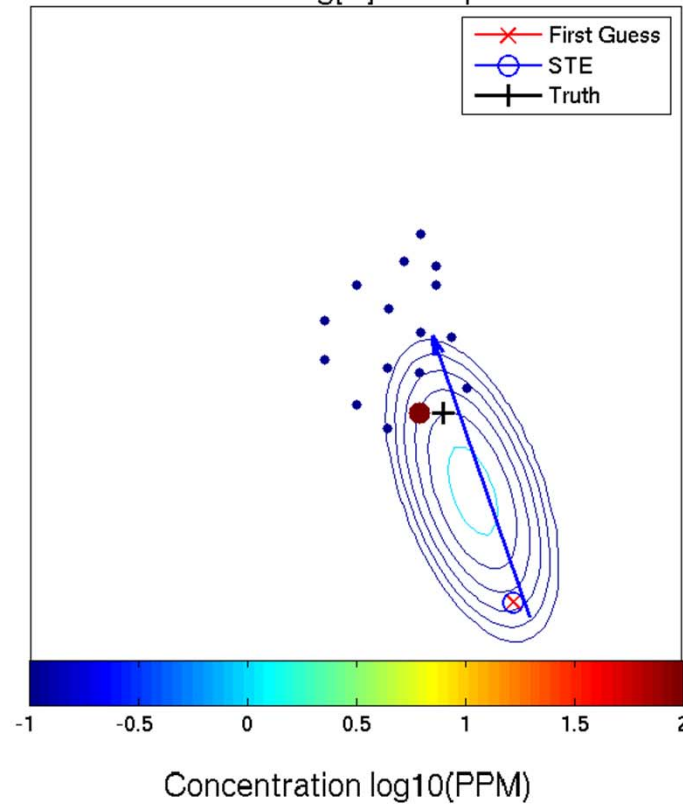


NCAR

FFT07 Case 37

First Guess

Iteration 0 Minimization on Log[C] 21-Sep-2007 16:01:21



Reverse SCIPUFF located the source (x)
567m South East from the true source (+)

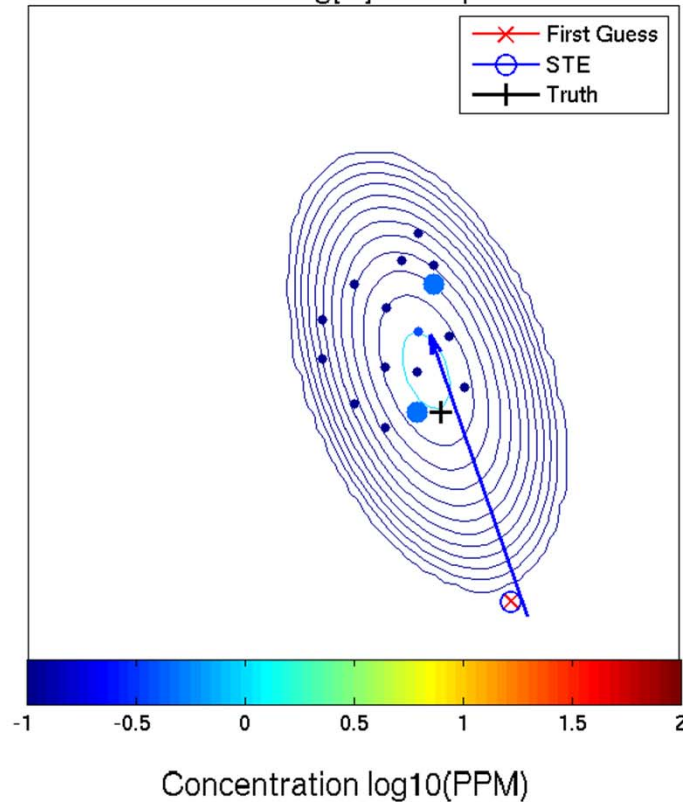


NCAR

FFT07 Case 37

all $[q_s, x_s, y_s, z_s, t_r, U_e, \theta_e]$ adjustment

Iteration 0 Minimization on Log[C] 21-Sep-2007 16:02:21



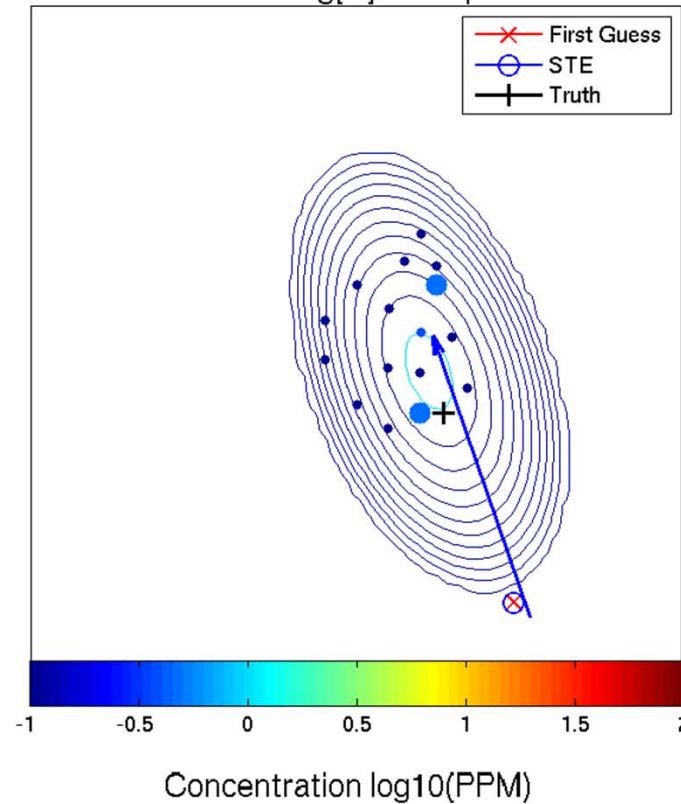
STE (o) moved the source location from SCIPUFF first guess (x) at **79m** from the true source (+)



FFT07 Case 37

NCAR $[q_s, x_s, y_s, z_s, U_e, \theta_e]$ adjustment (fixed $t_r = +36s$)

Iteration 0 Minimization on Log[C] 21-Sep-2007 16:02:21



STE (o) moved the source location from SCIPUFF first guess (x) to **99m** from the true source (+)

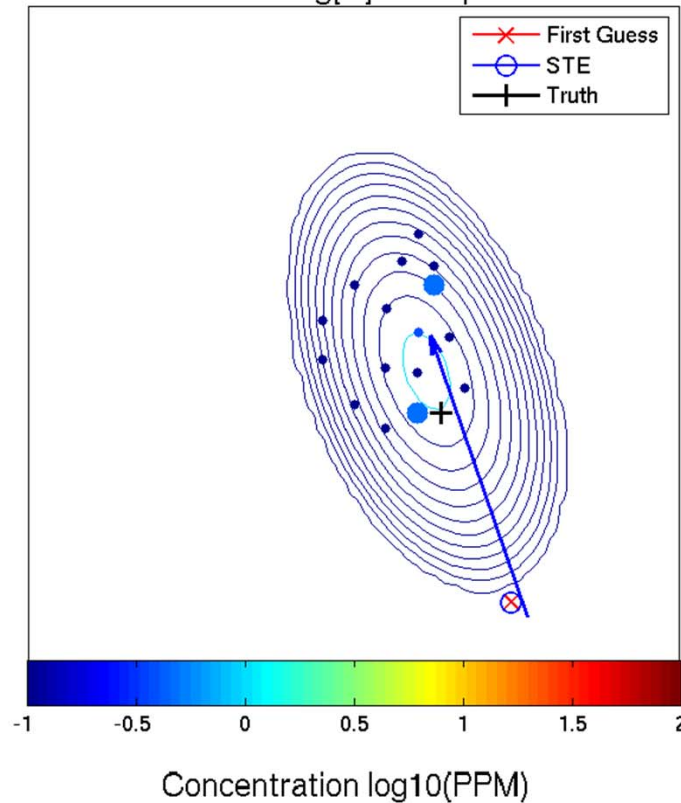


NCAR

FFT07 Case 37

$[q_s, x_s, y_s, z_s, t_r]$ adjustment (fixed U_e & θ_e)

Iteration 0 Minimization on Log[C] 21-Sep-2007 16:02:21

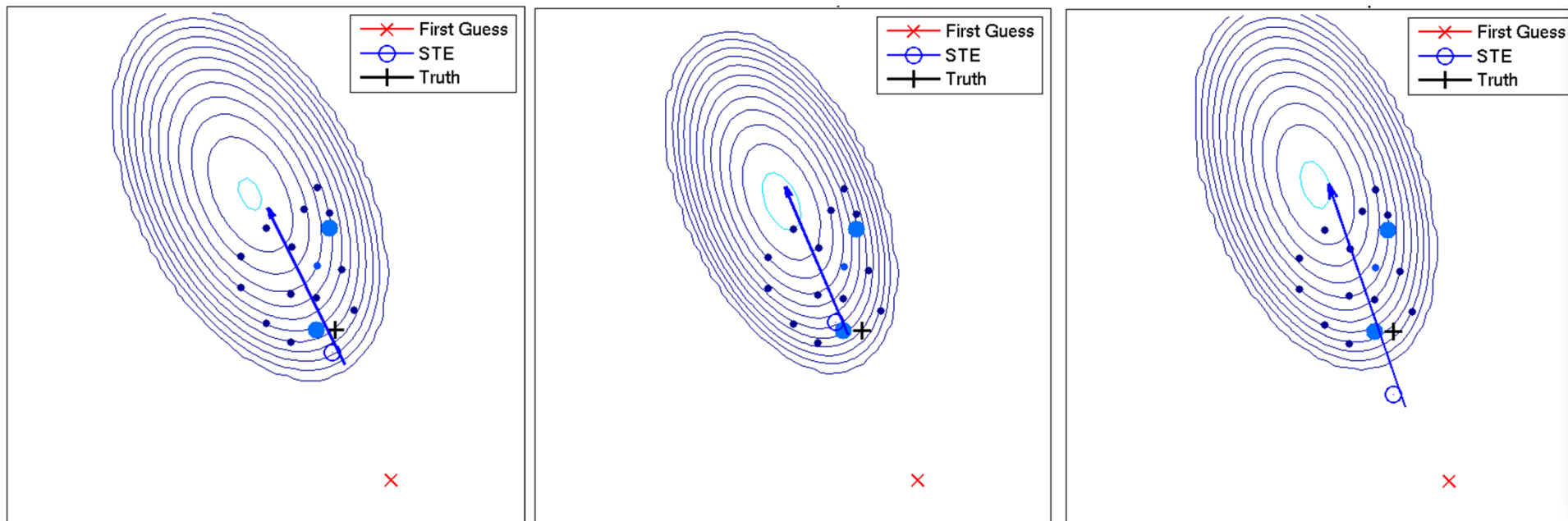


STE (o) moved the source location from SCIPUFF first guess (x) to **224m** from the true source (+)



NCAR

FFT07 Case 37



all parameter estimation
Error = 78m

No time estimation
Error = 99m

no wind estimation
Error = 224m



FFT07 Case 37

	FG	STE	Truth
Q kg/s	5	4.3	4
X m	3013	2814	2826
Y m	1436	1895	1972
Z m	1.6	1.6	1.6
T s	36	9	0
U m/s	6	4.4	??
Θ deg	109	116	??

all parameter estimation

Error = 78m

	FG	STE	Truth
Q kg/s	5	4.8	4
X m	3013	2732	2826
Y m	1436	2005	1972
Z m	1.6	1.6	1.6
T s	36	36	0
U m/s	6	4.0	??
Θ deg	109	113	??

No time estimation

Error = 99m

	FG	STE	Truth
Q kg/s	5	4.6	4
X m	3013	2819	2826
Y m	1436	1748	1972
Z m	1.6	1.6	1.6
T s	36	19	0
U m/s	6	6.0	??
Θ deg	109	109	??

no wind estimation

Error = 224m

Reported observed wind was $U = 6$ m/s, $\theta = 109^\circ$



Summary

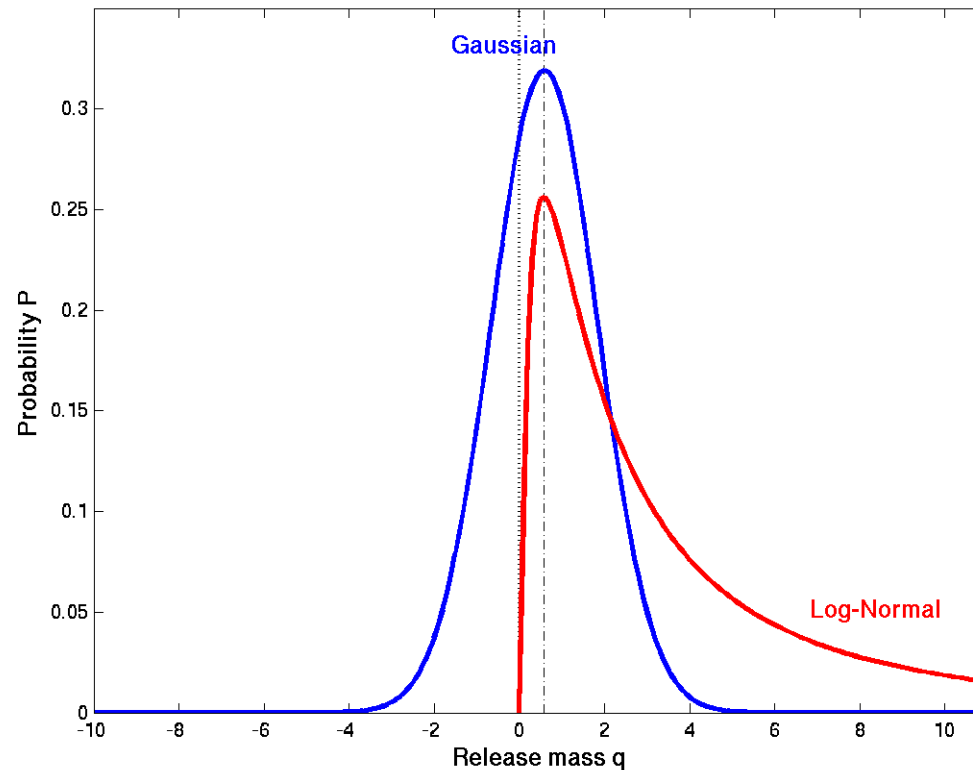
- **All parameter estimation performs best**
- **Observed winds were not consistent with concentration reports**
- **Accurate release time seems less important than accurate winds**
- **Mass estimation must be improved**



Current Work

1) Use of lognormal PDF for mass and concentration:

- One minimization for all
- No negative values





Next

- **Better characterization of uncertainty through the σ 's**
- **Addition of correlations, e.g. wind/position errors**