

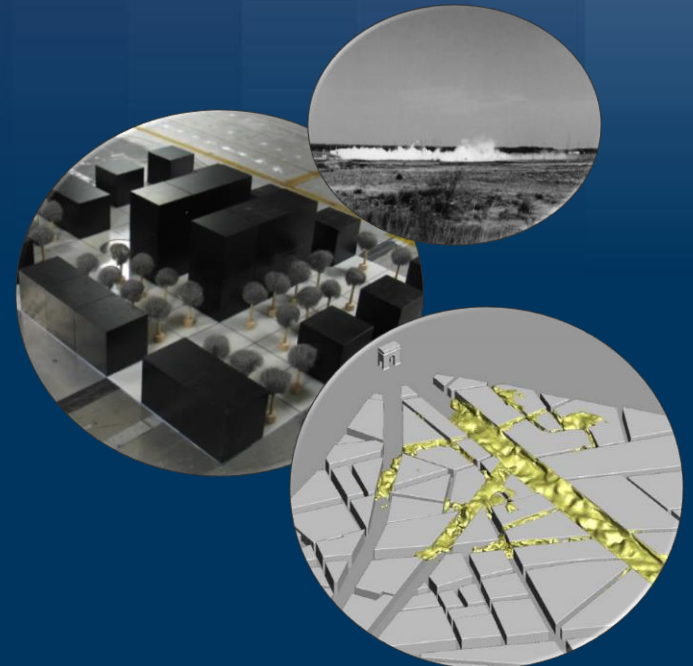
MODITIC

Modelling the dispersion of toxic industrial chemicals in urban environments

INVERSE MODELLING IN URBAN ENVIRONMENTS

Harmo'17
12.05.2016

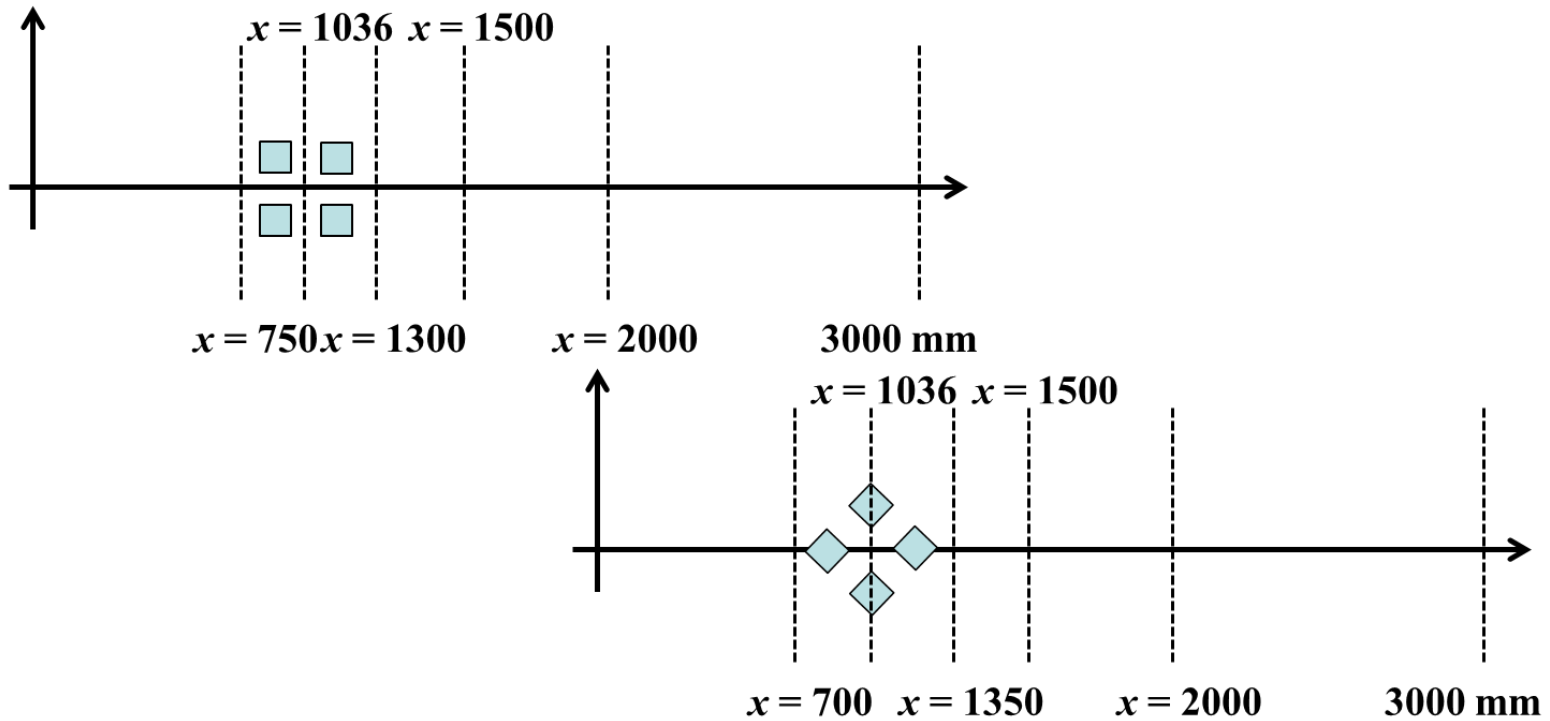
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Jan Burman, Xavier Busch, Jean-Pierre Issartel and Leif Å.
Persson



Contents

- Experimental setup
- Source-sensor relationship
- Model and sensor data, distance functions
- The renormalization method
- The normalized least squares method
- The Bayesian view on least squares
- Results, model comparisons
- Conclusions and remarks

Measurement stations, 4 FFIDs



- Array A:** $(1400, 0), (1600, 0), (2000, 0), (3000, 0)$
Array B: $(2000, -320), (2000, -100), (2000, 100), (2000, 320)$
Array C: $(2000, -320), (2000, 320), (3000, -320), (3000, 320)$
Array D: *as A with rough surface*

Simple array

Arrays used for 4FFID experiments

Detector arrays

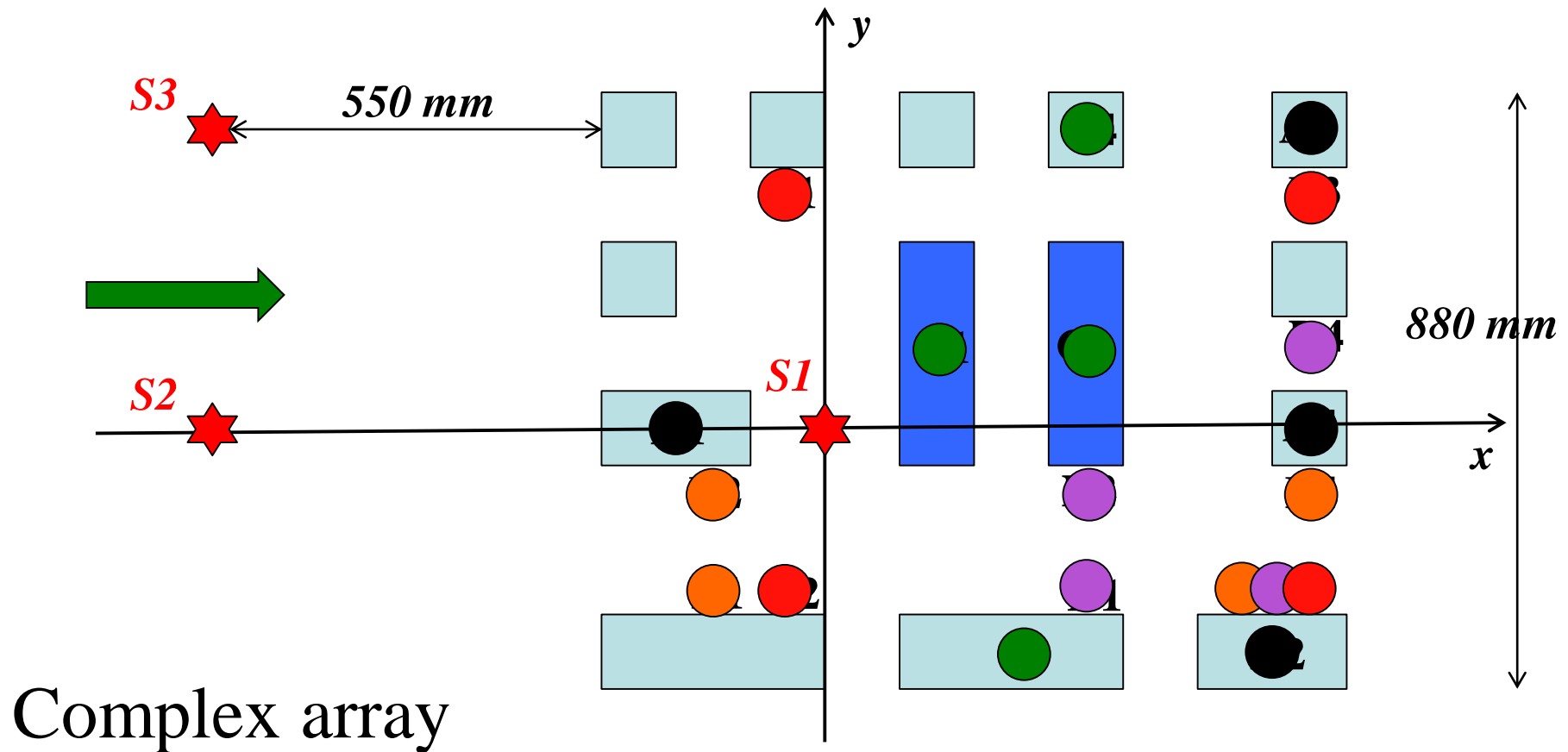
● *Array A (roof level)*

● *B (street level)*

● *C (roof)*

● *D (street)*

● *E (street)*



Source-sensor relationship

- Stationary plume from continuous point source with constant release rate
- Source parameters to estimate: x, y, z, q
- Forward model plume: fixed source, sensor positions at grid points
- Adjoint model plume: fixed sensor, source positions at grid points
- Adjoint model usually preferred for source estimation for computational efficiency

Model and measured data

- Sensors numbered $i=1,2,3,4$
- Model data: $c_i = q \chi_i(x,y,z)$
- $\chi_i(x,y,z)$ grid function, adjoint plume for sensor i
- Model data vector $\mathbf{c} = [c_1, c_2, c_3, c_4]$
- Measured data vector $\mathbf{d} = [d_1, d_2, d_3, d_4]$
- Adjoint plume vector function
 $\mathbf{X} = [\chi_1(x,y,z), \chi_2(x,y,z), \chi_3(x,y,z), \chi_4(x,y,z)]$

The source estimation problem

- Optimization problem
- Find (x,y,z,q) minimizing *distance* between model data vector $\mathbf{c}(x,y,z,q)$ and measured data vector \mathbf{d}
- Methods differ by
 - how distance is defined
 - numerical method for approximating (x,y,z,q)

Distance functions

- Issartel's renormalization distance: a weighted Euclidean norm based on the *visibility function* φ :

$$(\mathbf{d} - \mathbf{c})^T H_{\varphi}^{-1} (\mathbf{d} - \mathbf{c})$$

- Normalized Euclidean distance (Mahalanobis distance) D : $D^2 = \sum_i (d_i - c_i)^2 / c_i^2$

Visibility function and weights

- The *visibility function* $\varphi(x,y,z)$ is constructed from the adjoint plumes χ_i for all sensors by an entropy minimization principle
- Measuring the "visibility" from the sensor network
- The elements of the weight matrix H_φ are computed by numerical integration of products $\chi_i \chi_j / \varphi$.

Computational procedure

➤ By the particular properties of φ , the problem is reduced to a simpler maximization problem:

➤ Compute *distributed* renormalization source:

$$\sigma = \mathbf{d}^T H_{\varphi}^{-1} \mathbf{X}$$

on grid.

➤ Compute point source location (x,y,z) :

$$\sigma(x,y,z) = \max \sigma$$

➤ Compute point source release rate:

$$q = \sigma(x,y,z) / \varphi(x,y,z)$$

Normalized least squares

- Bilevel optimization
- Compute optimal $q = q^*(x,y,z)$ for each (x,y,z) in grid

- Obtain *envelope grid function*

$$c_i^* = q^*(x,y,z) \chi_i(x,y,z)$$

- Minimize the *minimum value grid function*

$$V(x,y,z) = \sum_i (d_i - c_i^*)^2 / (c_i^*)^2$$

Normalized least squares with regularization

• Add penalization term $\lambda q^*(x,y,z)$, penalizing large release rates:

• Minimize grid function

$$V(x,y,z) = \sum_i (d_i - c_i^*)^2 / (c_i^*)^2 + \lambda q^*(x,y,z)$$

• We have used $\lambda=1$ in this study.

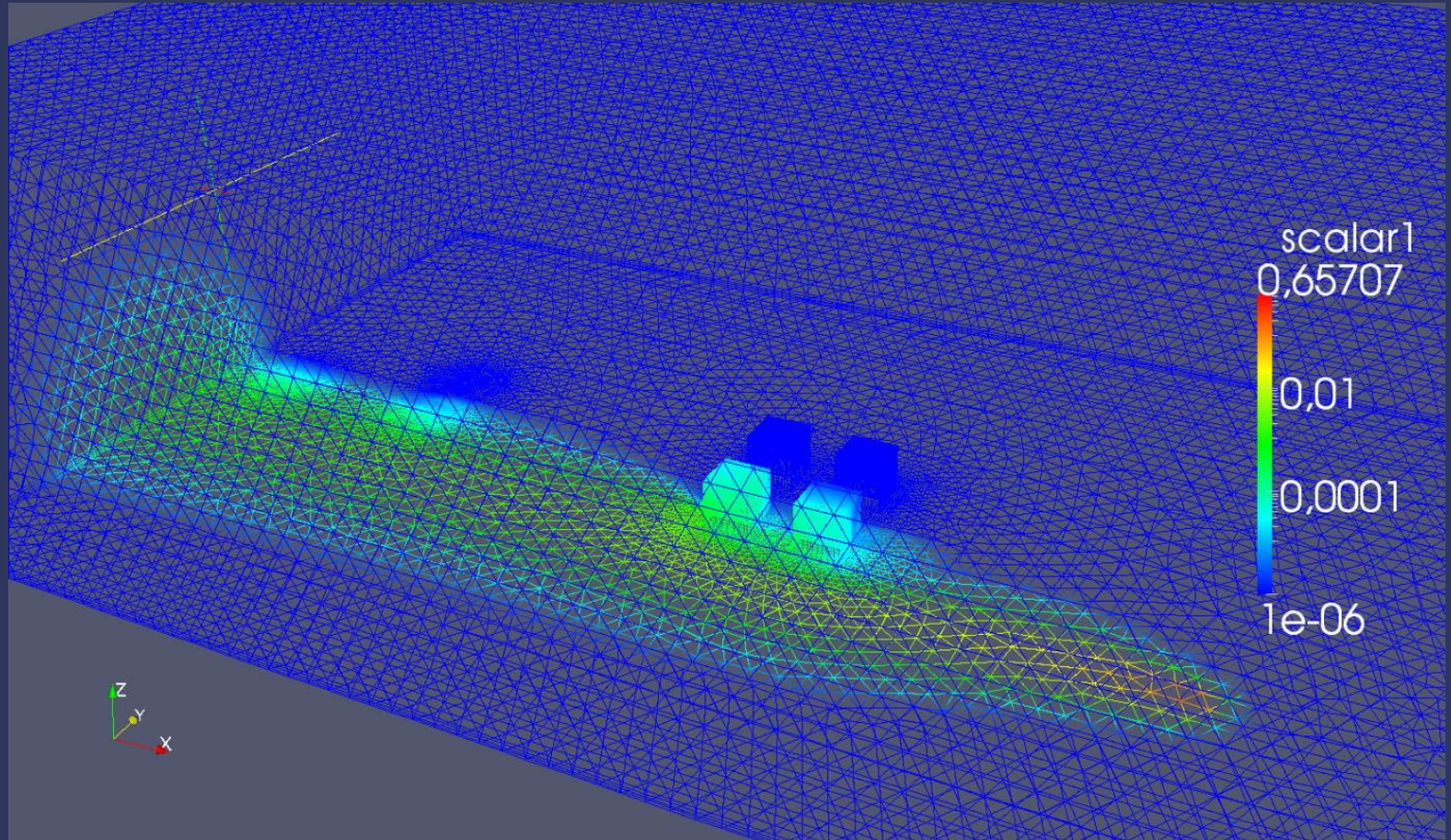
The Bayesian view on LS

- Minimization problem: $\min D^2$
- Equivalently, $\max \exp(-D^2)$, may be interpreted as a maximum likelihood estimation (MLE) problem
- By Bayes formula, $\exp(-D^2)$ may be interpreted as a posterior density (with noninformative prior)
- Regularization may be introduced as a (non-constant) prior density.

Adjoint plumes

- RANS advection-diffusion models
- Adjoint obtained from forward model by reversing advection and preserving diffusion (self-adjoint)
- RANS-solvers used:
 - Phoenics
 - Code Saturne v4

Adjoint plumes – Code Saturne



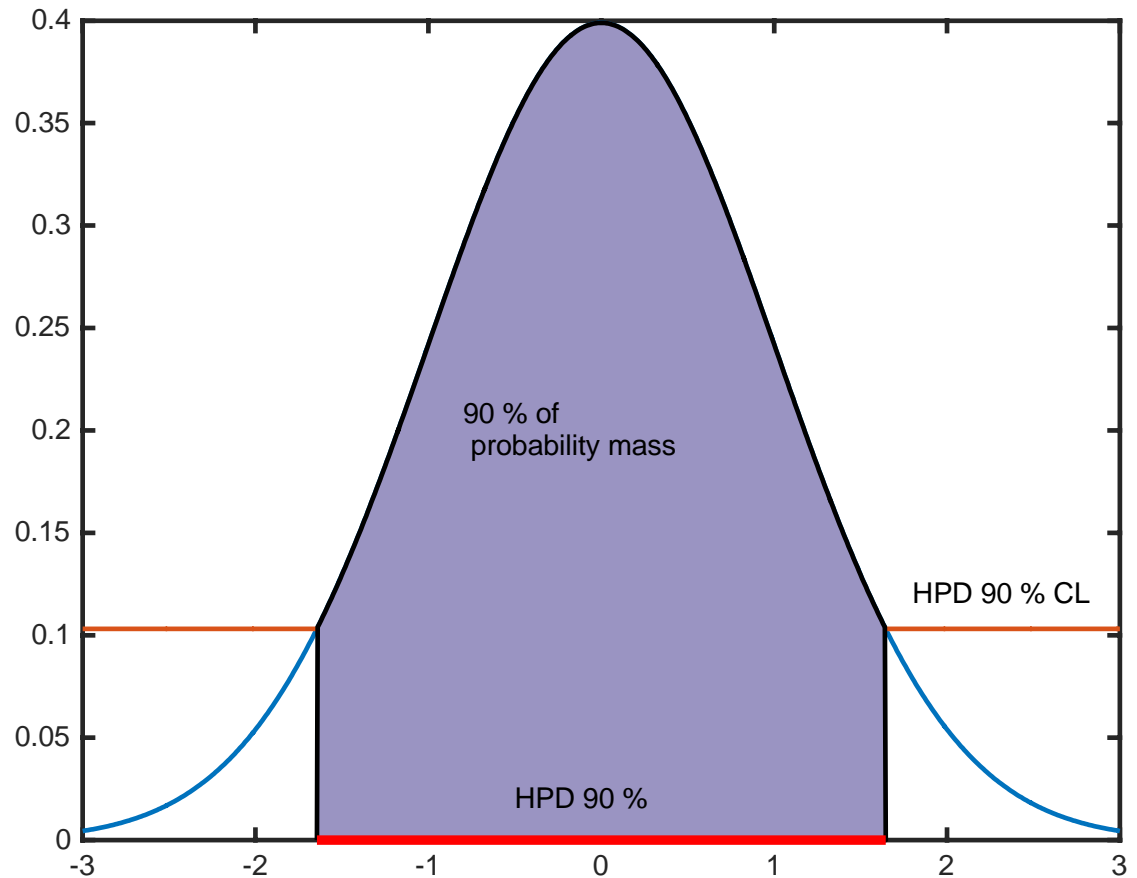
Results

- Source estimates (x,y,z,q) obtained by maximizing
 - The posterior densities (with or without regularization)
 - The distributed renormalization source
- Isosurface plots of objective functions
- Selected windtunnel data:
 - 5 configurations of the complex array.
 - 6 configurations of the simple array
 - 2-4 datasets/configuration, total number 24
 - PHOENICS adjoints; Code Saturne adjoints pending

3D and 2D results

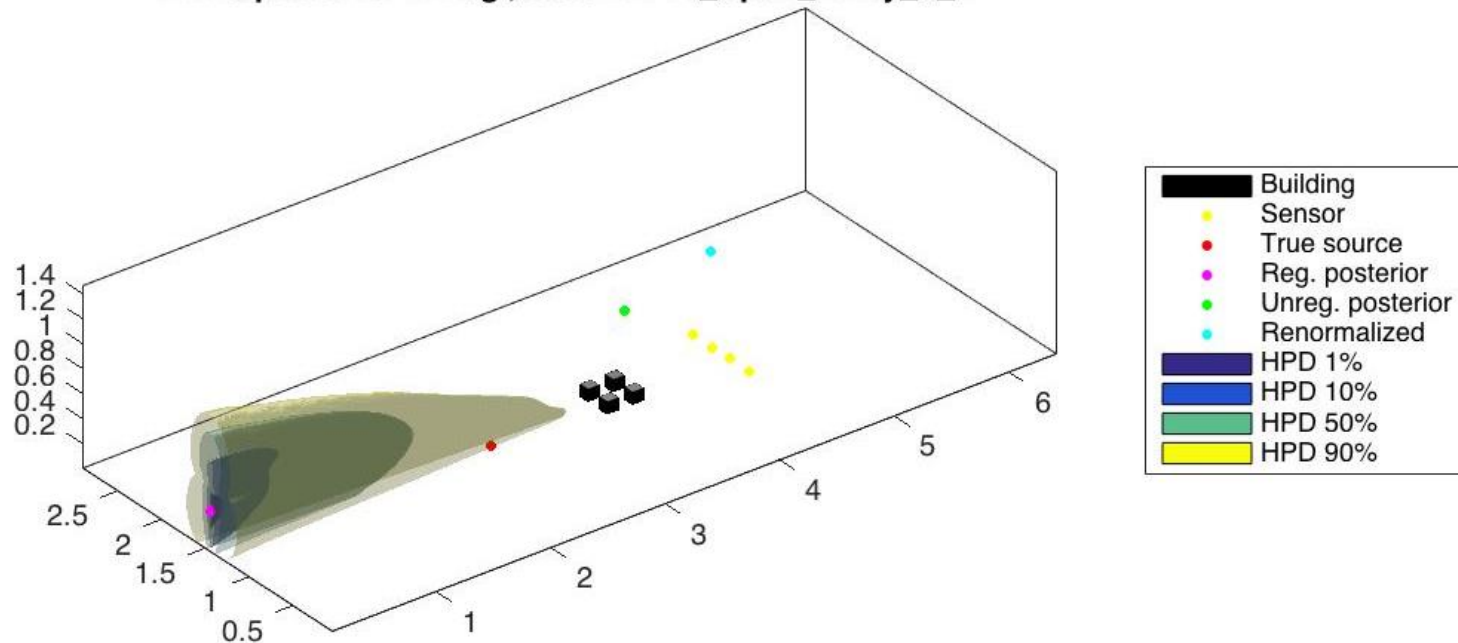
- 3D: Possibly elevated source
 - Source parameters (x,y,z,q)
 - Posteriors and renormalization source computed on 3D grid (x,y,z)
- 2D: Assuming ground source
 - Source *parameters* (x,y,q)
 - Posteriors and renormalization source computed on 2D grid $(x,y), z=0$
- Level sets presented as highest posterior density (HPD) domains

Highest posterior density (HPD) domains



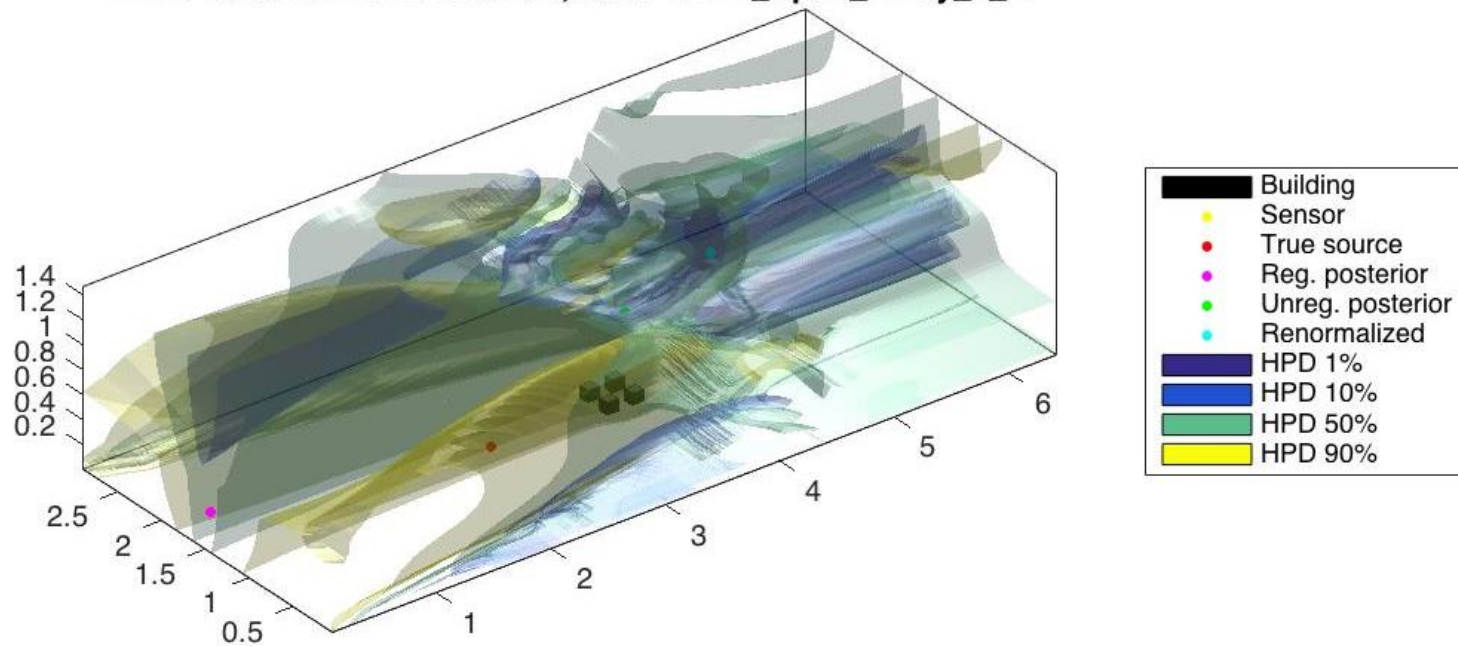
Isosurfaces, 3D posterior w/ reg.

Enflo posterior w/ reg., case 4FFID_Span_Array_1_2



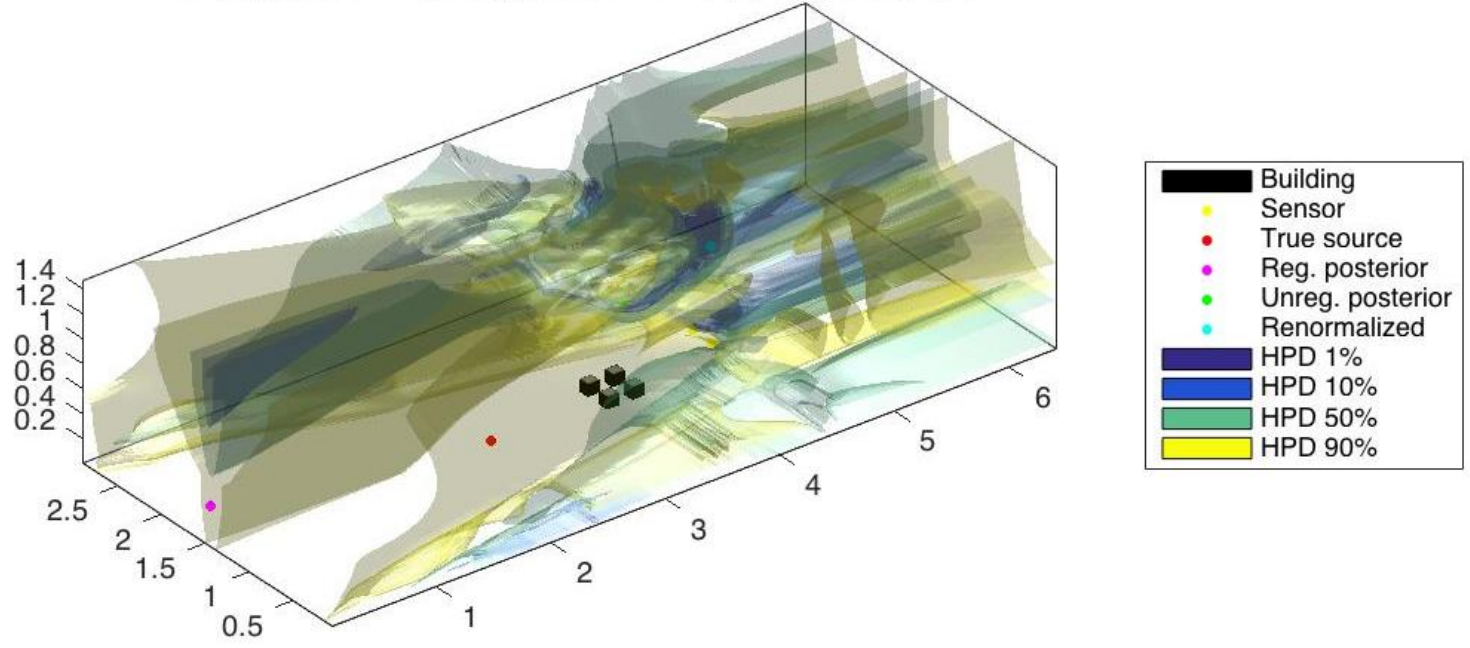
Isosurfaces, 3D renorm. source

Enflo renormalization source, case 4FFID_Span_Array_1_2

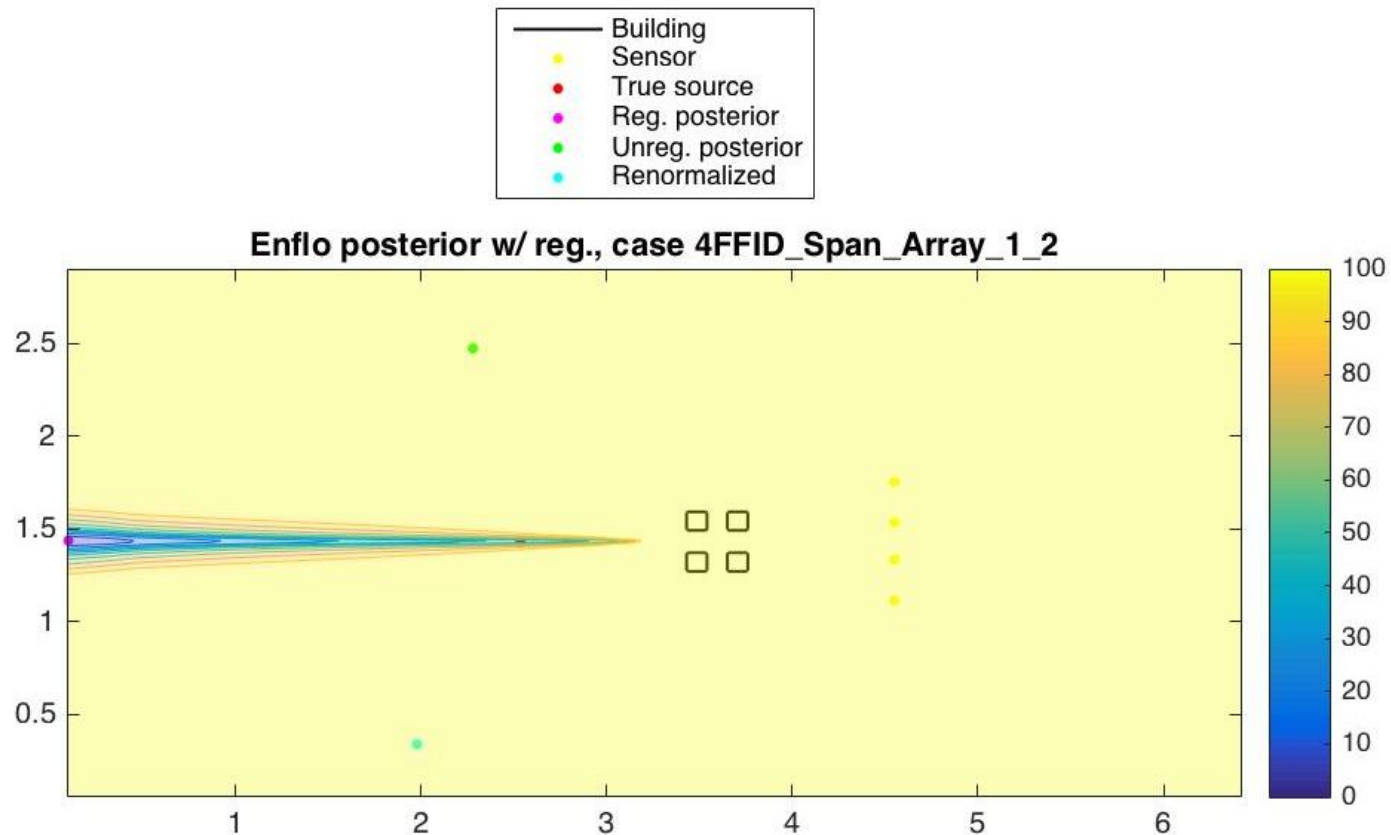


Isosurfaces, 3D posterior w/o

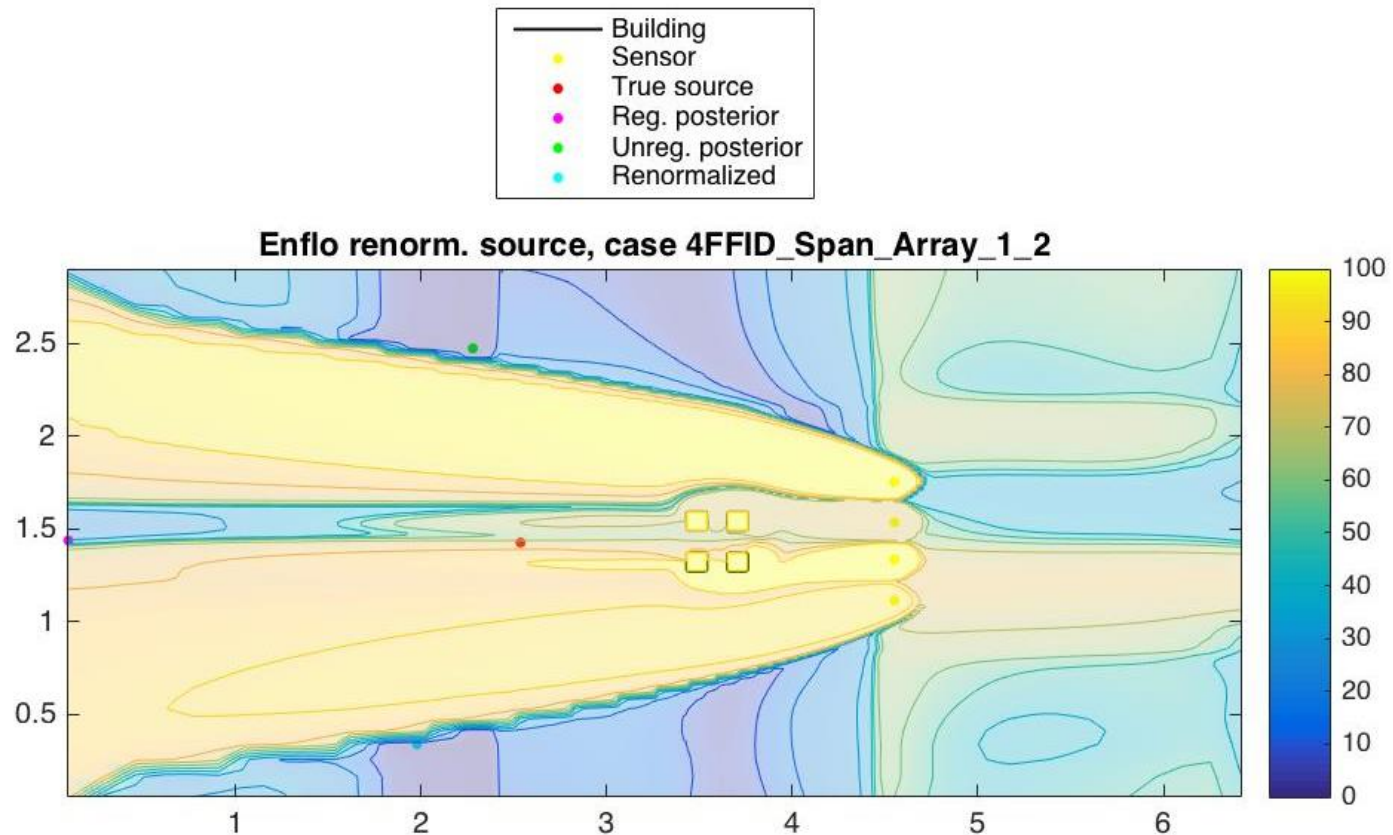
Enflo posterior w/o reg., case 4FFID_Span_Array_1_2



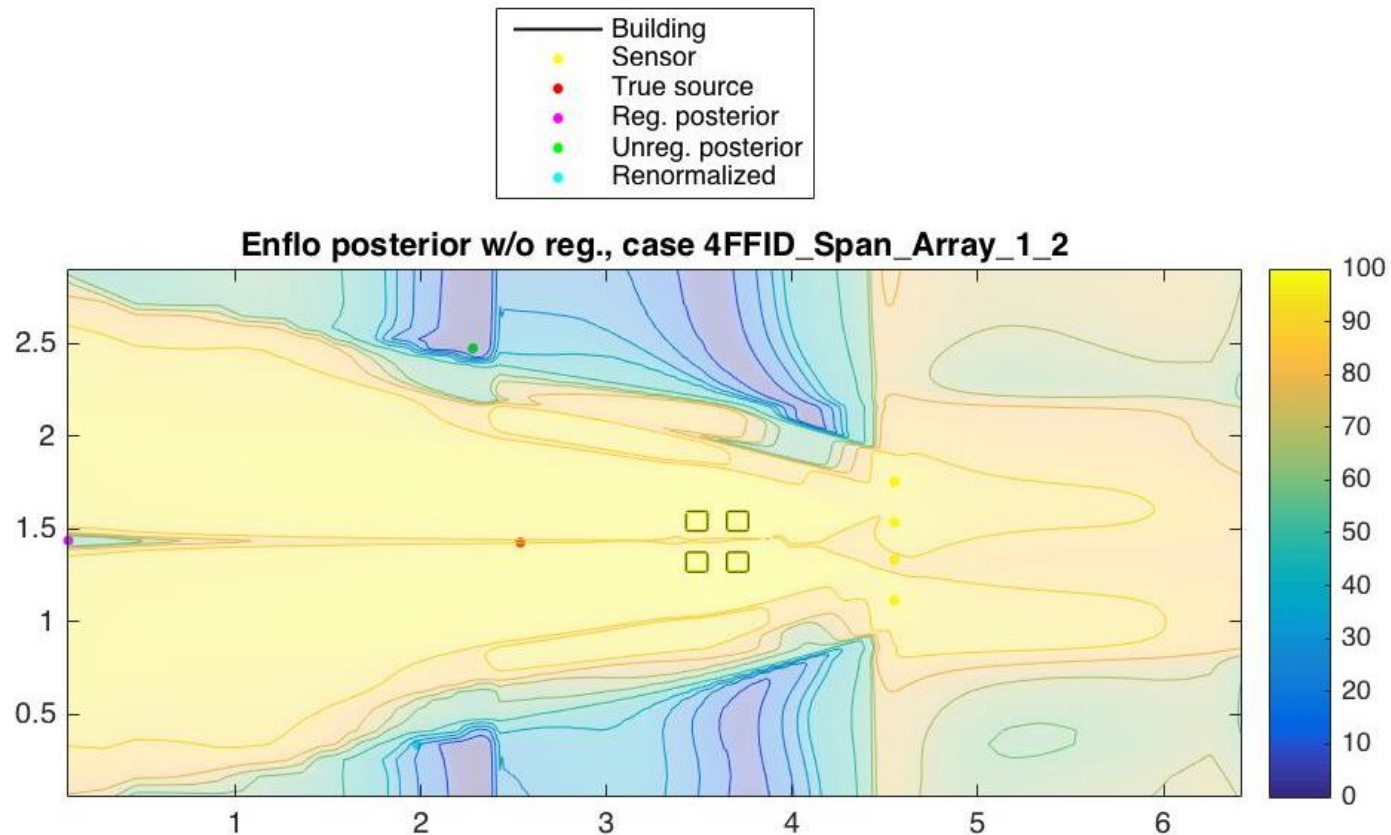
Isocurves, 2D posterior w/ reg.



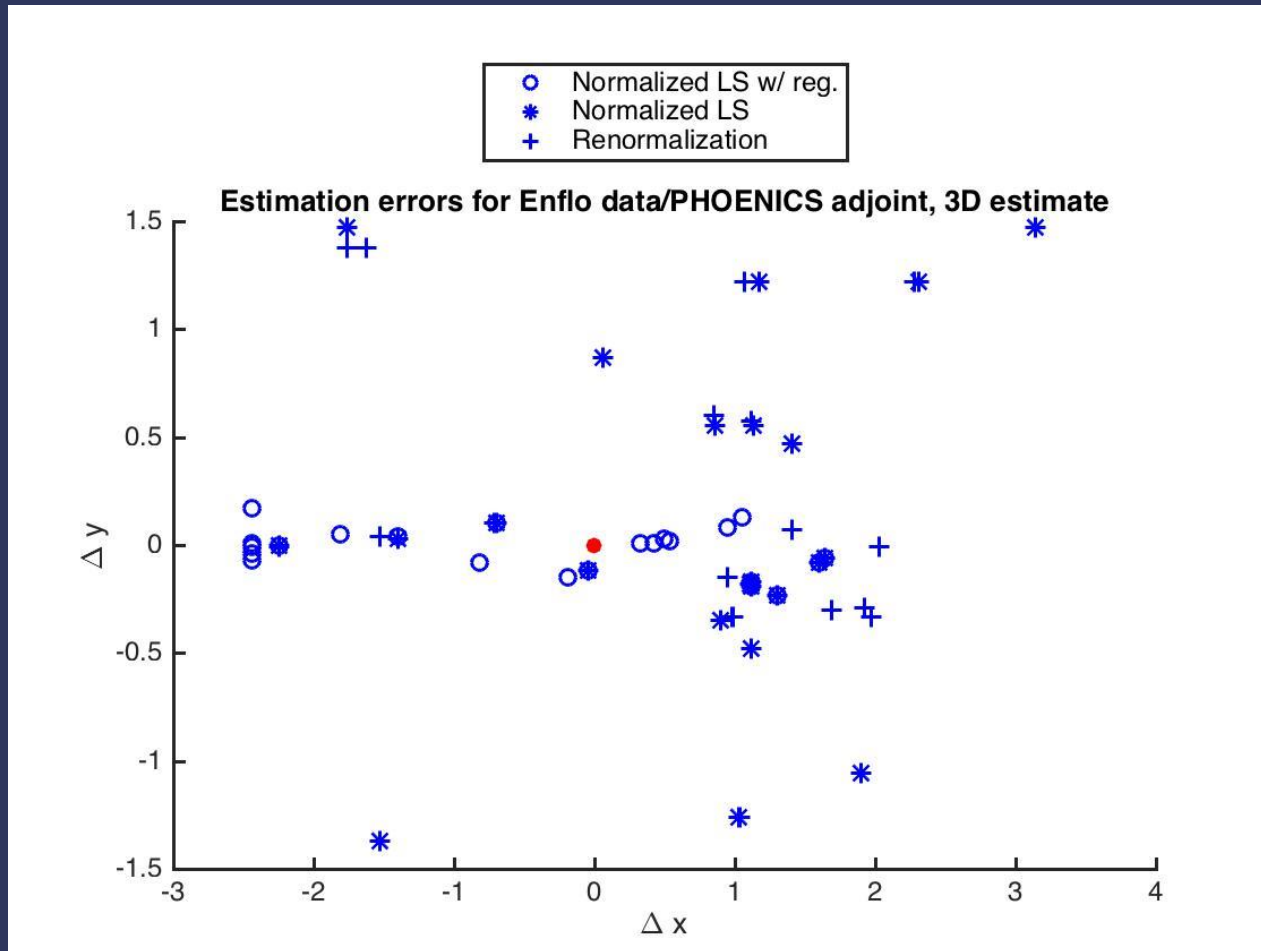
Isocurves, 2D renorm. source



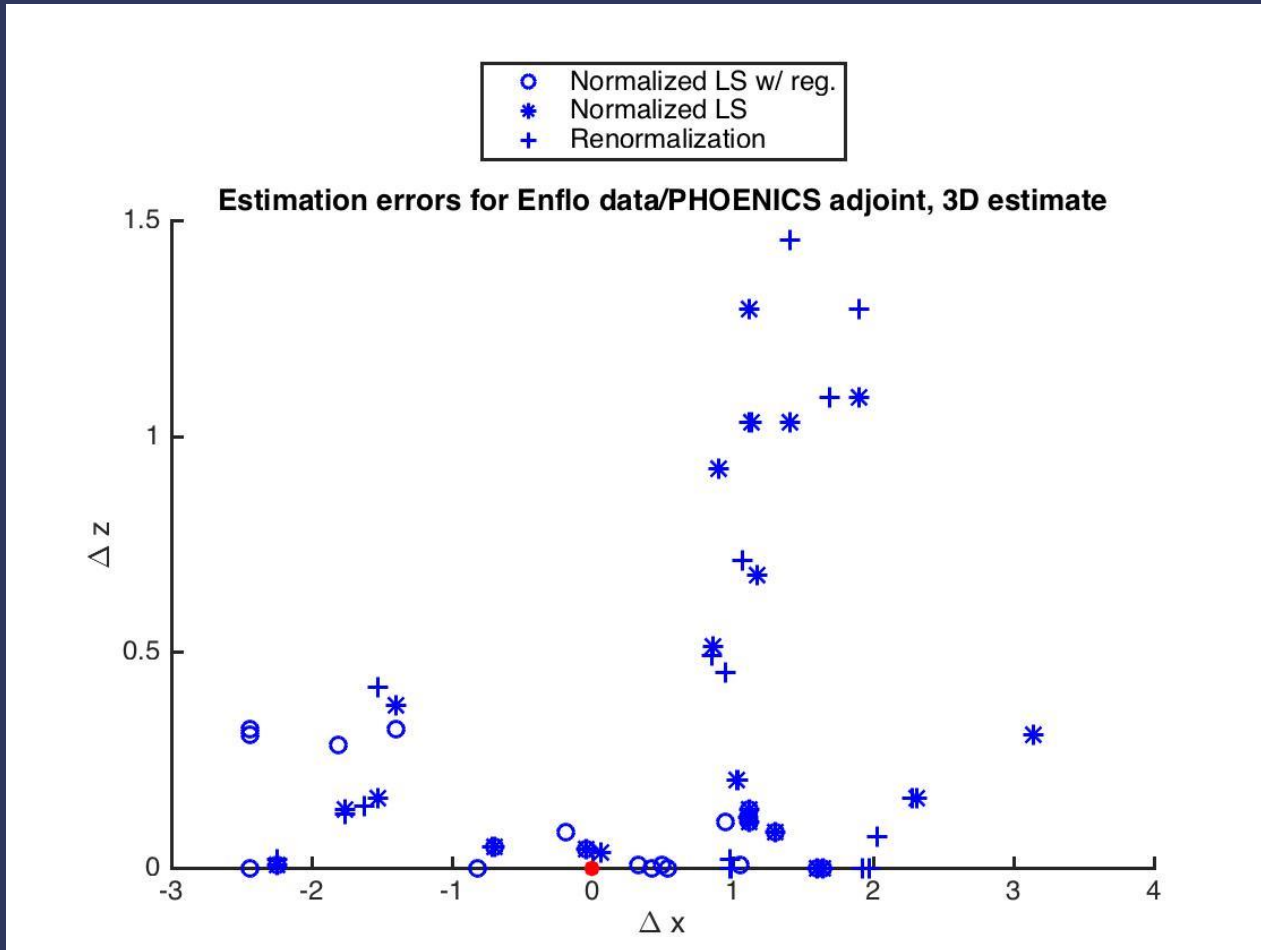
Isocurves, 2D posterior w/o reg.



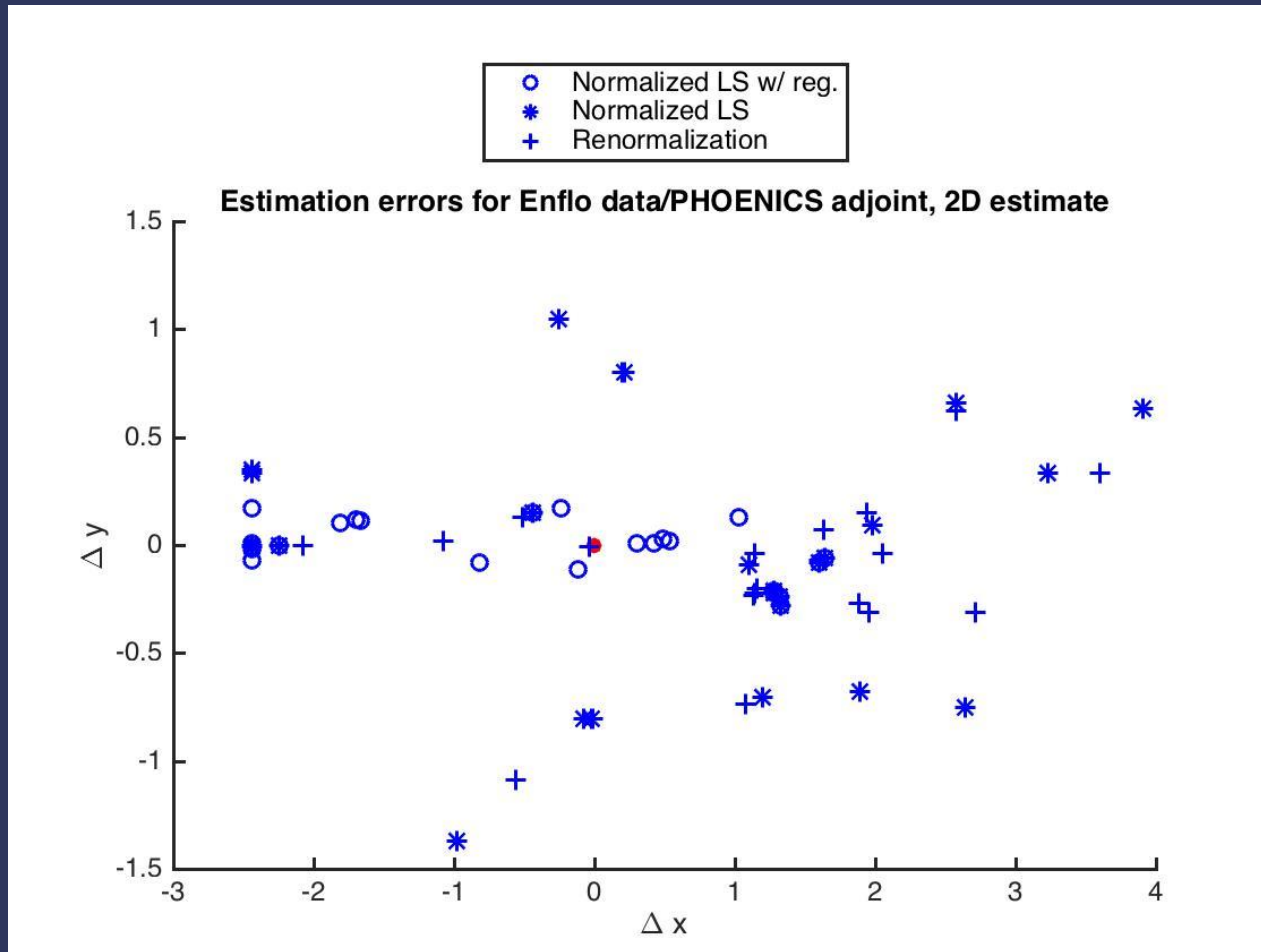
3D comparison, (x,y) errors



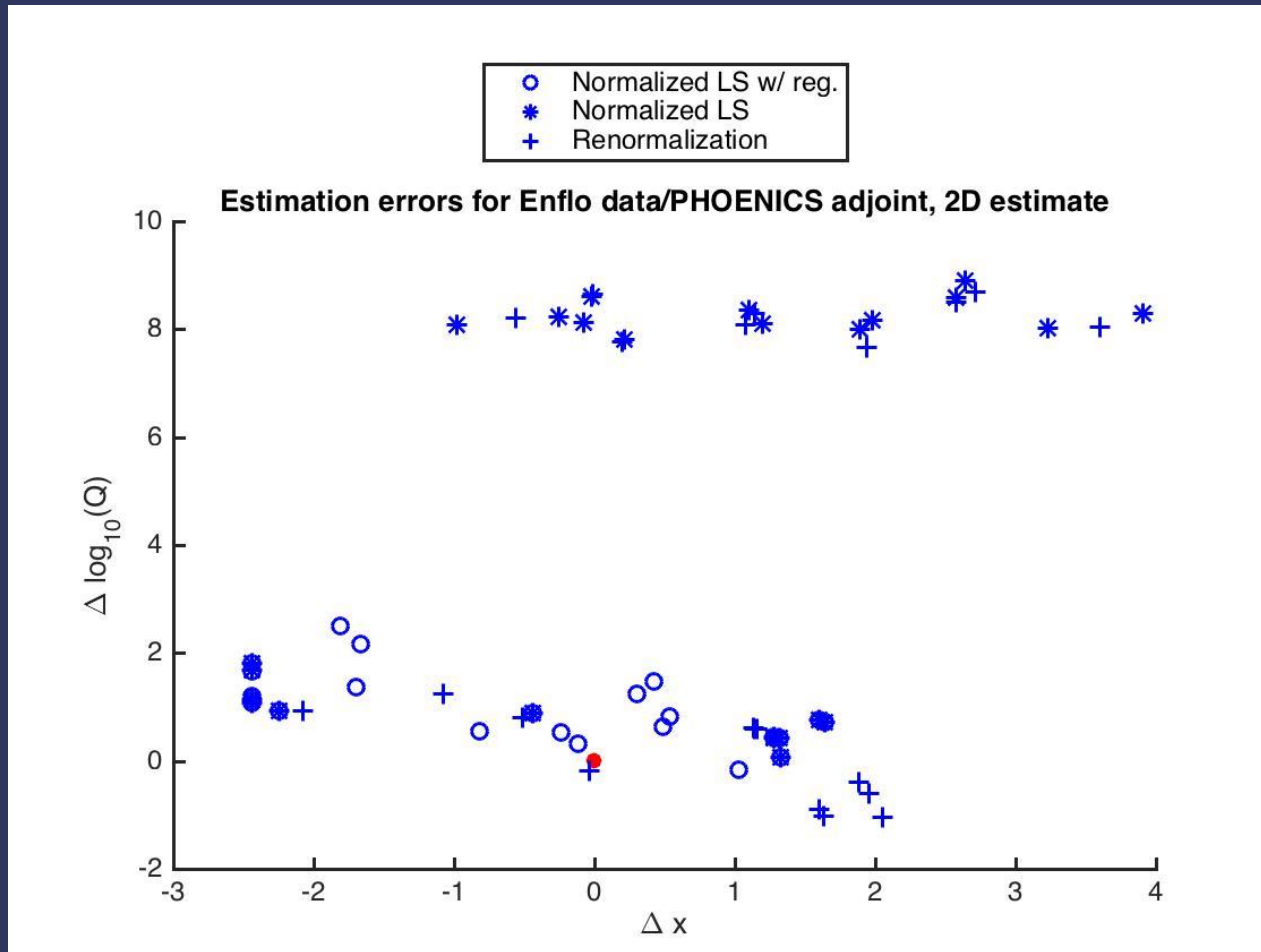
3D comparison, (x,z) errors



2D comparison, (x,y) errors



2D comparison, (x, q) errors



Mean absolute errors, 24 data sets

3D	LS with reg.	Renormalization	LS
x	1.29	1.47	1.35
y	0.085	0.63	0.62
z	0.083	0.39	0.62
$\log_{10}(q)$	0.87	2.15	4.97

2D	LS with reg.	Renormalization	LS
x	1.35	1.60	1.61
y	0.10	0.32	0.45
$\log_{10}(q)$	0.97	4.17	4.86

Some conclusions and remarks

- All methods suffers from outliers
- Regularization suppresses outliers in y, z, q but not so much in x
- Lack of regularization gives complicated objective functions and hard optimization problems, reflecting the ill-posedness of the inverse problem
- Implementation has been verified on synthetic data (not presented here)

Thank you!

